

dark matter distribution in the Milky Way halo

- 1) observational evidence
- 2) substructure
- 3) density profiles

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Sept 12, 2007

TAUP 2007, Sendai

What is dark matter ?

Evidence for DM on a wide range of scales:

Galaxy cluster dynamics (Zwicky, 1933)

Galaxy rotation curves

X-rays from galaxy groups and clusters

Kinematics of stellar halos,

satellite galaxy and globular cluster systems

Dwarf galaxy velocity dispersions

Strong and weak lensing

...

CMB, LSS, SN Ia, BBN → LambdaCDM

WMAP-3yr (alone, flat prior):

$\Omega_m = 0.238$

of which Ω_b is only 0.042

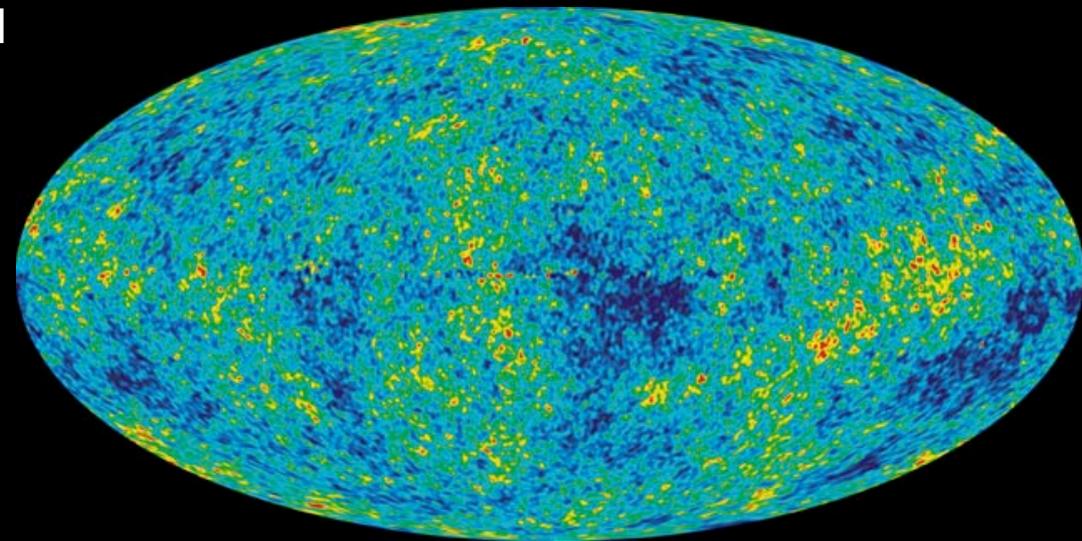
with small errors (less than 10%)

DM is “cold”, or at least “cool”:

Lyman-alpha forest, early reionisation



Coma, Credit: Lopez-Cruz et al



Credit: NASA/WMAP

→ 83% of the clustering matter is non-baryonic, quite “cold”, dark matter

We don't know yet what DM is, but we can still simulate its clustering ...

evidence for DM in the Milky Way

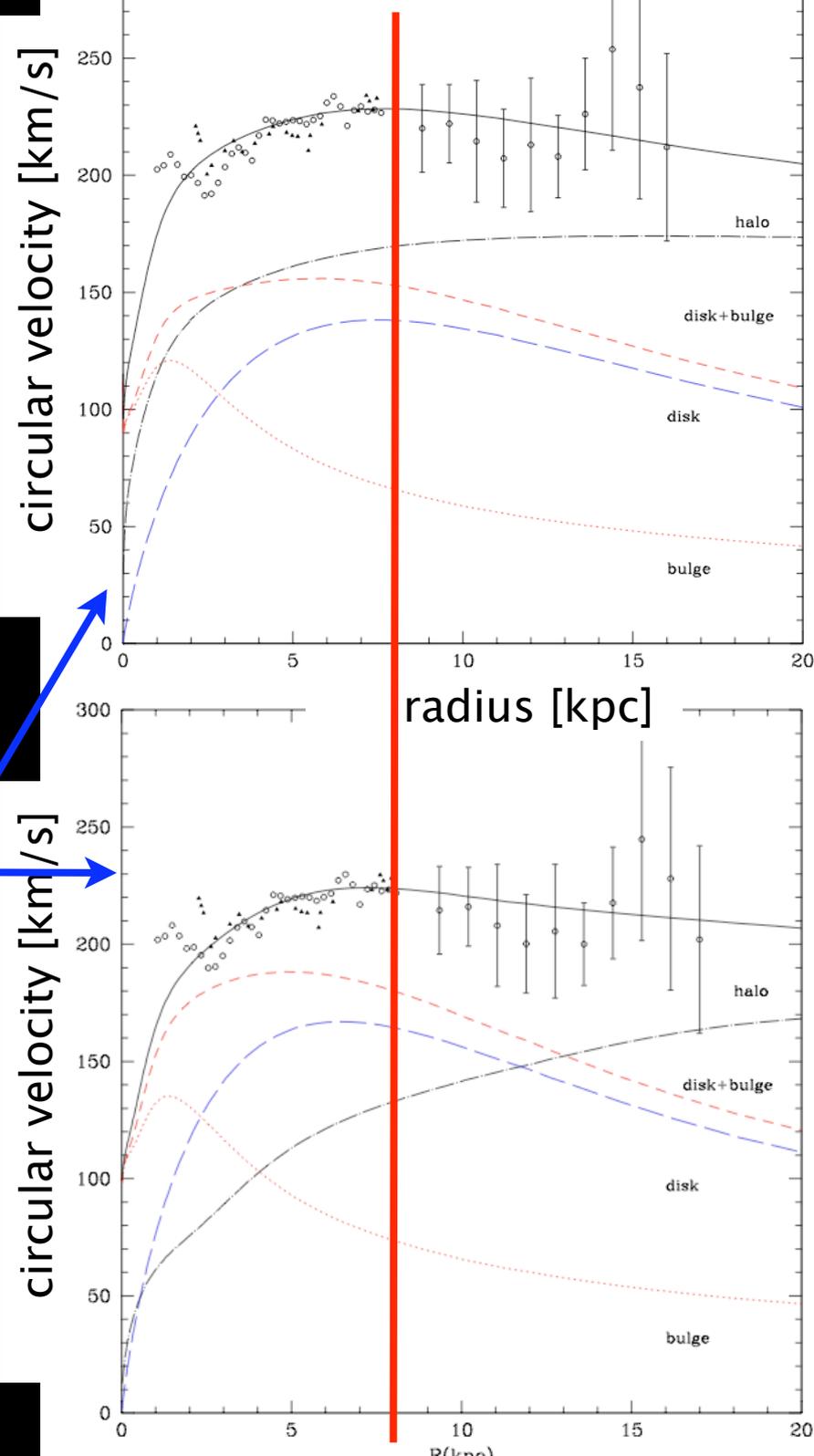
using rotation curve, satellites, local vertical force, Klypin et al 2001 find:

Virial mass $M_{\text{vir}} (M_{\odot}) = 1.0 \times 10^{12}$
preferred range: 0.7 - 2.0

Concentration = 12
preferred range: 10 - 17

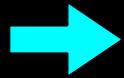
no exchange of angular momentum
with exchange

significant amounts of DM inside 8 kpc
35 to 60 percent of total enclosed mass



evidence for DM in the Milky Way

same two models from Klypin et al 2001



significant amounts of DM at 8 kpc
about 0.007 to 0.012 Msun/pc³

standard halo:

$$0.3 \text{ GeV/cm}^3 = 0.008 \text{ Msun/pc}^3$$

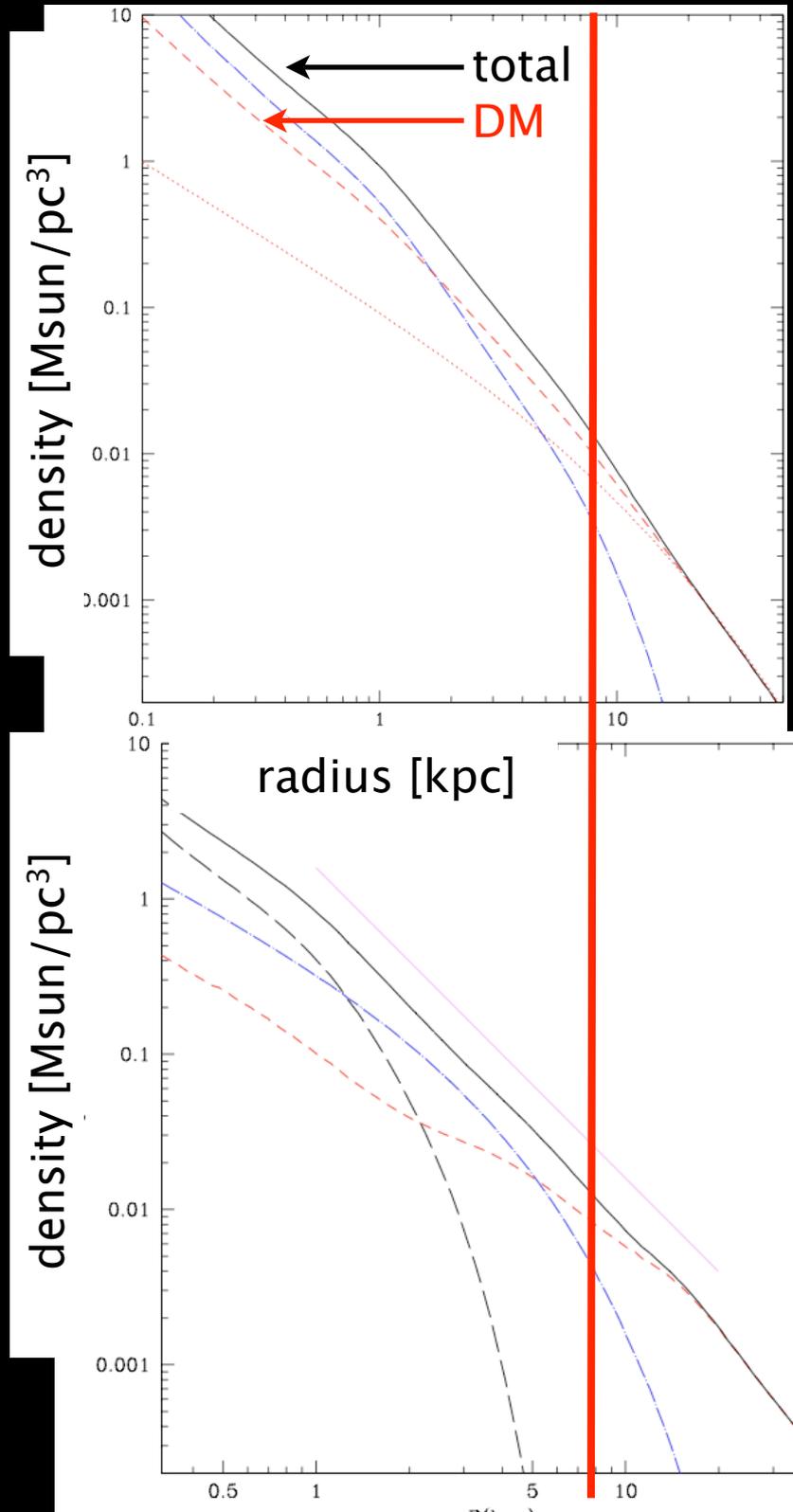
local surface density (Kuijken&Gilmore1989/91):

$$\Sigma_{\text{stars+gas}} = 48 \pm 8 \text{ M}_{\odot}\text{pc}^{-2}$$

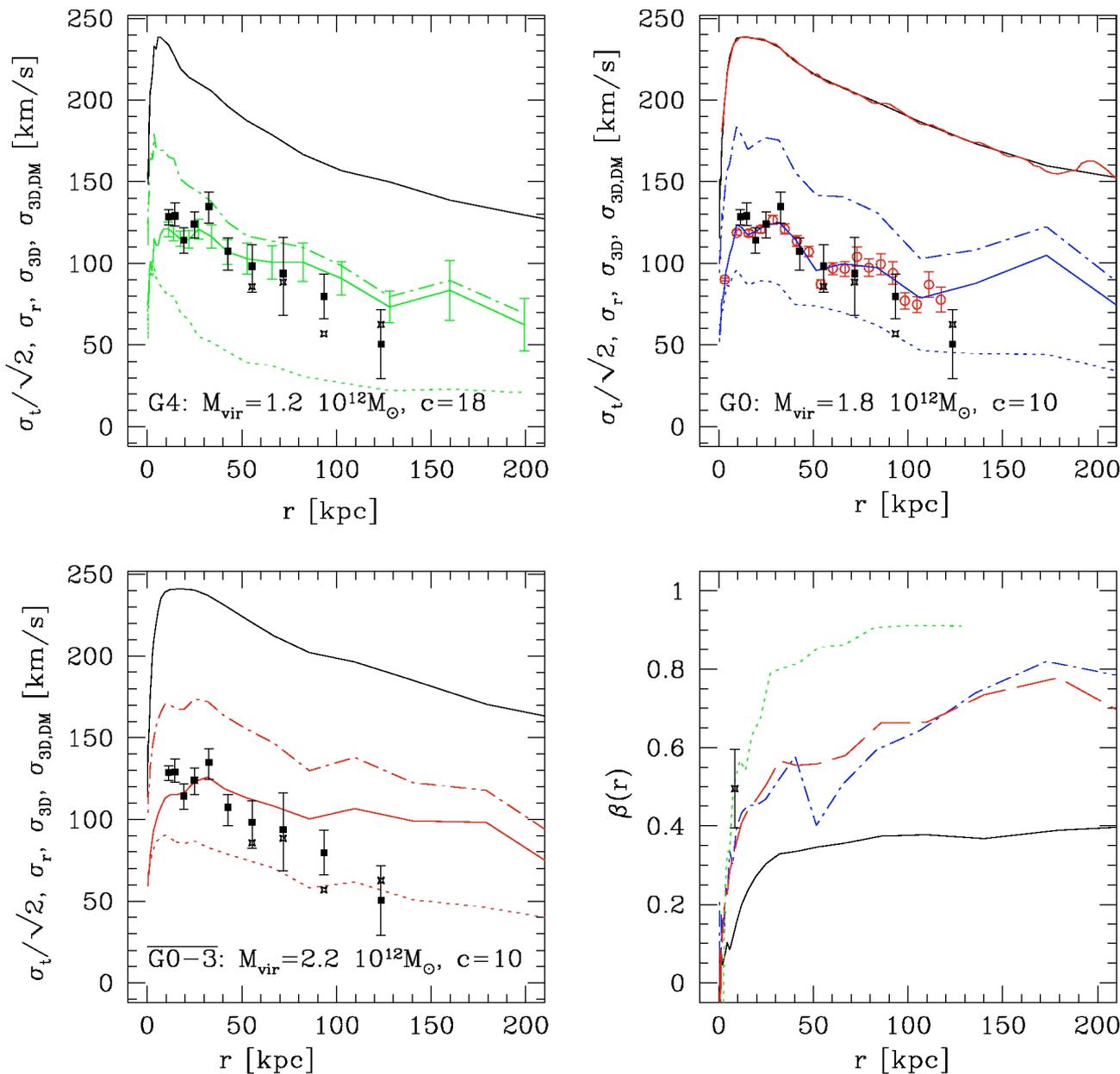
$$\text{total (inside 1.1 kpc)} = 71 \pm 6 \text{ Msun/pc}^2$$

also gives a mean local DM density of
about 0.01 Msun/pc³

(but, how smooth is DM locally ???)



