

*Short gravitational wave signal searches
in TAMA300 data :
stellar core collapse and black hole*

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TAMA collaboration

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Special Thanks to

M.Ando, T.Akutsu, R.Honda and Y.Tsunesada

TAMA's searches for Short GW

- ✦ 1. **Stellar-core collapse (SN) : Burst GW**
 - ✦ 1-1 Excess Power Filter
 - ✦ 1-2 ALF
 - ✦ 1-3 TF-Cluster
- ✦ 2. **Black-hole quasi-normal mode : Ringdown GW**
 - ✦ Matched filter
- ✦ 3. **Keyword for short signal searches**

Observational runs and data

<u>Data Taking</u>	<u>period</u>	<u>actual data amount</u>	<u>remarks</u>
DT1	8/6 - 7/1999	~3 + ~7 hours continuous lock	first whole system test
DT2	9/17 - 20/1999	31 hours	first Physics run
DT3	4/20 - 23/2000	13 hours	
--	8/14/2000	<u>World best sensitivity</u>	$h \sim 5 \times 10^{-21}$ [1/ $\sqrt{\text{Hz}}$]
DT4	8/21 - 9/3/2000	167 hours	stable long run
DT5	3/1 - 3/8/2001	111 hours	
Test Run 1	6/4 - 6/6/2001	Longest stretch of continuous lock is 24:50	keep running all day
DT6	8/1 - 9/20/2001	<u>1038 hours</u> duty cycle 86%	full-dressed run
DT7	8/31 - 9/2/2002	24 hours with duty cycle 76.7%	Recycling, $h \sim 3 \times 10^{-21}$ [1/ $\sqrt{\text{Hz}}$], Simultaneous obs with LIGO & GEO
DT8	2/14 – 4/14/2003	<u>1168 hours</u> , duty cycle 81.1%	coincidence obs with LIGO S2
DT9	10/31(Actually 11/28)/2003 – 1/5/2003	<u>558 hours</u> , (weekday: night time, weekend: full time)	partial coincidence run with LIGO S3 'crewless' operation