DM around the Milky Way: stellar halo radial velocities



cosmological stellar halo models fit the observed kinematics from G. Battaglia et al 2005

The outer halo is not well constrained yet:
 low M_{vir} / high c
 high M_{vir} / low c
 both possible

$$\beta = 1 - 0.5\sigma_t^2/\sigma_r^2$$

depends on tracer profile slope as in Hansen&Moore 2004
 local stellar halo: $\beta \sim 0.5$
 local DM: $\beta \sim 0.12$ (via lactea)

great observational advances expected:
 RAVE, SDSS SEGUE, GAIA, SIM(?), ...

from JD, Madau, Moore 2005

CDM around the Milky Way: stellar halo radial velocities

local escape velocity v_{esc}

using the RAVE survey and archival data from Beers et al 2000
M. C. Smith et al 2007 find:

$$498 \text{ km s}^{-1} < v_{\text{esc}} < 608 \text{ km s}^{-1}$$

at 90 % confidence

$$v_{\text{esc}} \gg 1.41 \times 220 \text{ km/s}$$

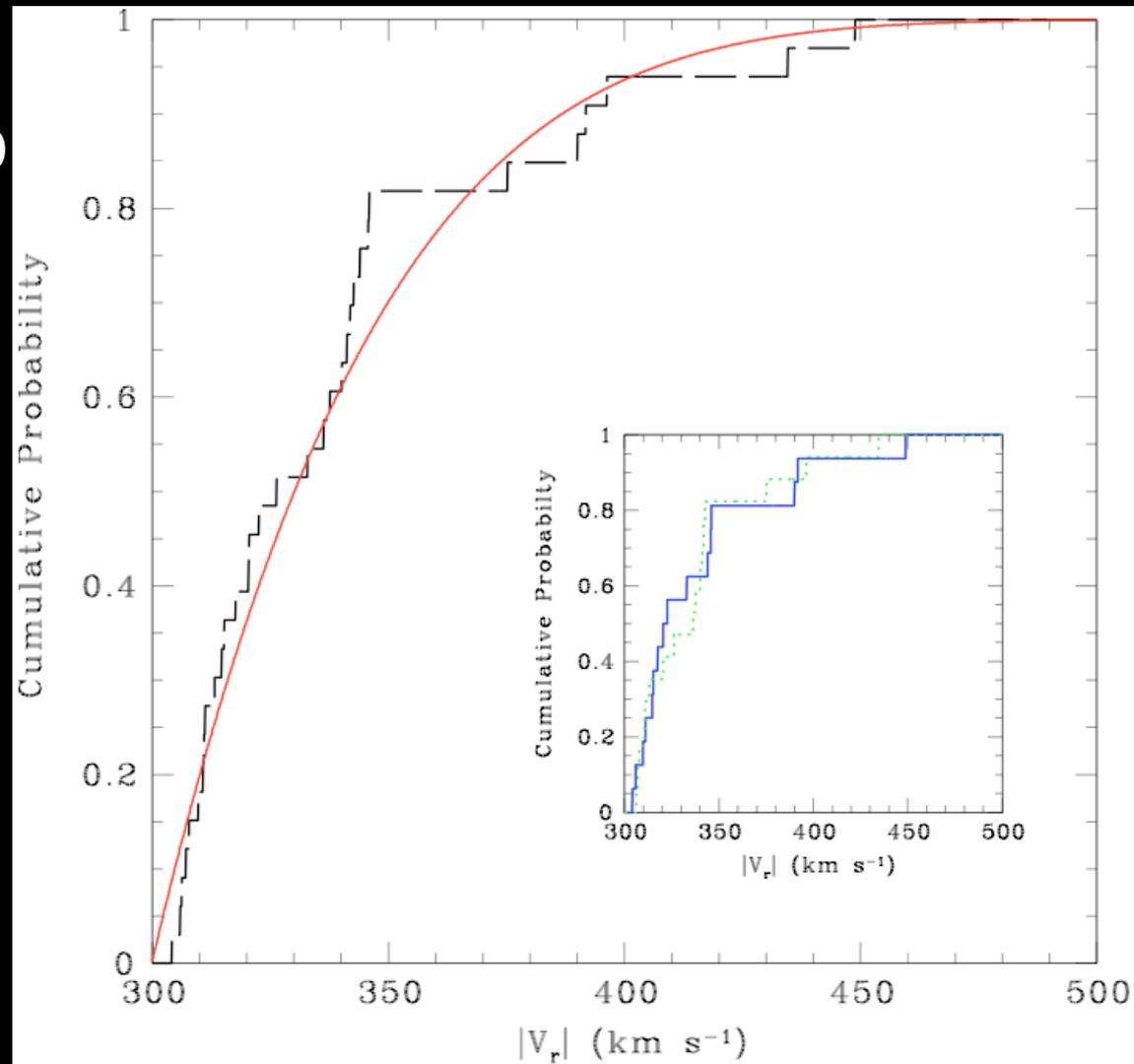
➔ there must be a massive halo around the Milky Way!

comparison with model stellar halos gives virial masses of:

$$1.42^{+1.14}_{-0.54} \times 10^{12} M_{\odot}$$

at 90 % confidence

if stellar $v_{\text{esc}} < \text{dynamical } v_{\text{esc}}$
these masses would be only lower limits



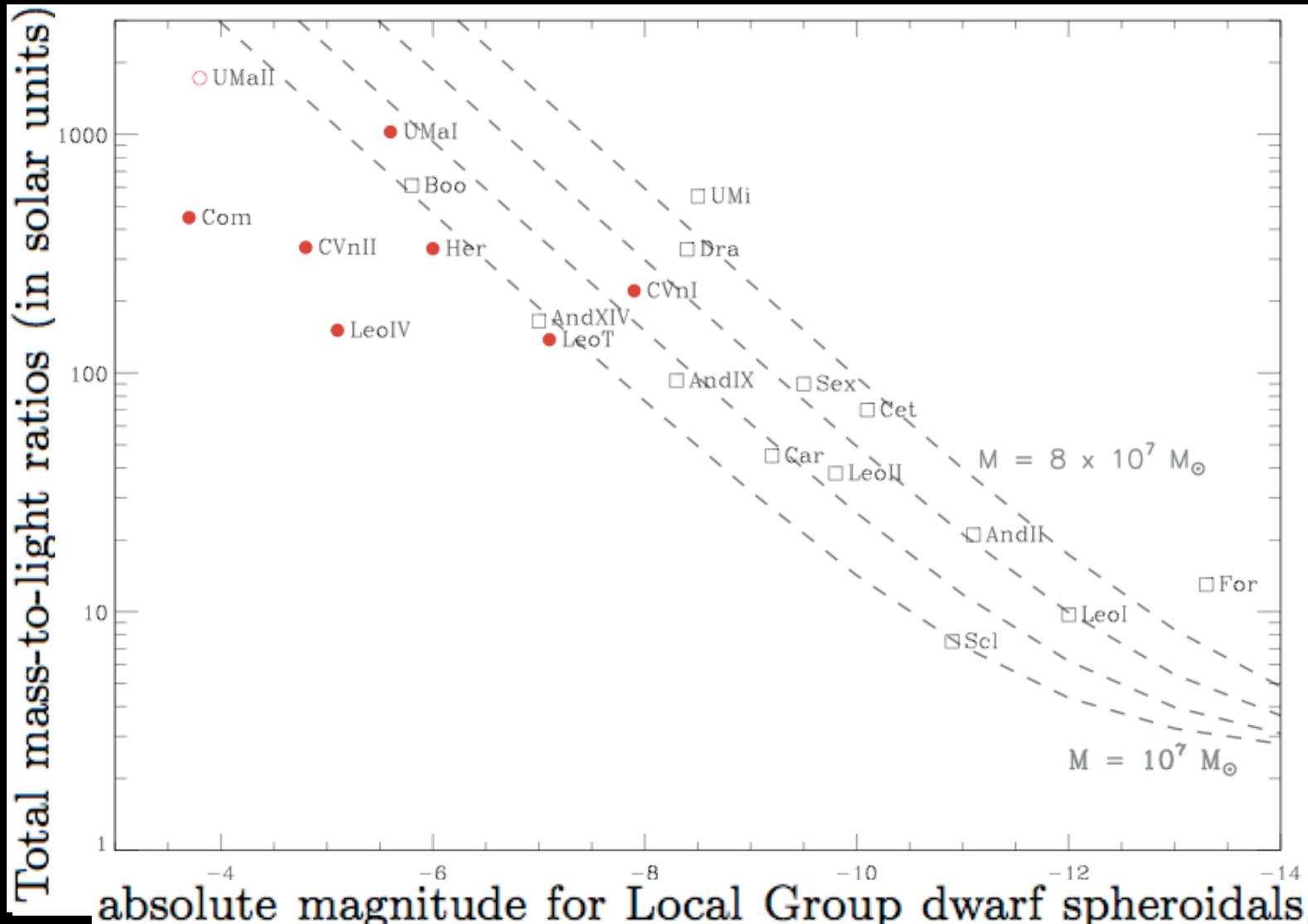
evidence for DM substructure in the Milky Way

survival of faint, old Local Group dSphs in the tidal field of the Milky Way

their kinematics confirm that they are dominated by dark matter (Simon&Geha 2007)

higher mass-to-light-ratios for fainter systems

might go to infinity on smaller scales ...



from Simon & Geha 2007

2) simulating structure formation

our approach:

collision-less (pure N-body, dark matter only) simulations

- treat all of Ω_m like dark matter
- bad approximation near galaxies, OK for dwarf galaxies and smaller scales
- simple physics: just gravity
- allows high resolution
- no free parameters (ICs known thanks to CMB)

→ accurate solution of the idealized problem

complementary approach:

hydrodynamical simulations

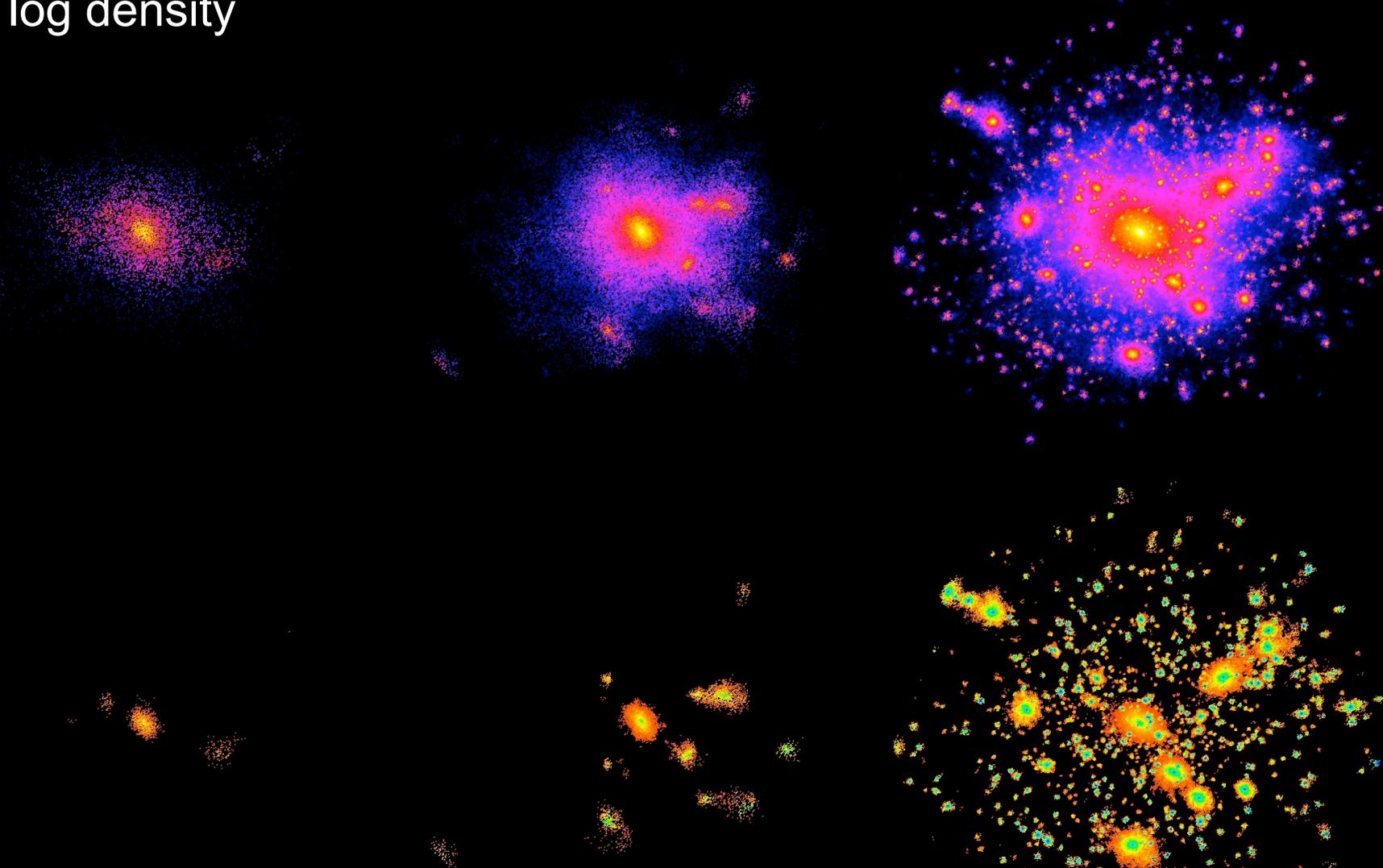
- computationally expensive, resolution relatively low
- hydro is not trivial (SPH and grid disagree even in simple tests, Agertz et al 2007)
- important physical processes far below the resolved scales (star formation, SN, ... ?)
implemented through uncertain functions and free parameters

→ approximate solution to the more realistic problem

Simulating structure formation

N-body models approximating CDM halos (about 1995 to 2000)

log density



log phase space density

from Ben Moore : www.nbody.net

the “via lactea” simulation

a Milky Way halo simulated with over 200 million particles

➤ collision-less (no hydro) → accurate solution of an idealized problem
no free parameters, no subgrid physics

➤ largest DM simulation to date
320,000 cpu-hours on NASA's Project Columbia supercomputer



➤ 213 million high resolution particles, embedded in a periodic 90 Mpc box
sampled at lower resolution to account for tidal field.

➤ WMAP (year 3) cosmology:
 $\Omega_m=0.238$, $\Omega_L=0.762$, $H_0=73$ km/s/Mpc, $n_s=0.951$, $\sigma_8=0.74$.

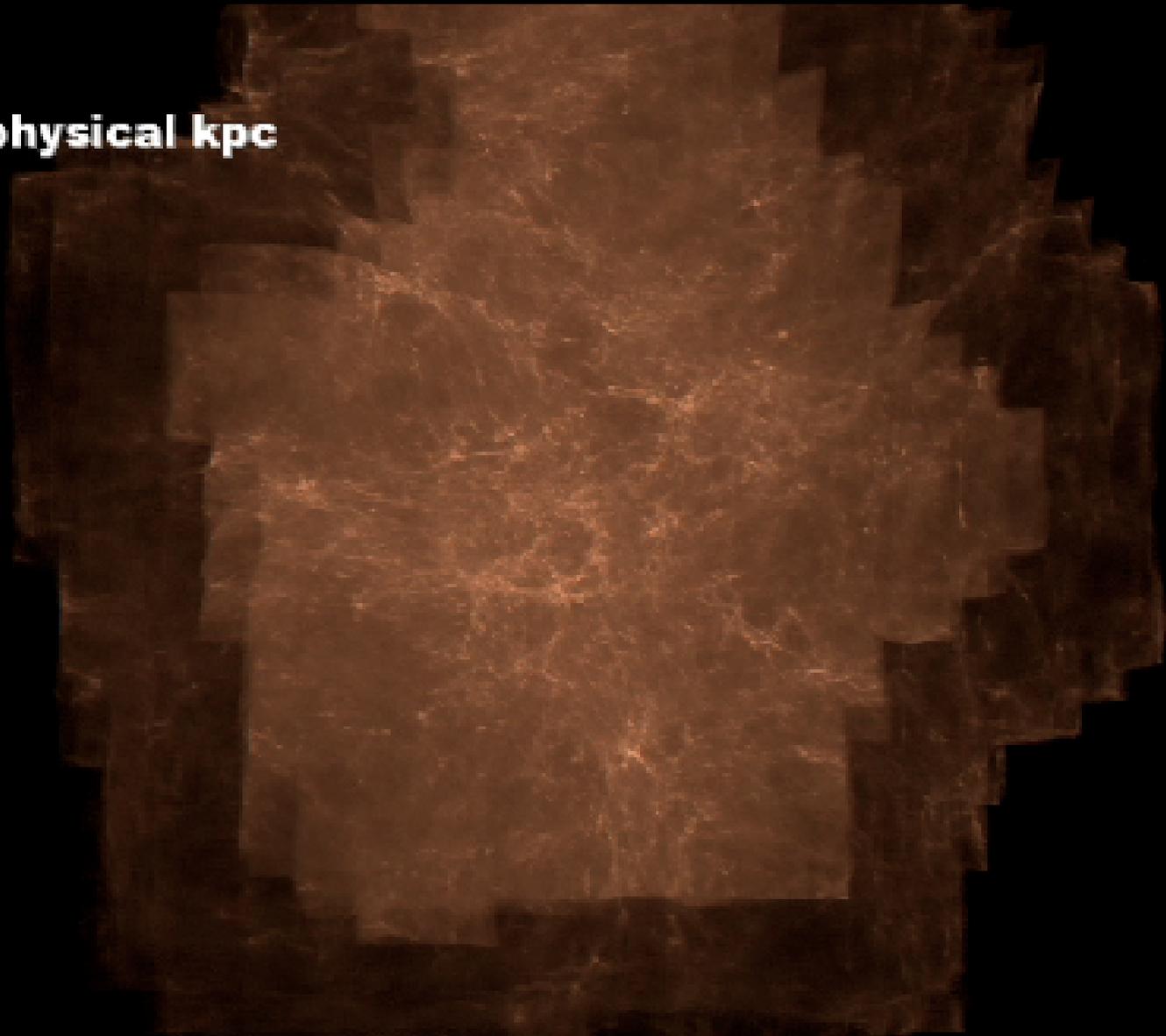
➤ force resolution: 90 parsec

➤ time resolution: adaptive time steps as small as 68,500 years

➤ mass resolution: 20,900 M_\odot

$z=11.9$

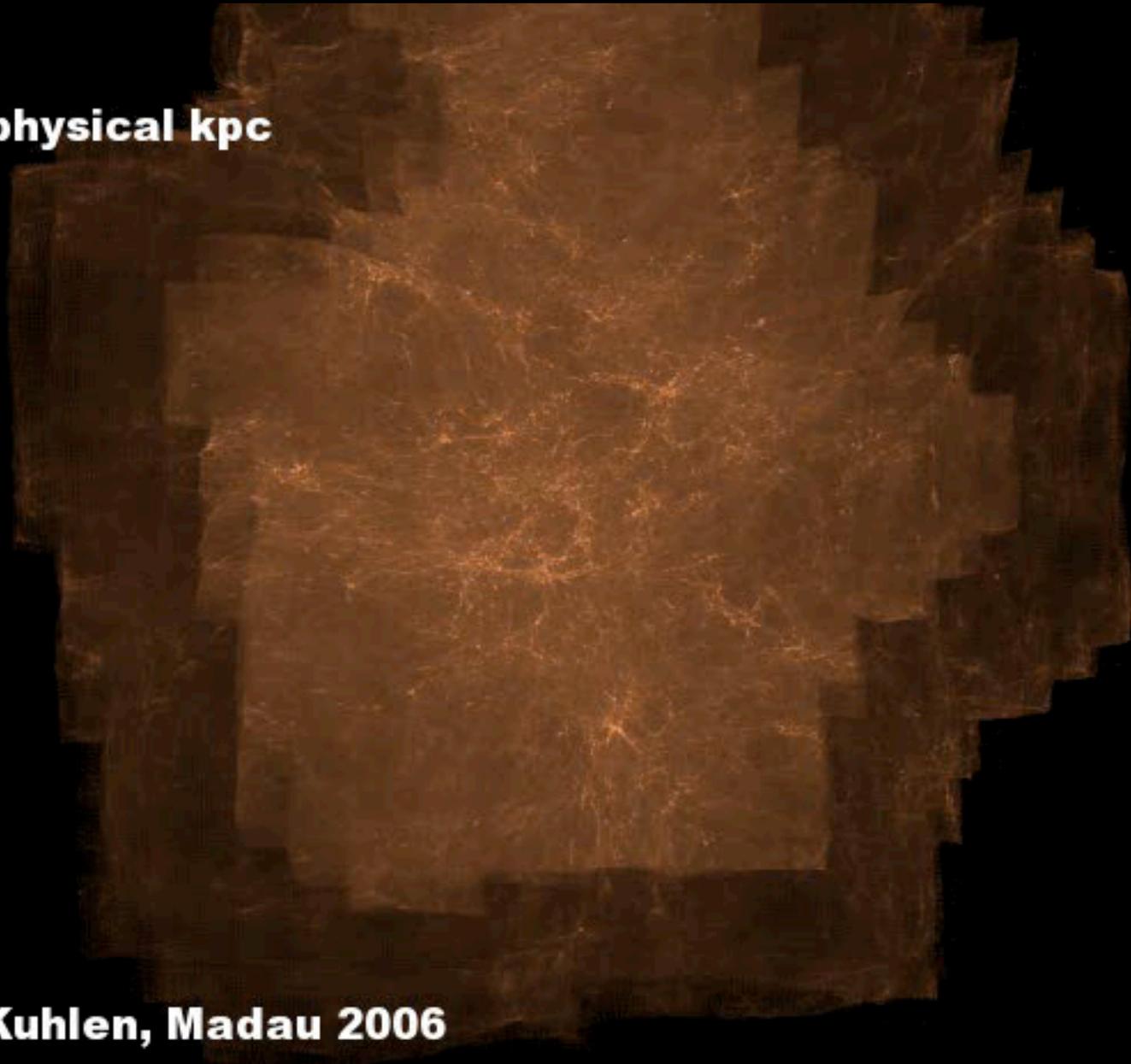
800 x 600 physical kpc



Diemand, Kuhlen, Madau 2006

$z=11.9$

800 x 600 physical kpc



Diemand, Kuhlen, Madau 2006

via lactea

a Milky Way dark matter halo simulated with 234 million particles on NASA's [Project Columbia](#) supercomputer

[main](#)

movies

[movies](#)

These animations show the projected dark matter density-square maps of the simulated Milky Way-size halo Via Lactea. The logarithmic color scale covers the same 20 decades in projected density-square in physical units in each frame. All movies are encoded in MPEG format and some are available in different quality versions.

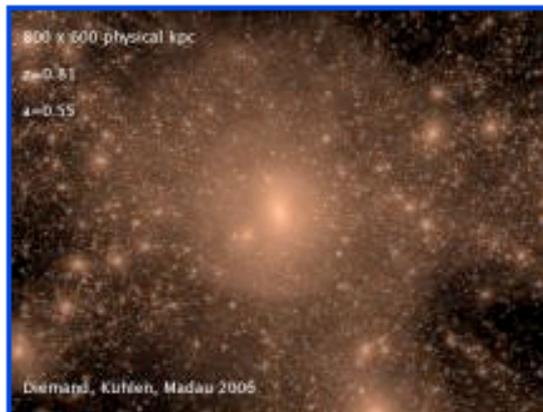
[images](#)

[publications](#)

the formation of the via lactea halo

[data](#)

[screensavers](#)



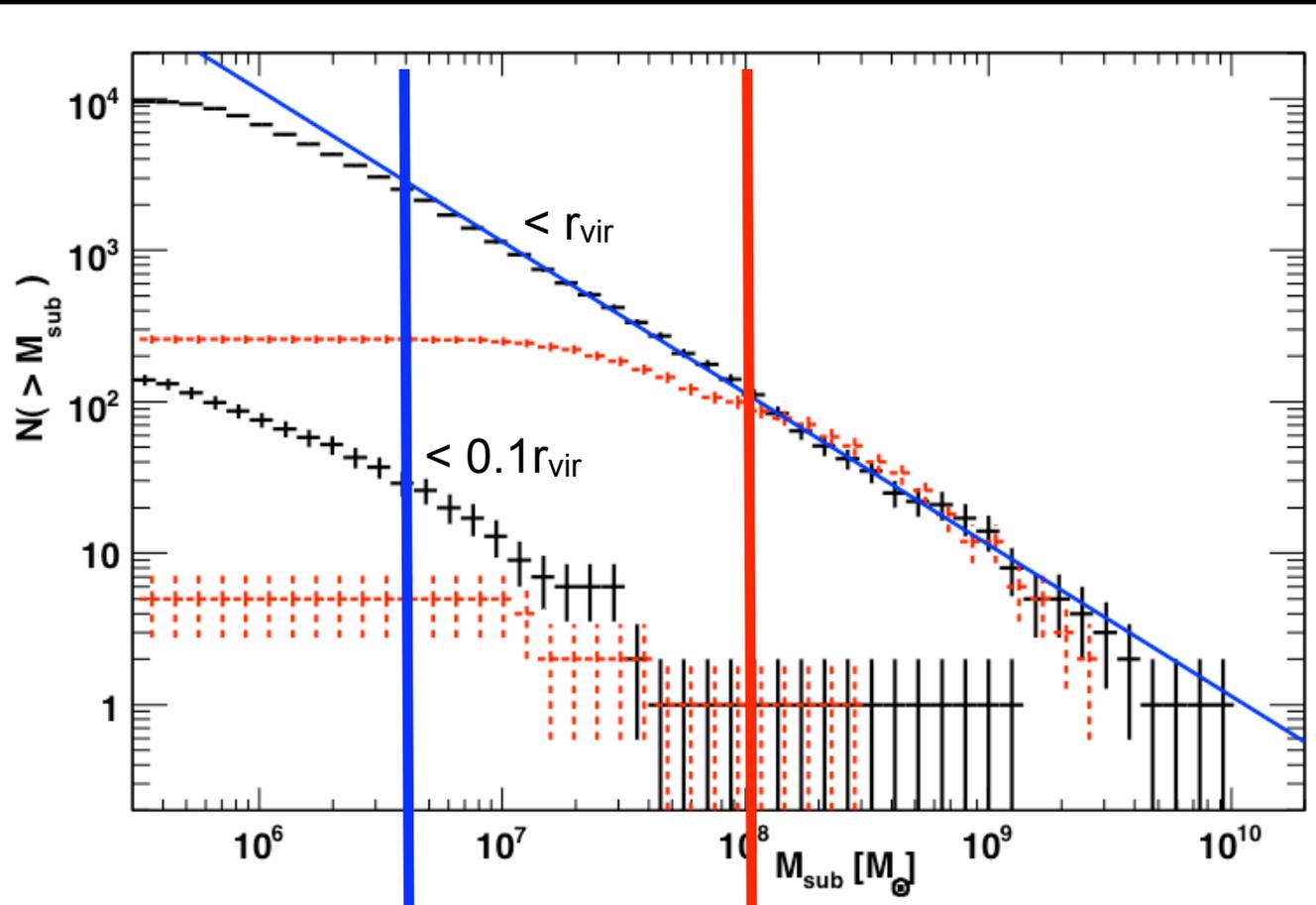
- entire formation history ($z=12$ to 0): [high quality \(218 MB\)](#)
smaller frames, quality: [high\(55 MB\)](#) [medium\(11 MB\)](#) [low\(4.7 MB\)](#)
- entire formation history, plus rotation and zoom at $z=0$:
quality: [high\(433 MB\)](#) [medium\(72 MB\)](#)
- early, active phase of merging and mass assembly ($z=12$ to 1.3): [\(81 MB\)](#)
- late, passive and stationary phase ($z=1.3$ to 0): [\(137 MB\)](#)

rotation and zoom into the via lactea halo at $z=0$ (today)



$z=0$ results from “via lactea” subhalo mass functions

JD, Kuhlen, Madau, astro-ph/0611370



200 particle limits
via lactea
lower resolution run

$$N(>M) \sim M^{-a}$$

with a between 0.9 and 1.1,
depending on mass range:

steeper at high M
due to dynamical friction

shallower at low M
due to numerical limitations

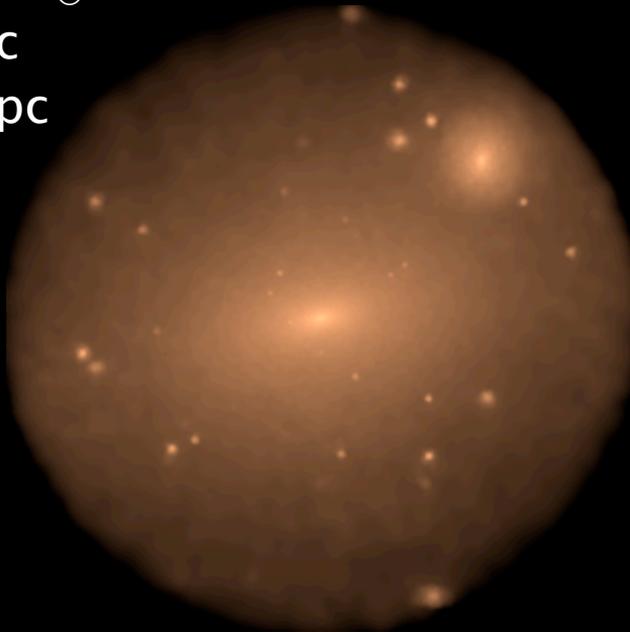
Close to constant contribution
to mass in subhalos
per decade in subhalo mass