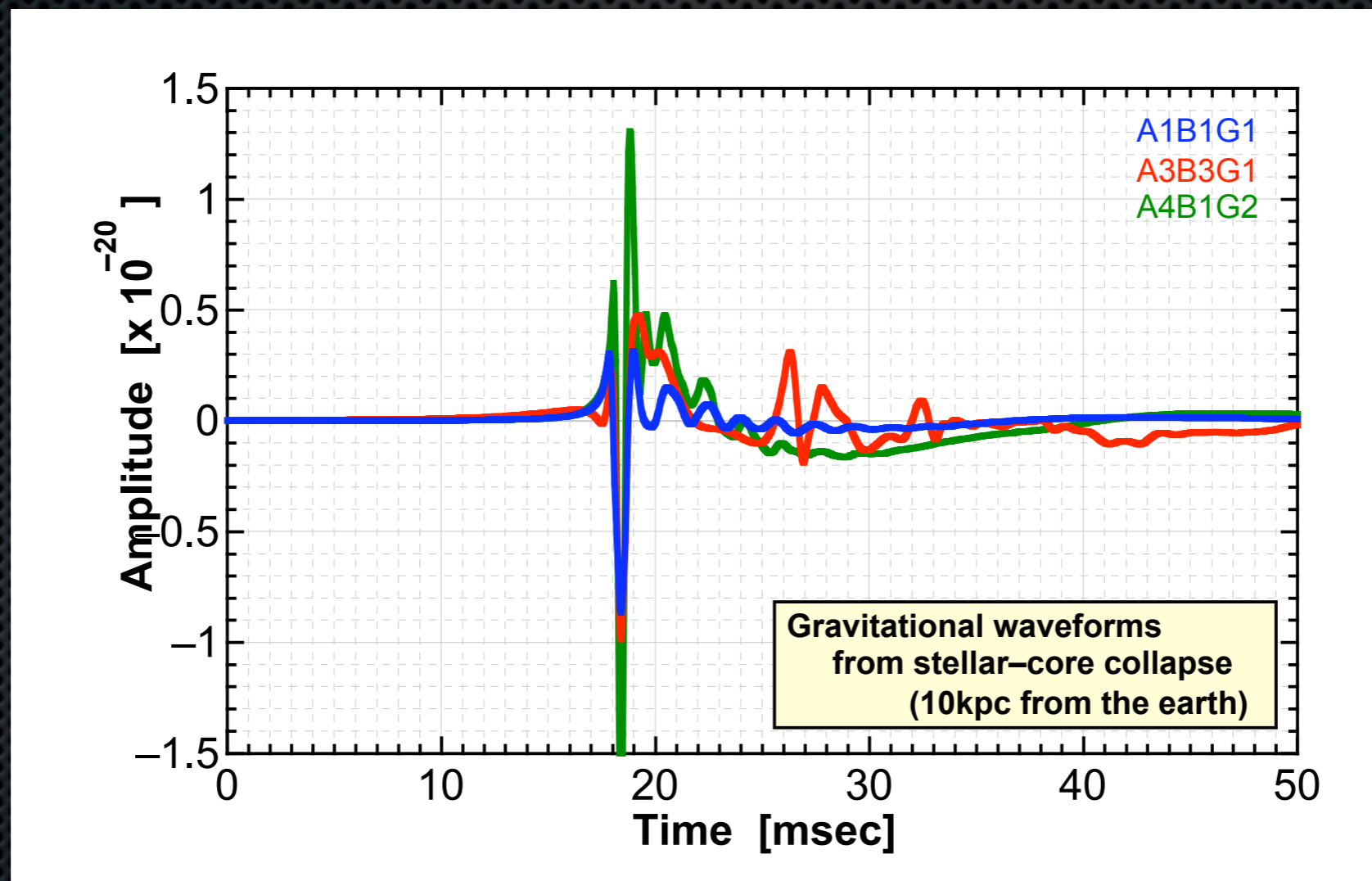
1. Burst Gravitational Waves from Stellar-core collapse

- Numerical Simulation Predicts GW Waveform.

Komatsu et al. (1989)

Zwenger & Müller (1997)

[Dimmelmeier et.al., \(2001,2002\)](#)