sub-subhalos in all well resolved subhalos

$M_{\text{sub}} = 9.8 \cdot 10^9 M_{\odot}$

$r_{\text{tidal}} = 40.1 \text{ kpc}$

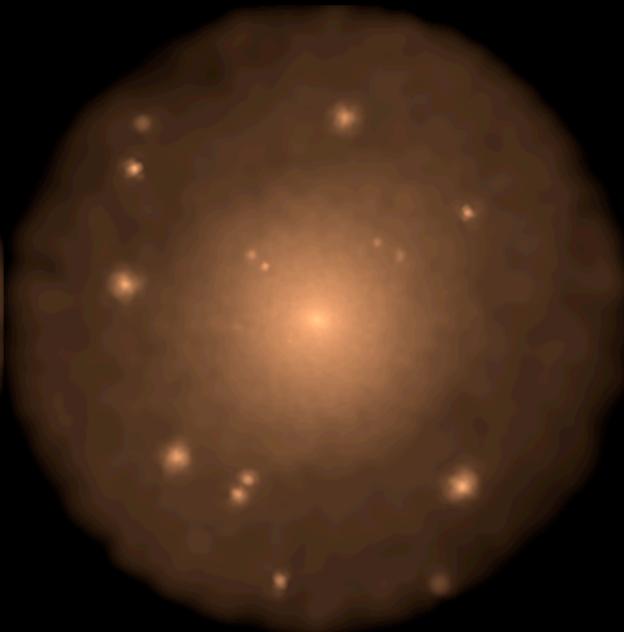
$D_{\text{center}} = 345 \text{ kpc}$



$M_{\text{sub}} = 3.7 \cdot 10^9 M_{\odot}$

$r_{\text{tidal}} = 33.4 \text{ kpc}$

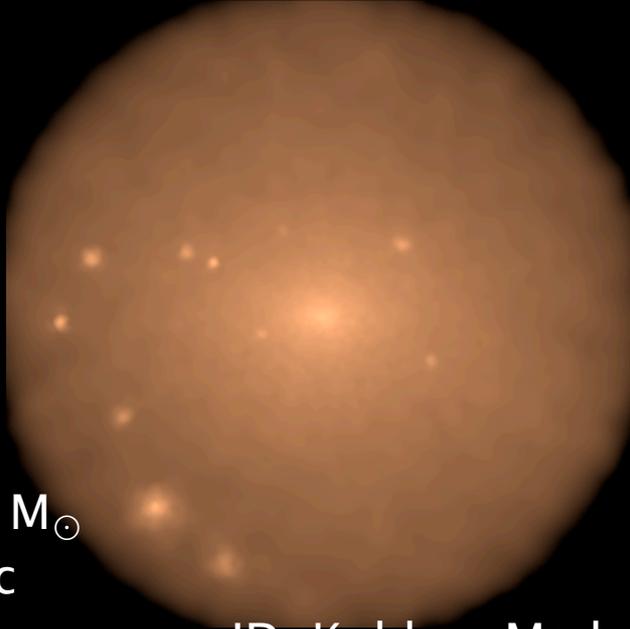
$D_{\text{center}} = 374 \text{ kpc}$



$M_{\text{sub}} = 2.4 \cdot 10^9 M_{\odot}$

$r_{\text{tidal}} = 14.7 \text{ kpc}$

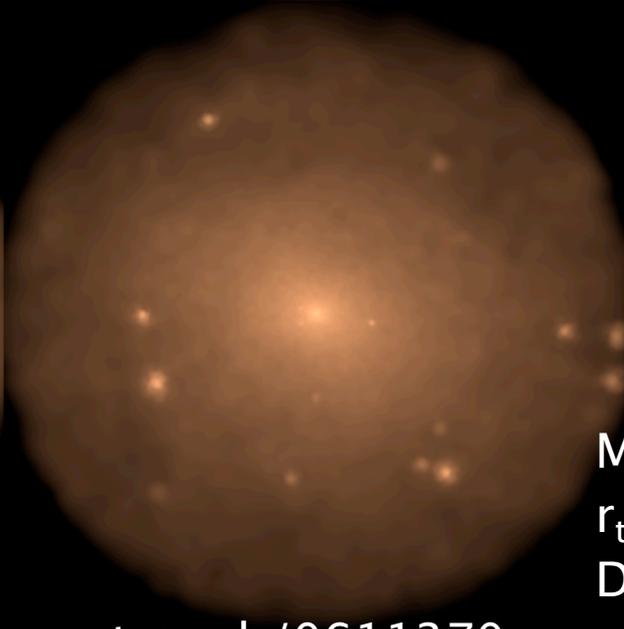
$D_{\text{center}} = 185 \text{ kpc}$



$M_{\text{sub}} = 3.0 \cdot 10^9 M_{\odot}$

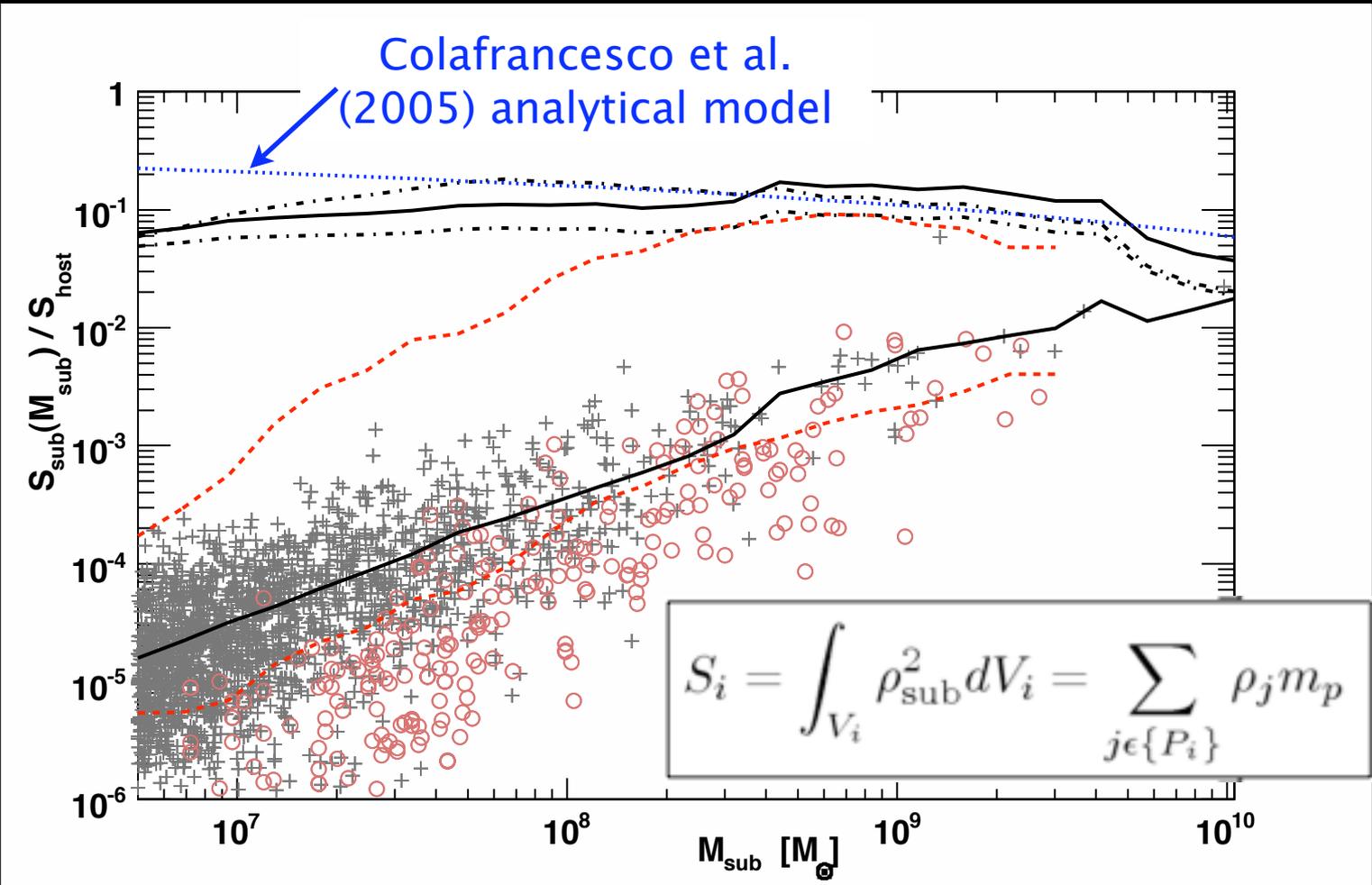
$r_{\text{tidal}} = 28.0 \text{ kpc}$

$D_{\text{center}} = 280 \text{ kpc}$



JD, Kuhlen, Madau, astro-ph/0611370

DM annihilation signal from subhalos



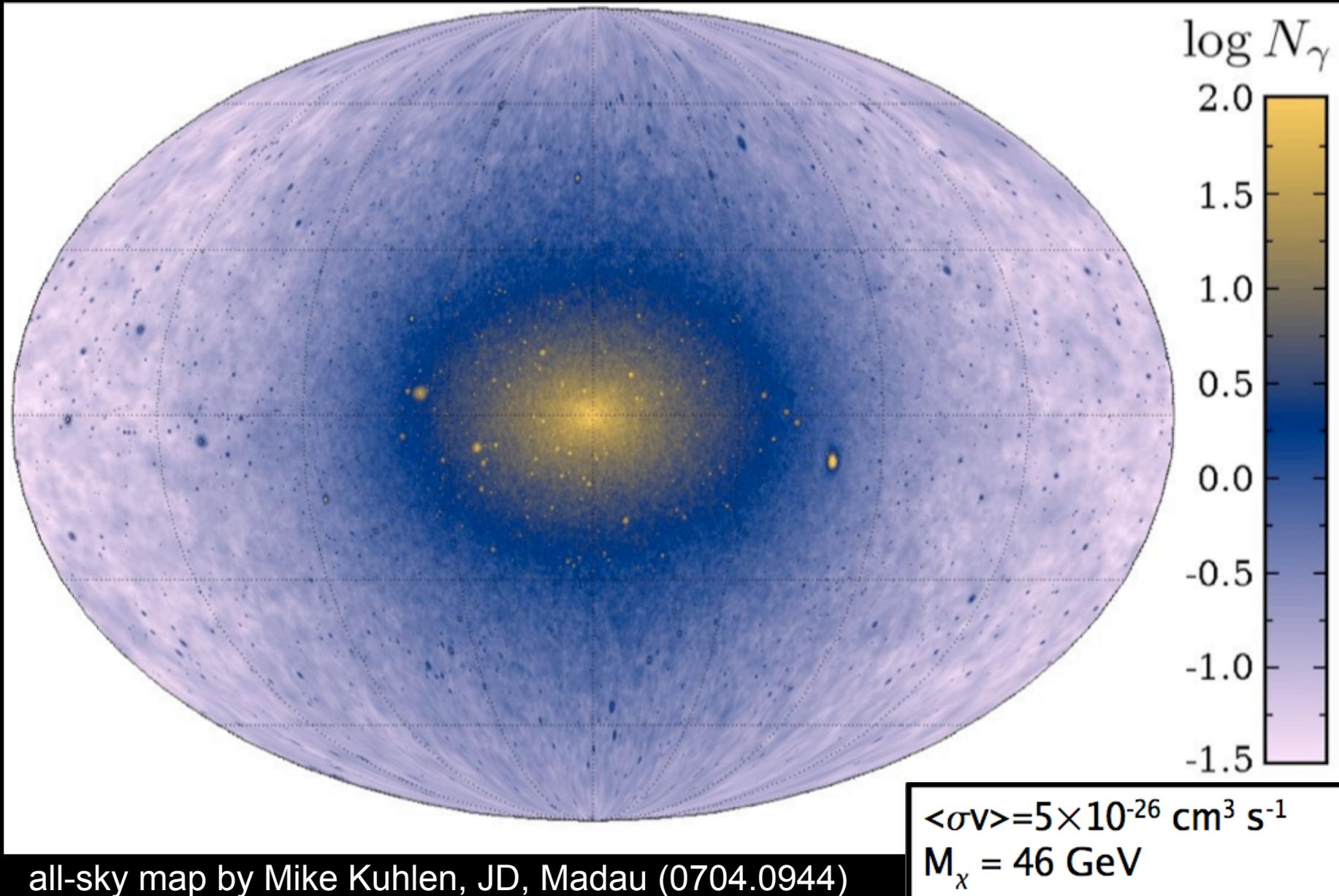
Total signal from subhalos is constant per decade in subhalo mass

The spherically averaged signal is about half of the total in Via Lactea, but the total signal has not converged

total boost factor from subhalos:
between 3 (constant) and 8 (more from small subs)

total boost factor including sub-sub-....-halos:
between 13 (constant) and about 80

(optimistic) photon counts for GLAST (2yr exp.)



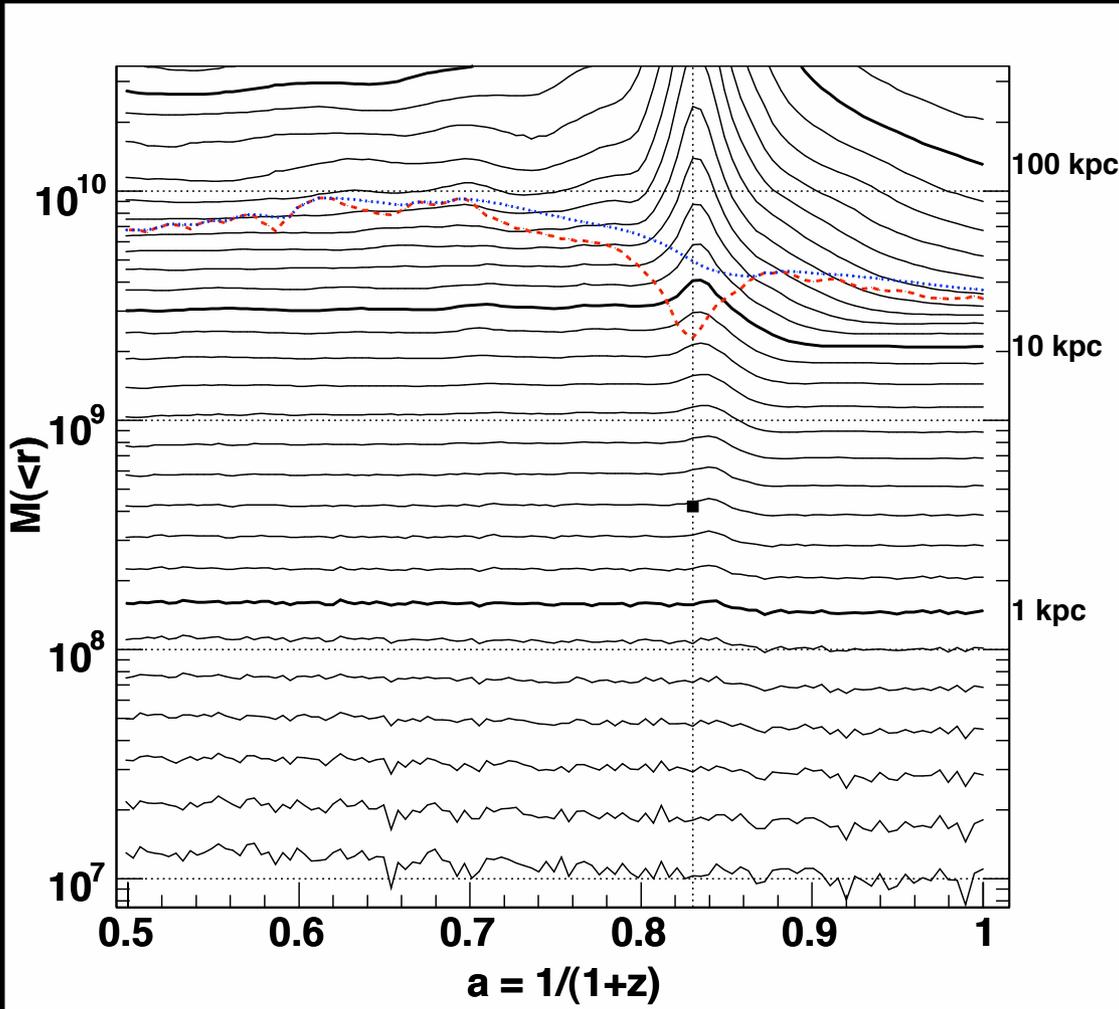
all-sky map by Mike Kuhlen, JD, Madau (0704.0944)

assuming sub-substructure boosts subhalo luminosities by a factor of 10

NOTE: We do not resolve all relevant subhalos yet !

boost of the unresolved component not included (see Pieri et al 2007)

evolution of subhalo density profiles



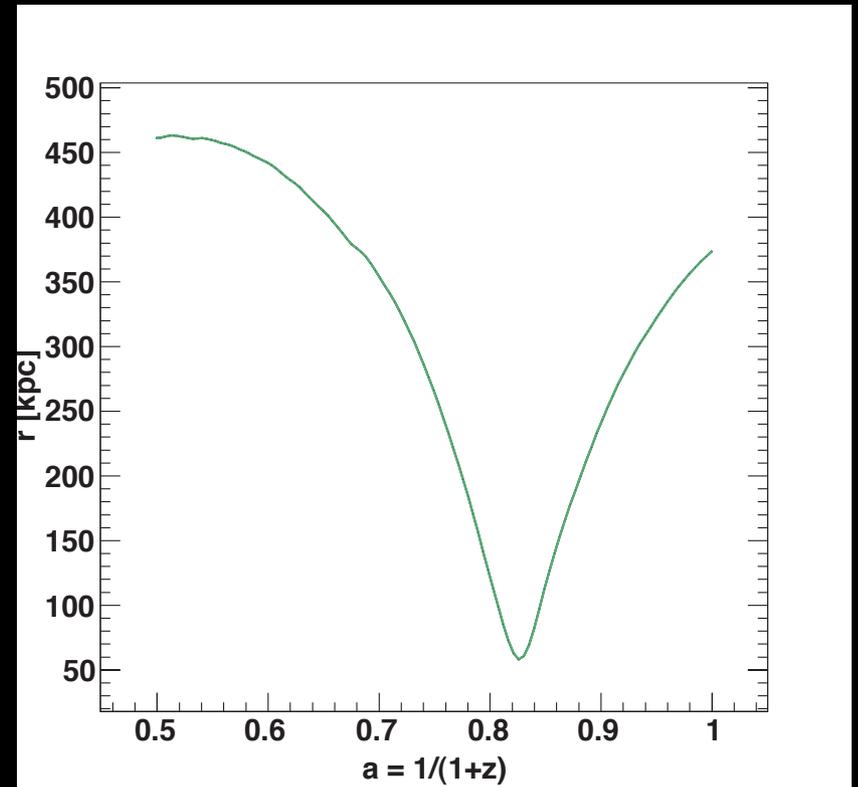
weak, long tidal shock

duration :

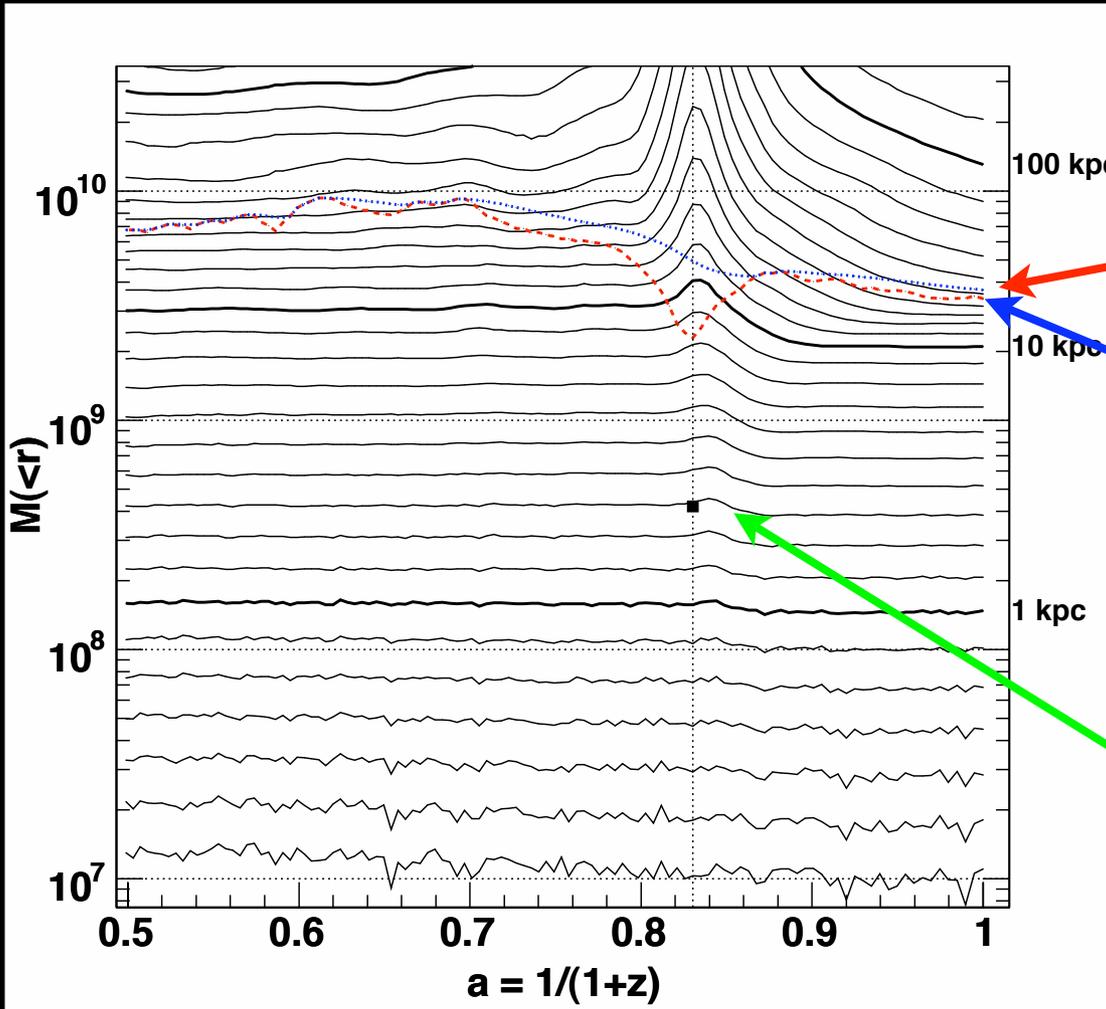
$$\tau = \pi(56 \text{ kpc}) / (423 \text{ km/s}) = 406 \text{ Myr}$$

total mass in spheres around subhalo center

this subhalo has one pericenter passage at 56 kpc



evolution of subhalo density profiles



tidal mass is smaller than the bound mass at pericenter

“delayed” tidal mass

$$\Delta m = M(> r_t) \delta t / T_s$$

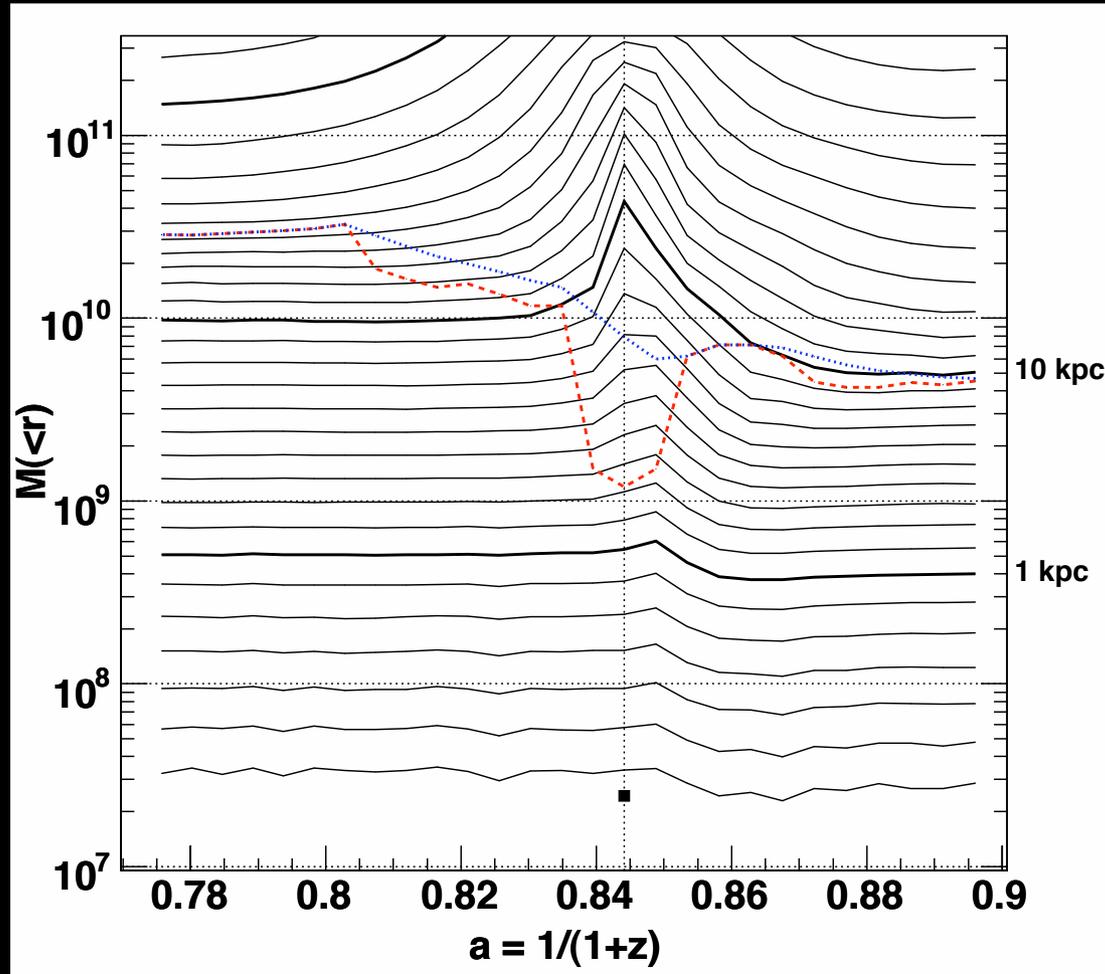
with $T_s = T_{\text{orbit}} / 6$

shock duration = internal subhalo orbital time

weak, long tidal shock
causes quick compression followed by expansion

mass loss is larger further out

evolution of subhalo density profiles

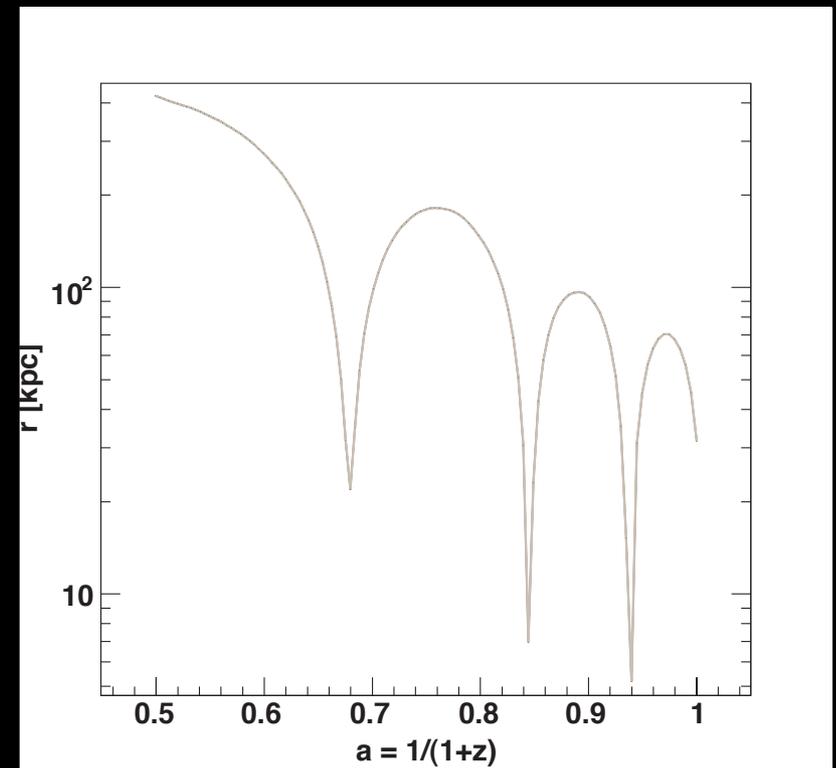


strong, short tidal shock

short duration : 43 Myr ➡ also affects inner halo, but mass loss still grows with radius

at pericenter $r_{\text{tidal}} = 0.2 r_{\text{Vmax}}$, but the subhalo survives this and even the next pericenter

this subhalo has its second of three pericenter passages at 7.0 kpc



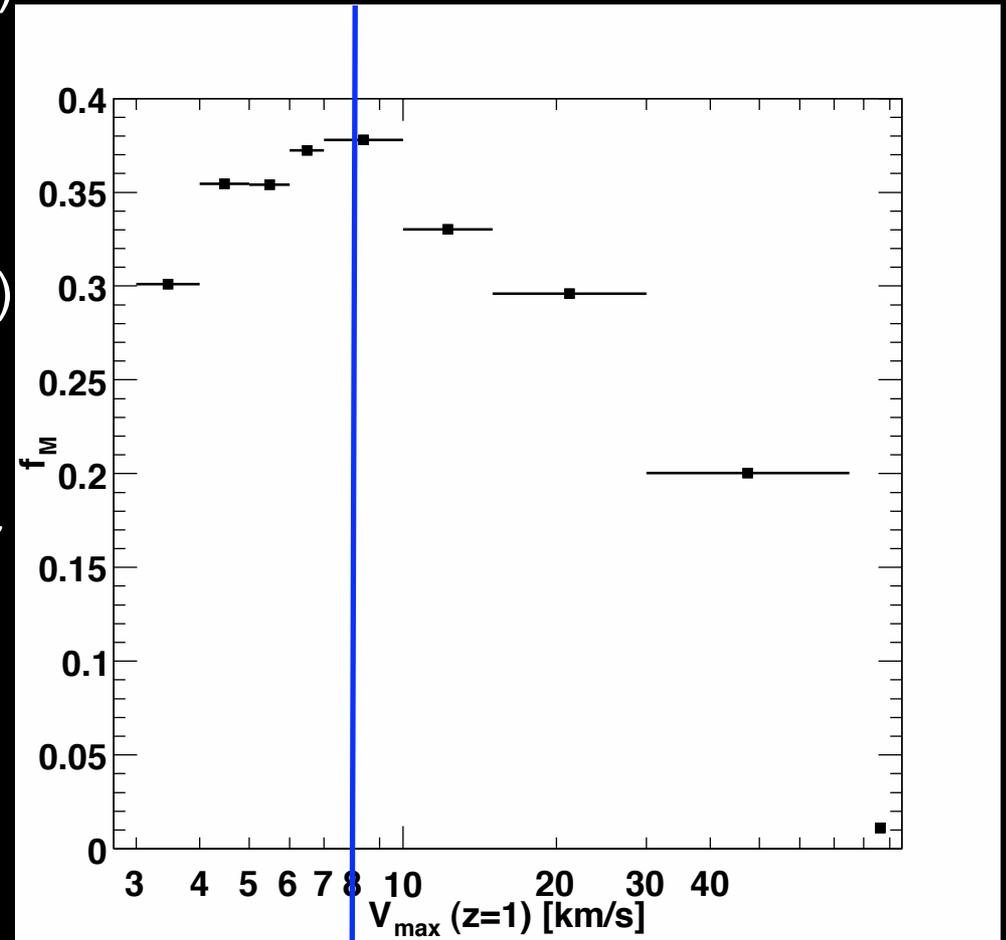
subhalo survival and merging

out of 1542 well resolved ($V_{\max} > 5$ km/s)
 $z=1$ subhalos:

97 % survive until $z=0$

(only 1.3% merge into a larger subhalo)

The average mass fraction that remains
bound to them until $z=0$ depends on their
(initial) size



← affected by numerical limitations

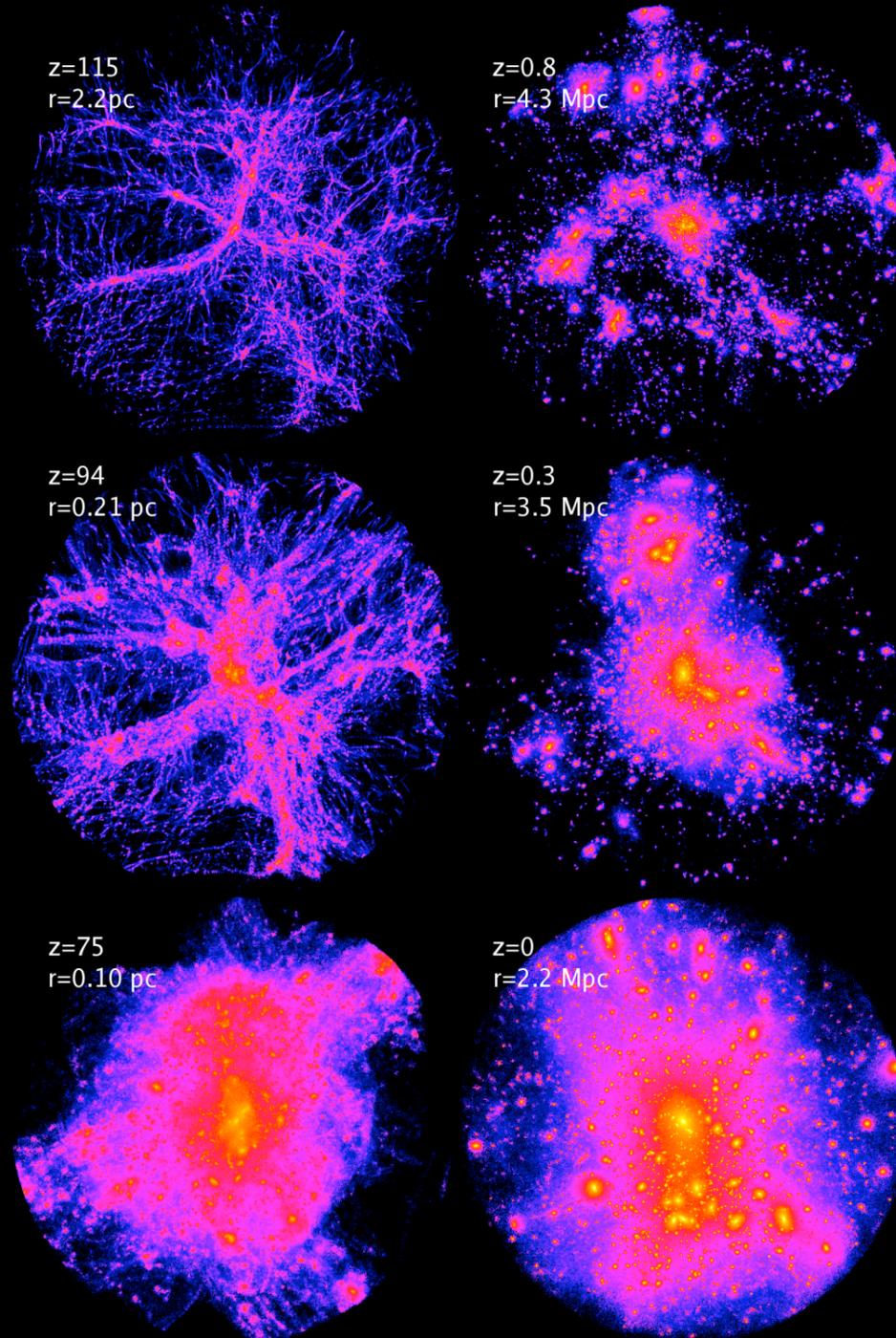
→ stronger dynamical friction

high redshift micro-subhalos are only slightly more fragile despite their flat $\sigma(M)$

almost simultaneous collapse of a $0.01 M_{\text{sun}}$ halo at $z=75$

lower density contrast, but similar subhalo abundance as in a $z=0$ cluster

JD, Kuhlen, Madau
astro-ph/0603250



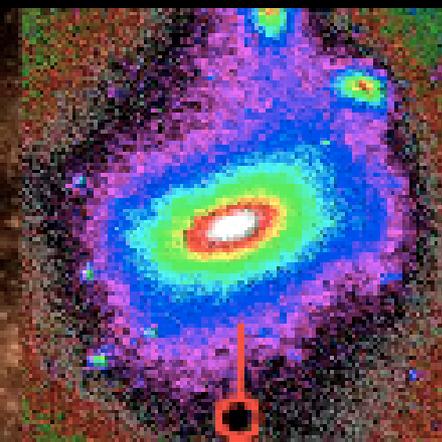
hierarchical formation of a $z=0$ cluster

same comoving DM density scale from 10 to 10^6 times the critical density

in each panel the final $M_{\text{vir}} \sim 20$ million particles are shown

$z=2.0$

800 x 600 physical kpc



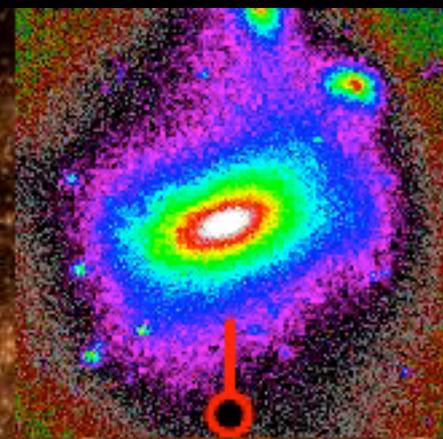
$M_t = 1.6e+10 M_\odot$

Diemand, Kuhlen, Madau 2006

survives several close pericenter passages (comes within 5.1 kpc)
becomes rounder with time and major axes tend to point towards the host center
(Kuhlen, JD, Madau 0705.2037, Faltenbacher+0706.0262, Pereira+0707.1702)

$z=2.0$

800 x 600 physical kpc



$M_t = 1.6e+10 M_\odot$

Diemand, Kuhlen, Madau 2006

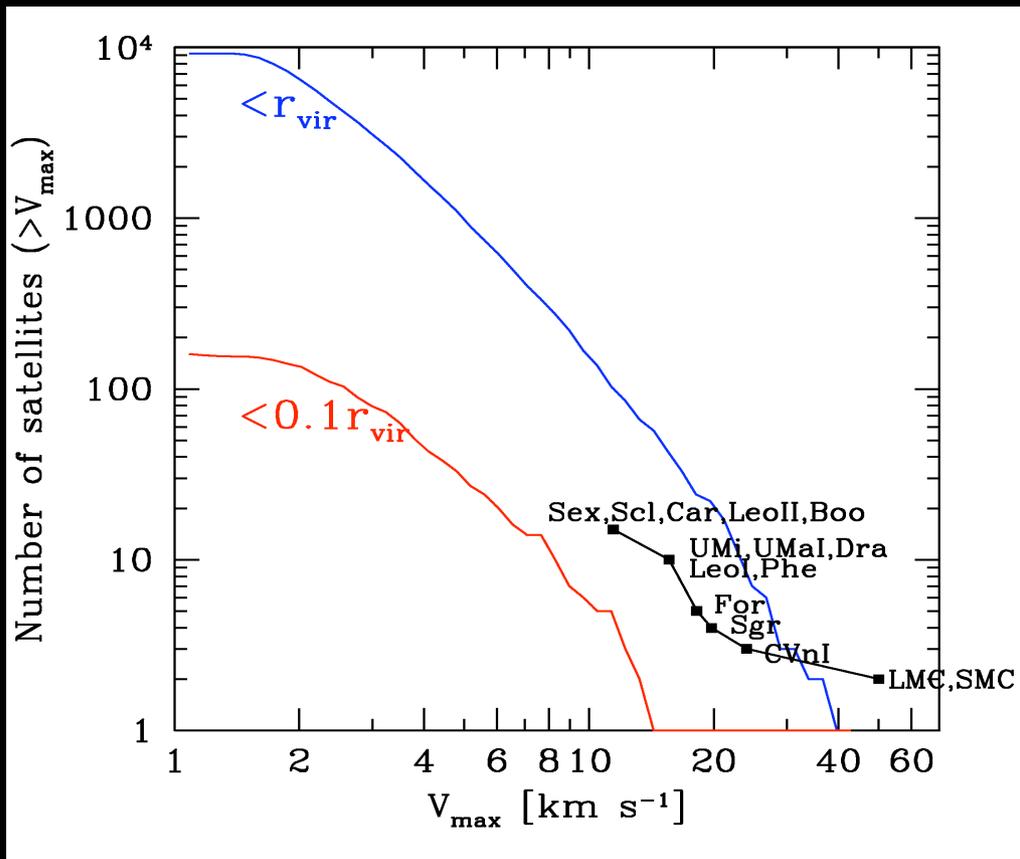
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missing satellites?

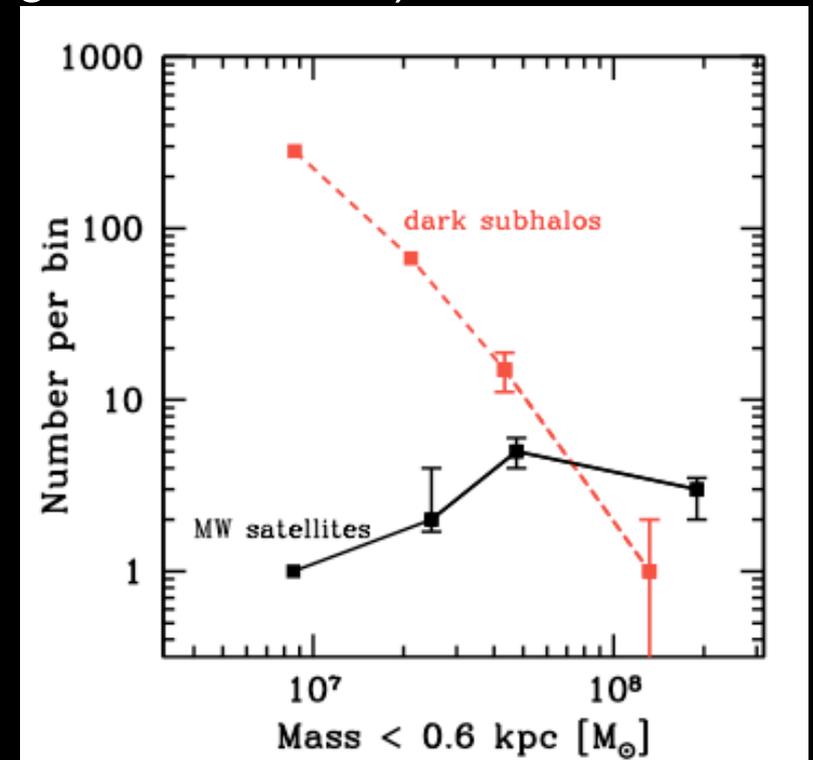
CDM only predicts subhalos, not dwarf galaxies. Luckily, CDM predicts (more than) enough structures to host all known Local Group satellites.

Plausible galaxy formation models roughly reproduce the observed numbers of dwarfs. Many CDM subhalos remain dark (Governato et al. 2007)

As in the original (Moore+99, Klypin+99) comparisons we assumed $\sqrt{3} \sigma_{1D}^* = V_{max}$

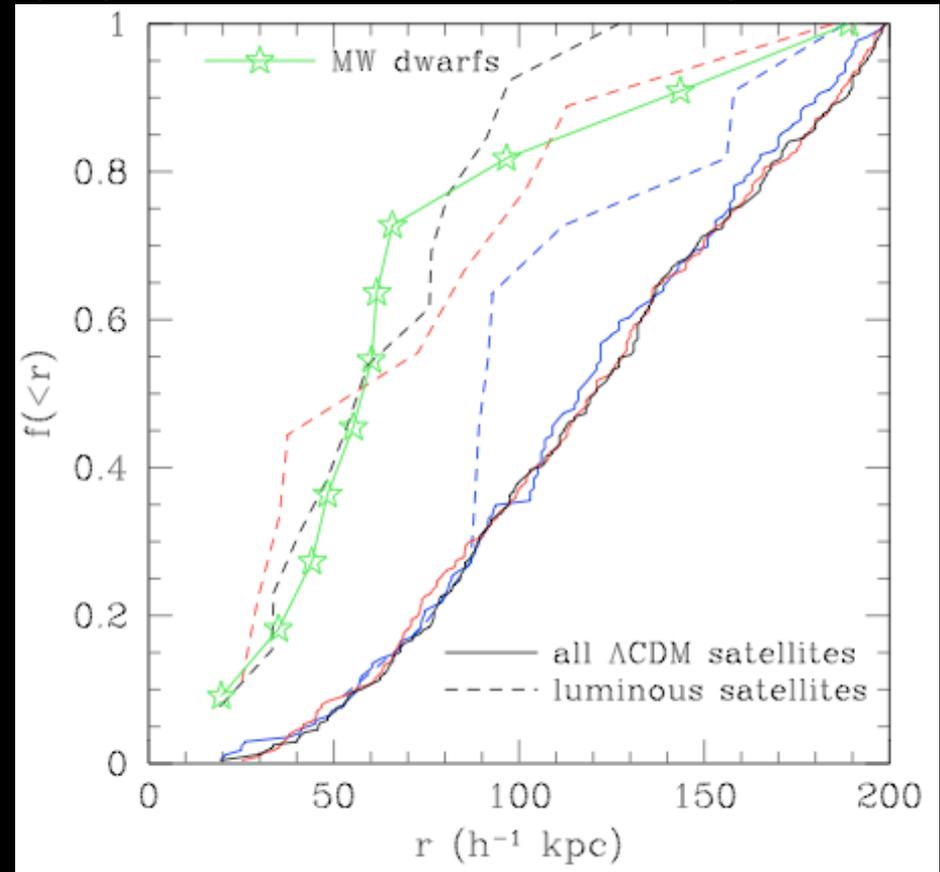
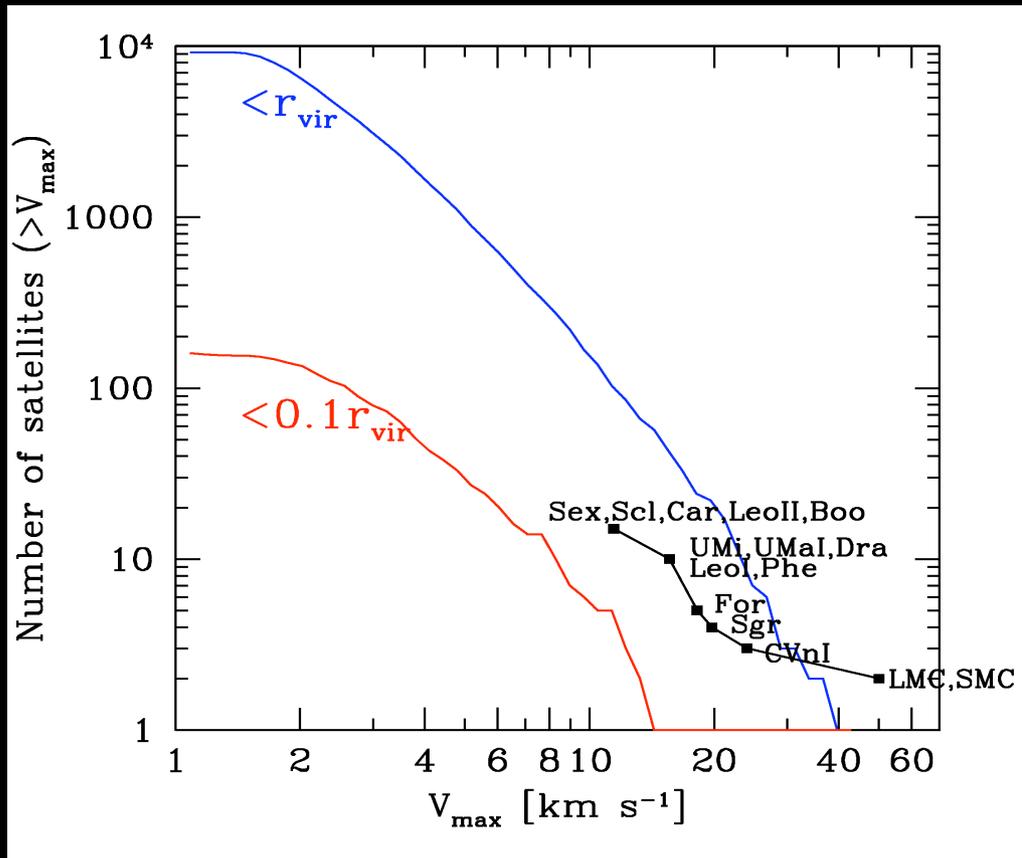


this seems to be roughly right (Strigari+0704.1817):



missing satellites?

the largest subhalos are much further away (Taylor+2003, Kravtsov+2004):

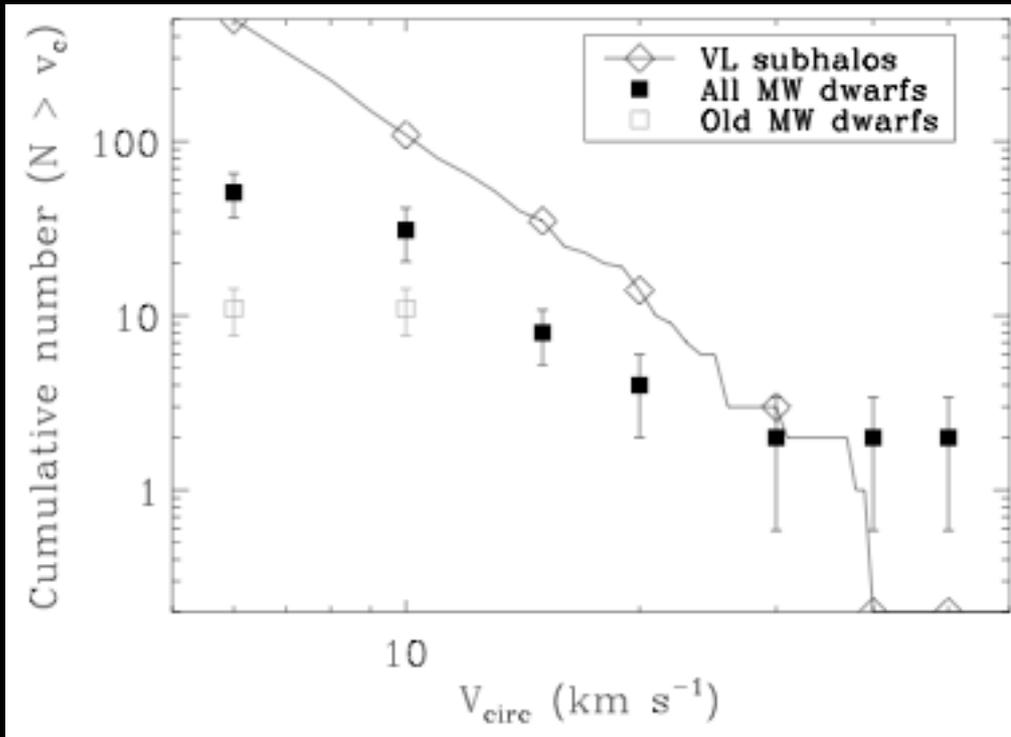


we need more subhalos than dwarfs at a given size to have enough hosts at the correct distances!

(lowering the normalization would be a problem on LMC/SMC scales
Via Lactea is near the median, rms halo to halo scatter is about a factor of two)

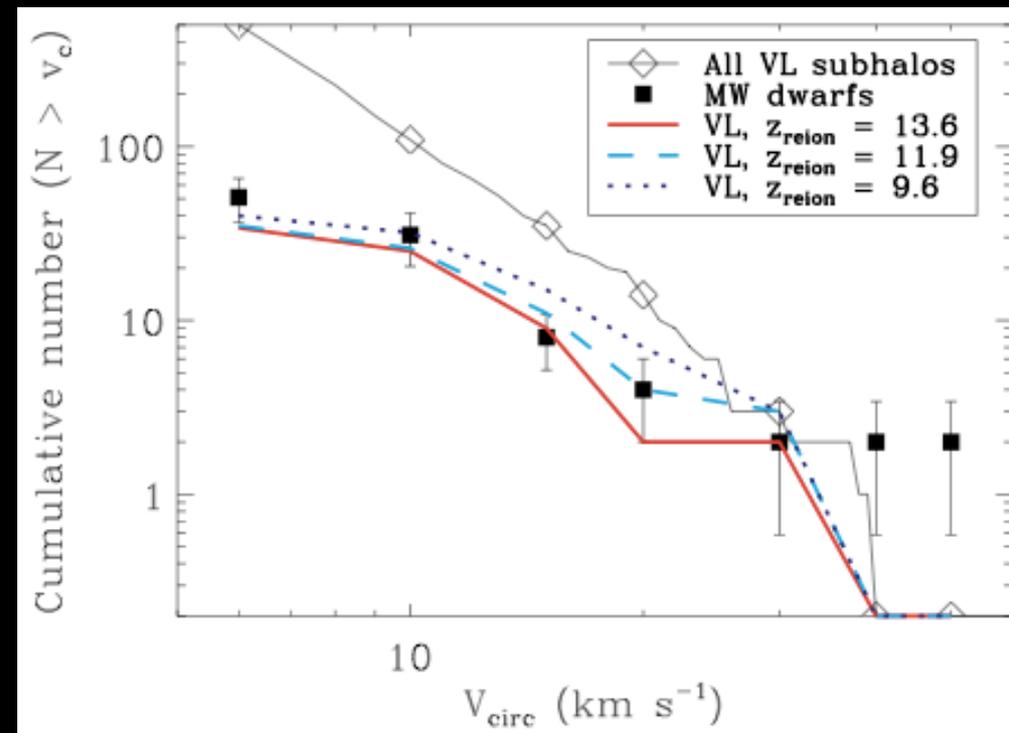
missing satellites?

adding the new ultra faint dwarfs from SDSS helps (Simon+Geha2007):

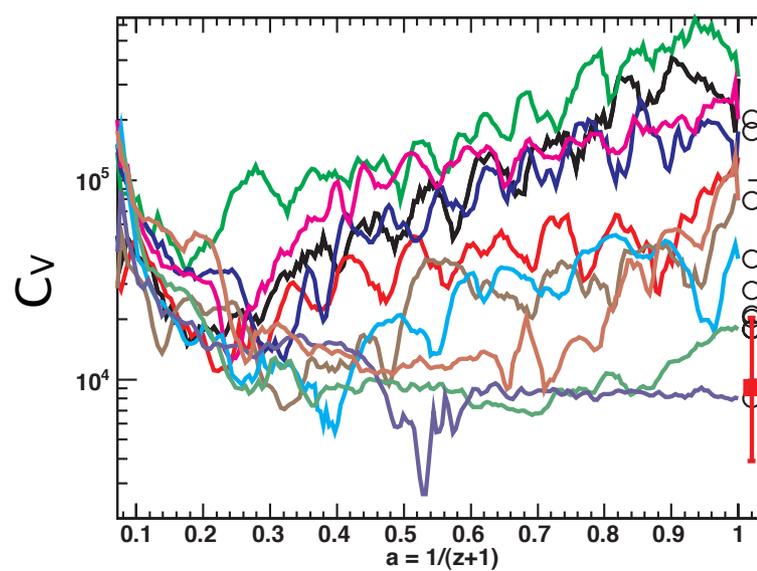
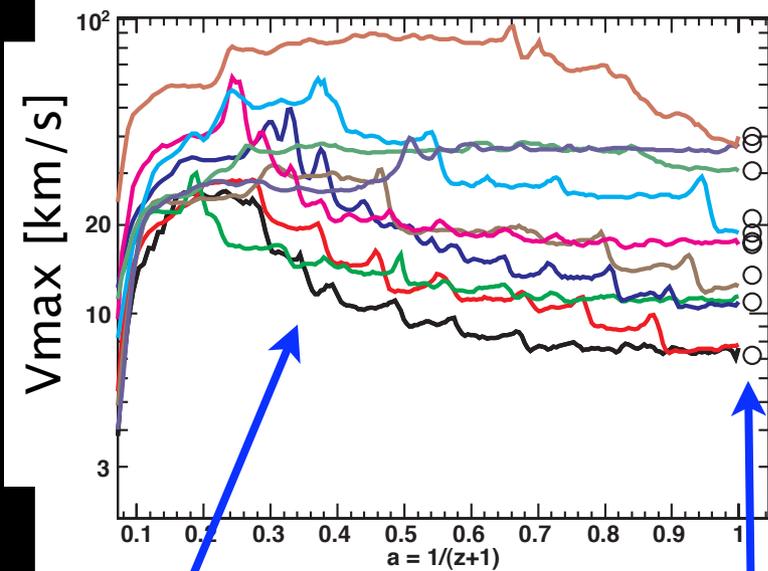
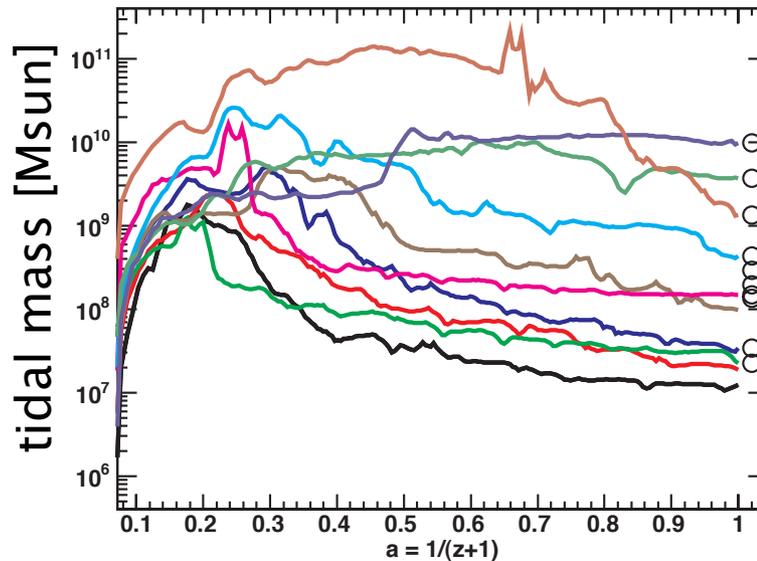
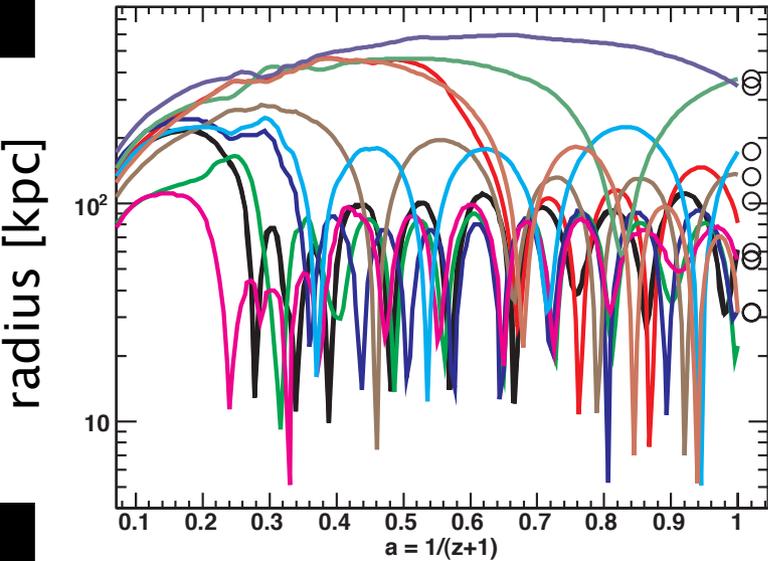


earliest forming “EF” subhalos
(or the largest before accretion “LBA”)
would have roughly the right masses

and also the correct spatial distribution
(Moore,JD et al 2006)



possible hosts of Local Group dwarfs



diverse histories:

0 to 11
pericenters
inner subhalos
tend to have
more of them
and starting
earlier

none to very
large mass loss

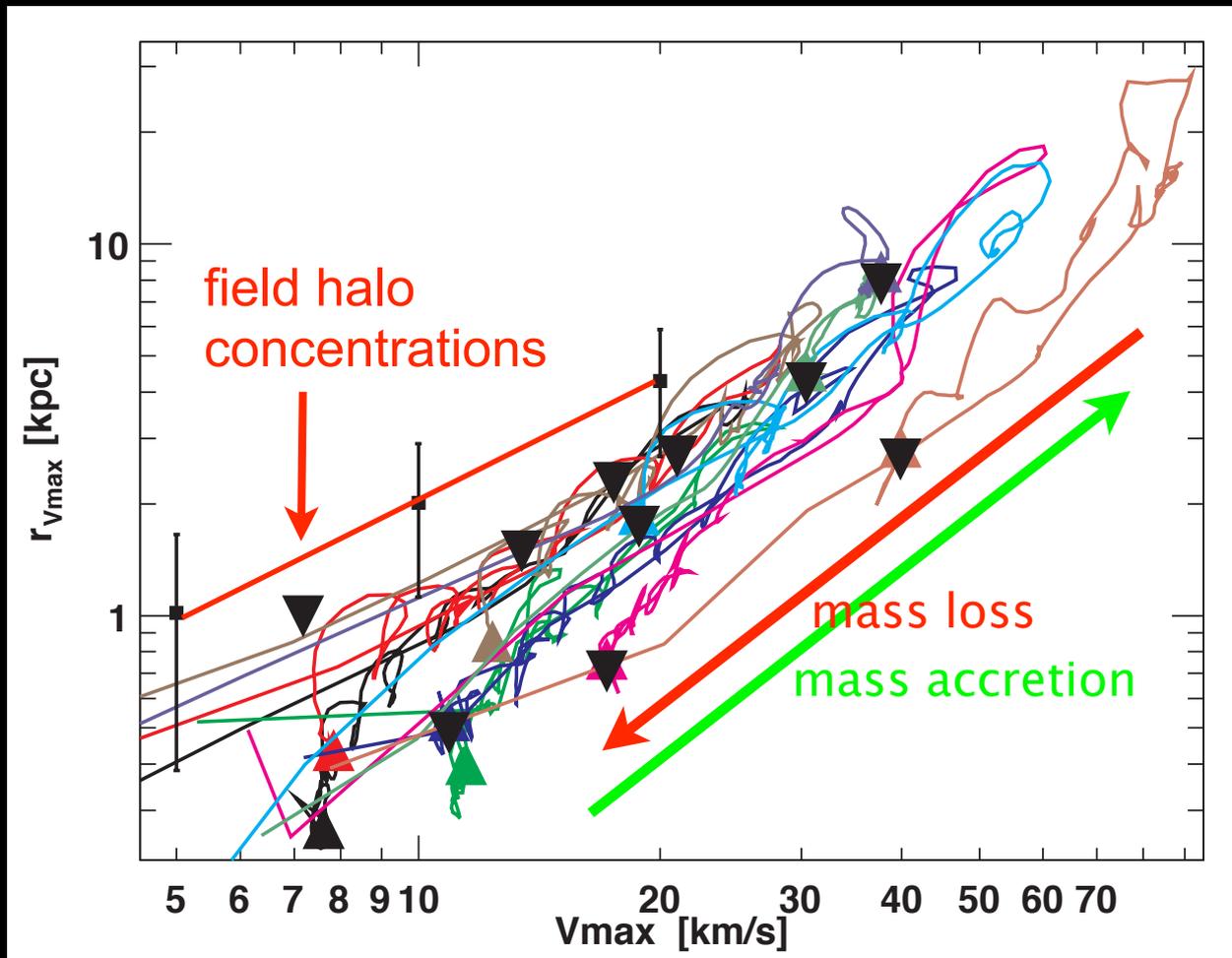
concentrations
increase during
tidal mass loss

field halo
concentrations

tracks of 10 EF subhalos

$z=0$ properties of LBA

possible hosts of Local Group dwarfs



same 10 tracks

tidal mass loss from the outside in partially undoes the inside out halo assembly

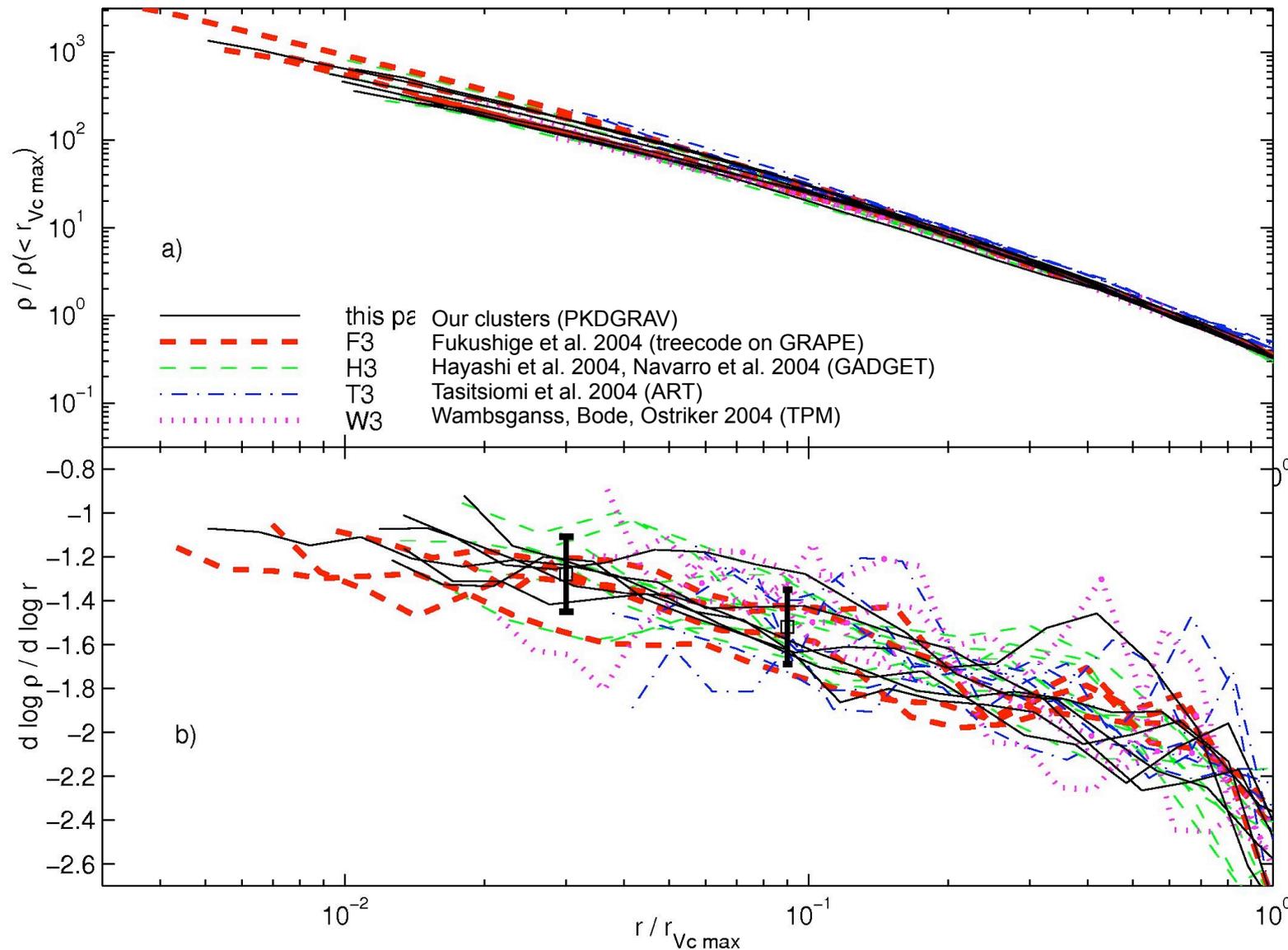
→ stripped halos resemble high redshift systems

→ they have high concentrations

3) CDM density profiles

eg. Fukushige et al 2004, Navarro et al 2004, JD et al 2004

CDM cluster density profiles are close to universal (e.g. NFW),
but individual halo density profile shapes have scatter:



JD, Moore, Stadel,
MNRAS, 2004

scatter in CDM cluster density profiles

	$1\%r_{\text{vir}}$	$3\%r_{\text{vir}}$	$3\%r_{\text{Vcmax}}$	$9\%r_{\text{Vcmax}}$
<i>A9</i>	1.22	1.36	1.24	1.64
<i>B9</i>	1.33	1.43	1.21	1.63
<i>C9</i>	1.24	1.21	1.25	1.26
<i>D12</i>	1.28	1.54	1.32	1.58
<i>E9</i>	1.31	1.44	1.41	1.62
<i>F9cm</i>	1.19	1.47	1.22	1.43
a) A-F	1.26 ± 0.05	1.41 ± 0.11	1.28 ± 0.08	1.53 ± 0.15
b) F03	1.25 ± 0.05	1.52 ± 0.06	1.33 ± 0.15	1.54 ± 0.15
c) H03	1.18 ± 0.13	1.38 ± 0.14	1.23 ± 0.17	1.50 ± 0.14
d) T03	1.50 ± 0.14	1.79 ± 0.07	—	1.56 ± 0.12
e) W03	1.11 ± 0.04	1.41 ± 0.13	—	1.35 ± 0.06
avg.(a-e)	1.26	1.50	—	1.49
avg.(a-c)	1.23	1.44	1.28	1.52
NFW			1.12	1.32
Moore et al.			1.54	1.65

JD, Moore, Stadel,
MNRAS, 2004, 353, 624

why are profiles nearly universal?

what causes the scatter?

fitting functions

2 parameter functions (only two 'scaling' parameters):

NFW

$$\rho = \frac{\rho_s}{x(1+x)^2}$$

$$x = r/r_s$$

Moore et al 1999

$$\rho = \frac{\rho_s}{x^{1.5}(1+x)^{1.5}}$$

3 parameter functions (one additional 'profile shape' parameter):

gamma-model (cusp)
JD, Moore, Stadel, 2004

$$\rho_G(r) = \frac{\rho_s}{(r/r_s)^\gamma (1 + (r/r_s)^\alpha)^{(\beta-\gamma)/\alpha}}$$

$$\alpha = 1 \quad \beta = 3$$

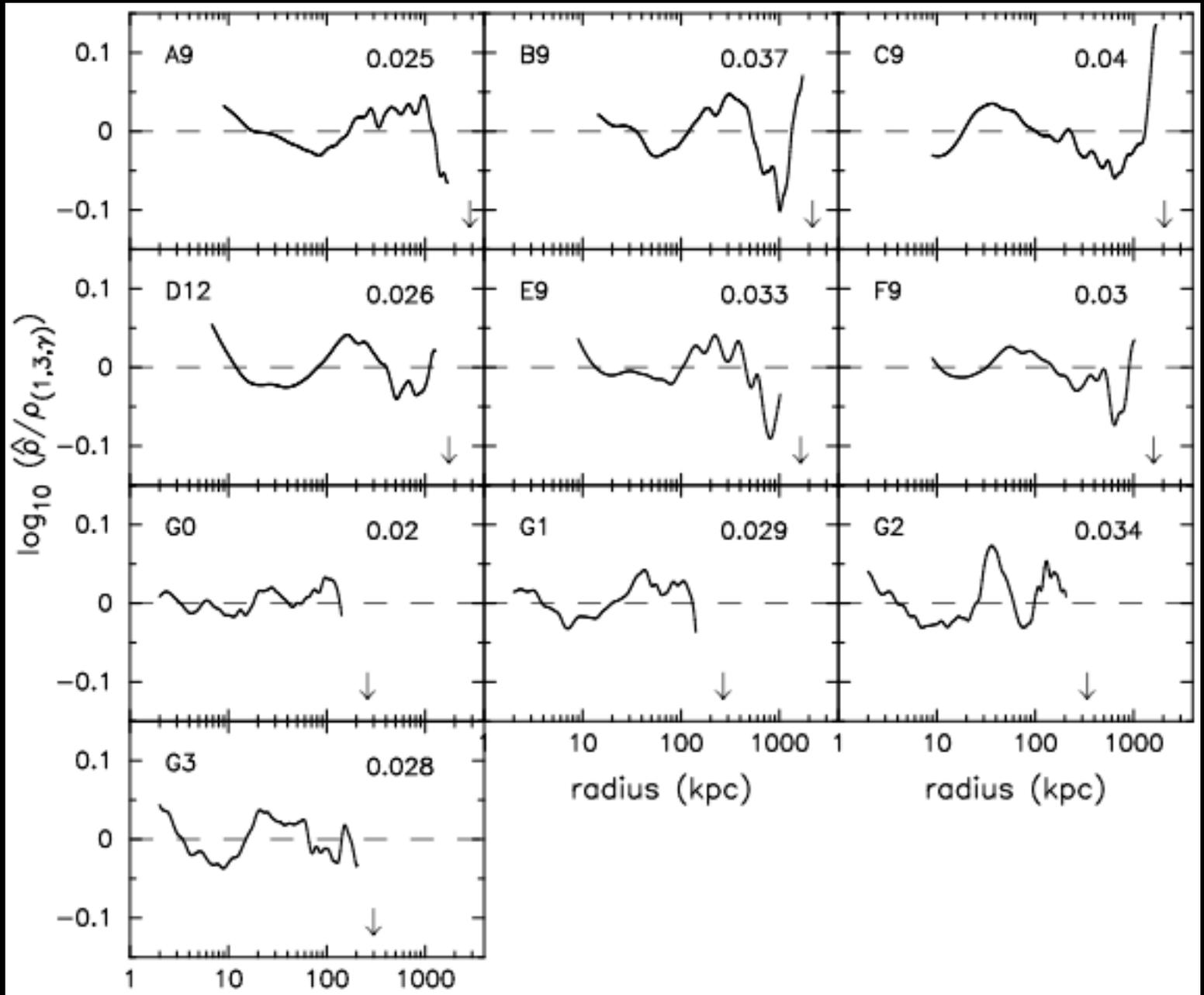
Einasto-model (core)
Navarro et al 2004
Merrit et al 2005/2006

$$\rho(r) = \rho_e \exp \left\{ -d_n \left[(r/r_e)^{1/n} - 1 \right] \right\}$$

3 parameter functions (one additional 'profile shape' parameter):

gamma-model

fitted to
non-parametric
density profiles



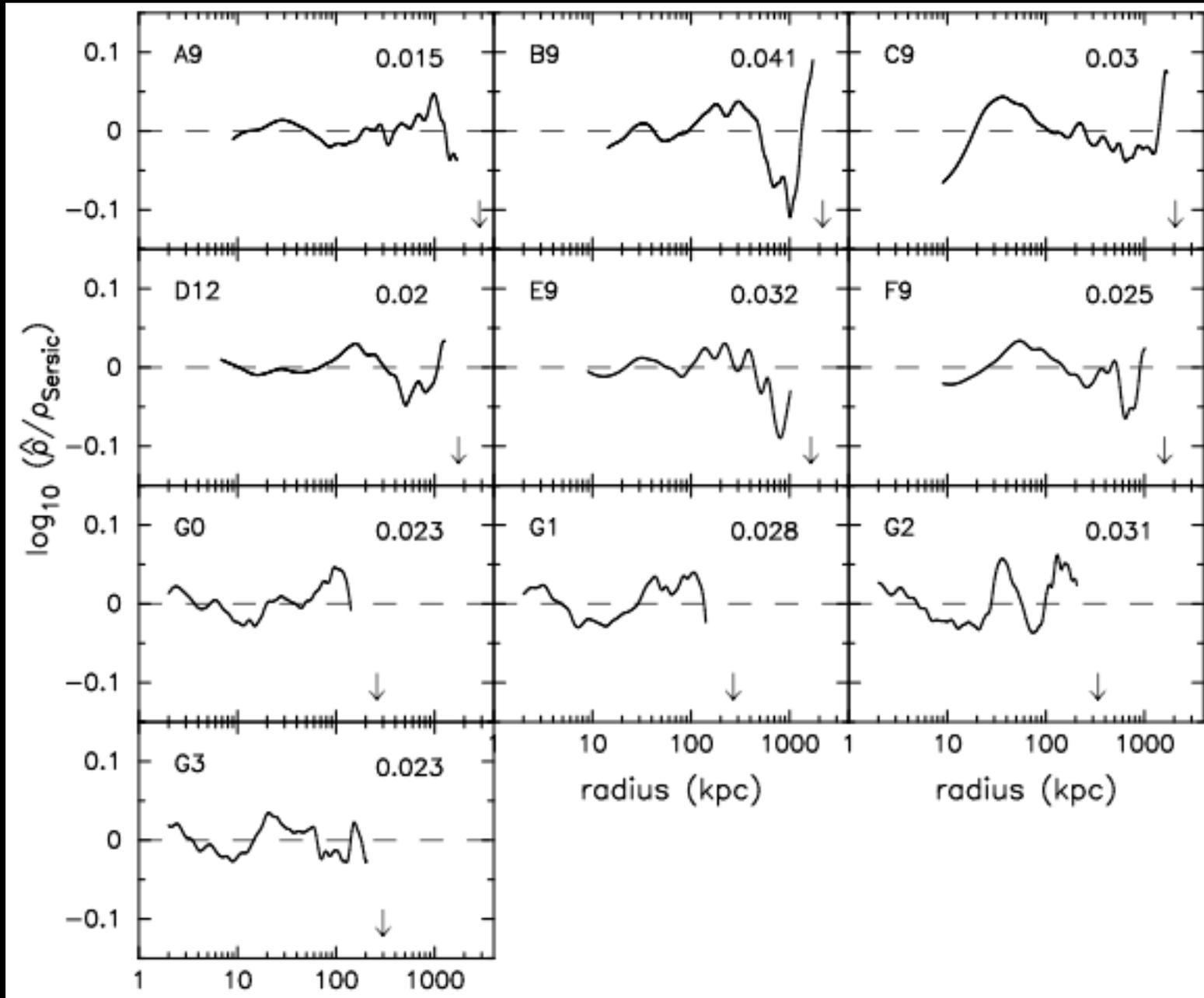
3 parameter functions (one additional 'profile shape' parameter):

Einasto-model

rms deviations
are often
smaller than
for the
gamma-model

both have largest
deviations in the
outer halo

which one fits the
inner halo better?



resolving the very inner profile

JD, Zemp, Moore, Stadel, Carollo,
MNRAS, 2005, 364, 665

physical time-steps:

the empirical $\Delta t_i < \eta \sqrt{\epsilon/a_i}$, $\eta=0.25$ is no longer sufficient

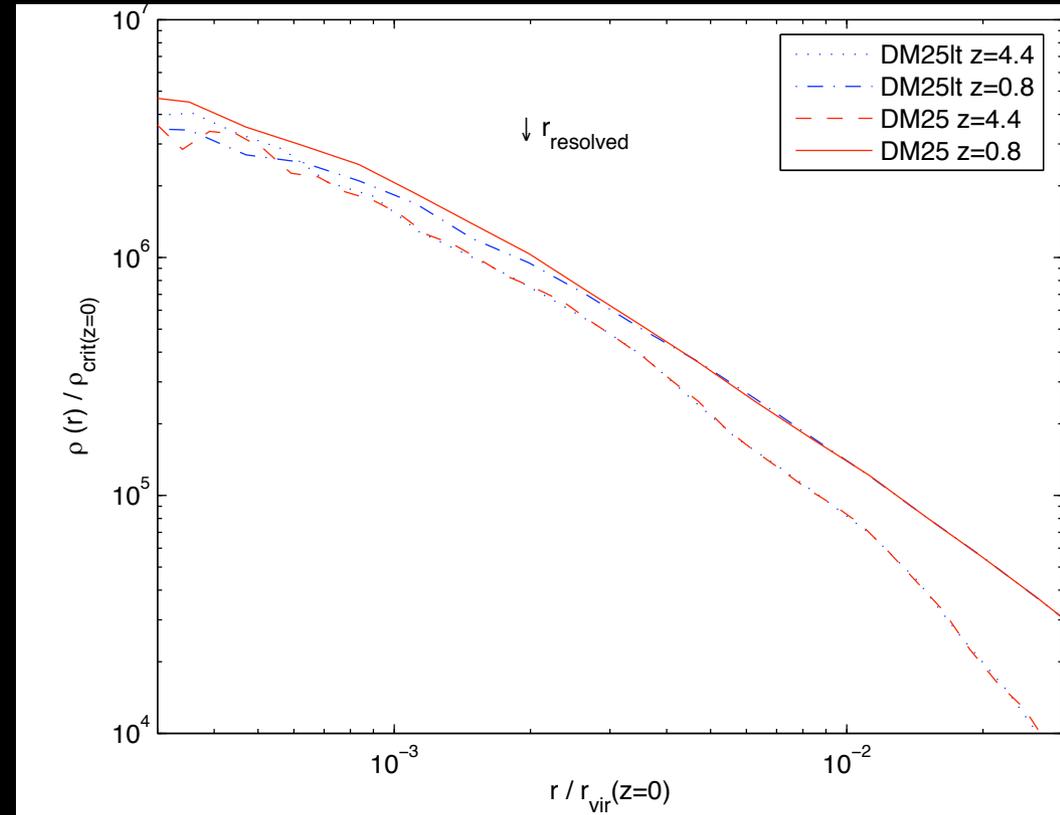
using $\Delta t < \min(\eta \sqrt{\epsilon/a_i}, \eta/4 \sqrt{G\rho_i})$ instead

this ensures steps are at least 12 times smaller than the local dynamical time

$$1/\sqrt{G\rho(< r_i)}$$

but increases CPU time by a factor of two

recently Zemp+2006 have implemented a more efficient algorithm which scales with the local dynamical time everywhere



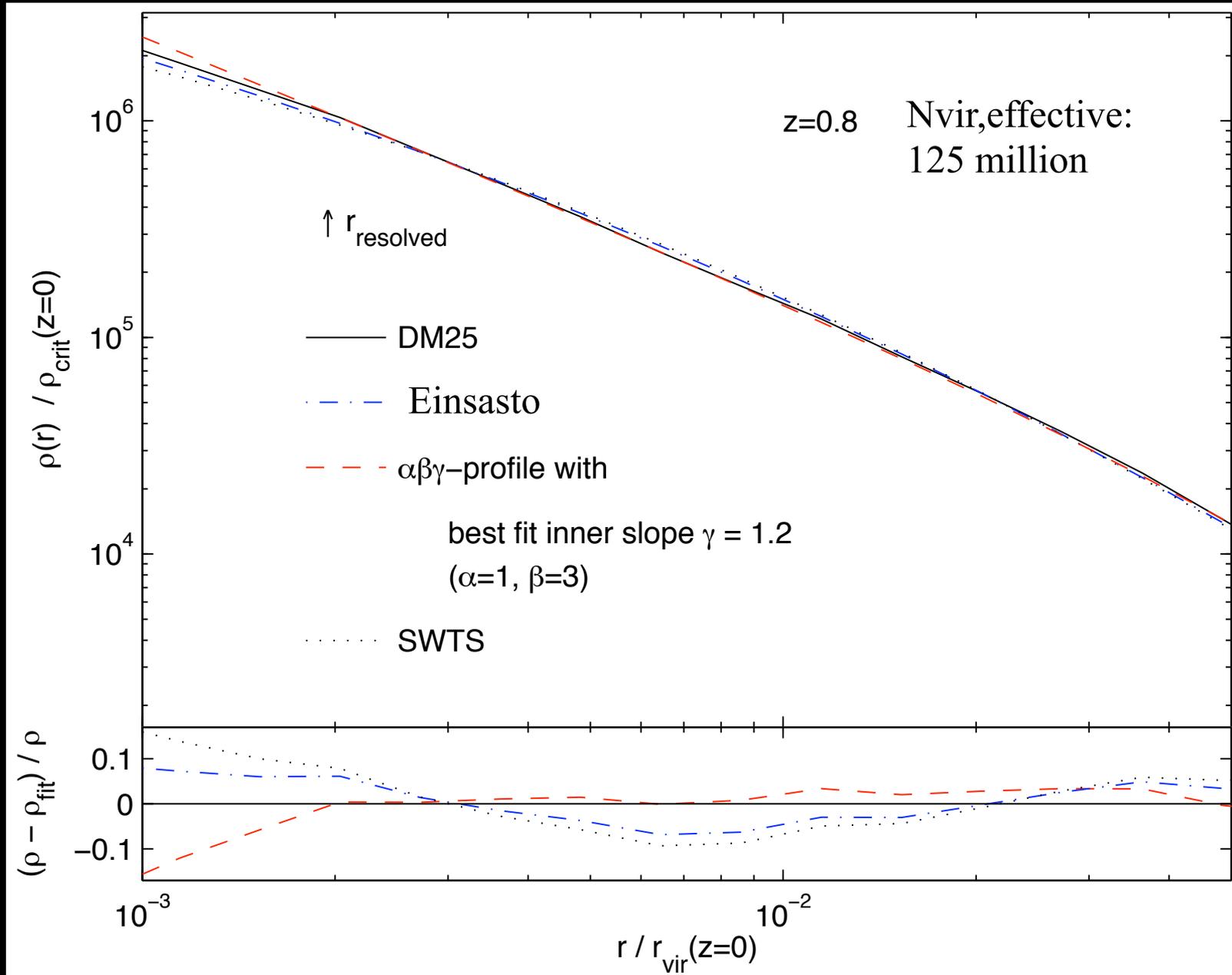
resolving the very inner profile

JD, Zemp, Moore, Stadel, Carollo,
MNRAS, 2005, 364, 665

3 parameter fitting functions

Einasto fit tends to underestimate the very inner densities

even inside of r_{resolved} , where the simulated densities are probably too low



summary : CDM* density profiles

(*) NOTE: in the real universe these profiles would be altered by galaxy formation on some scales

CDM density profile shapes are not exactly universal:
inner slopes at a give fraction of the scale radius have about 0.2 rms halo to halo scatter

outer slopes (near R_{vir}) are very noisy

most CDM clusters are denser than NFW at $0.01 R_{\text{vir}}$, but not as dense as the Moore et al 1999 fit

CDM cluster profiles resolved with around 20 million particles can be fitted equally well with a cuspy gamma-model and with the cored Einasto function

the one halo resolved with substantially higher mass, force and time-resolution is consistent with a -1.2 cusp
its inner halo is denser than the best fit Einasto-model

summary : substructure

small subhalos contribute significantly to the mass fraction in subhalos and to the total DM annihilation signal. therefore both quantities have not converged yet

tides remove subhalo mass from the outside in and lead to higher concentrations for subhalos. the effect is stronger near the galactic center

CDM predicts enough subhalos to host all the currently known Local Group dwarfs

most (97%) subhalos survive from $z=1$ until today. smaller ones loose less mass

high redshift micro-subhalos are only slightly more fragile despite their flat $\sigma(M)$