TAMA300 Sensitivity : Range of Detection for Burst GW from Stellar-Core Collapse

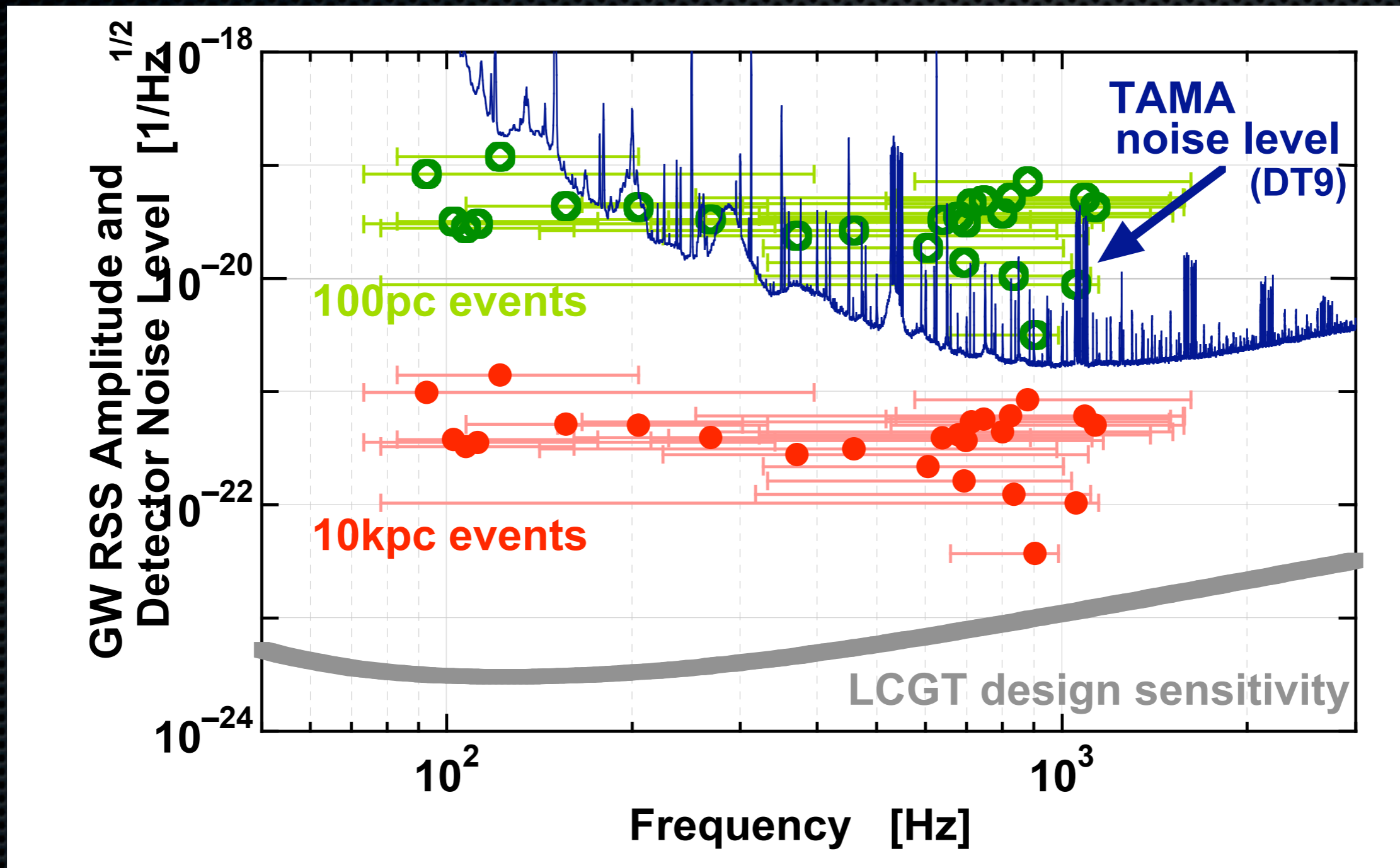
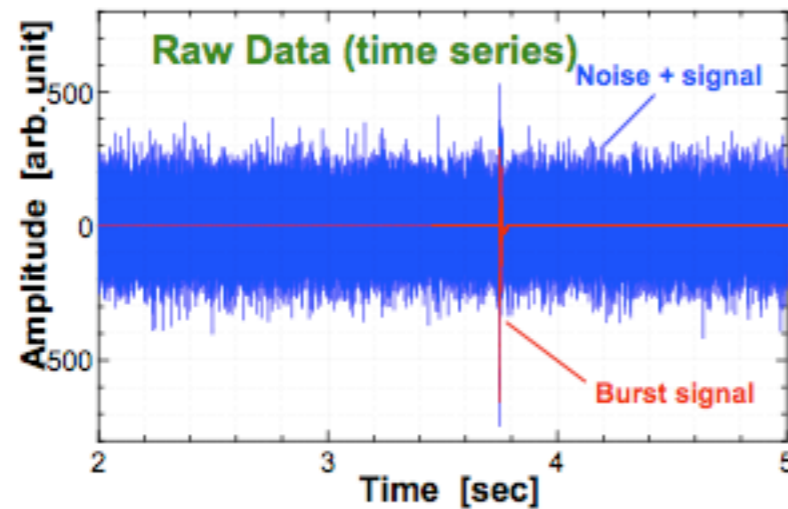


Figure by M.Ando,
GW signals by Dimmelmeier, et al. (2002)

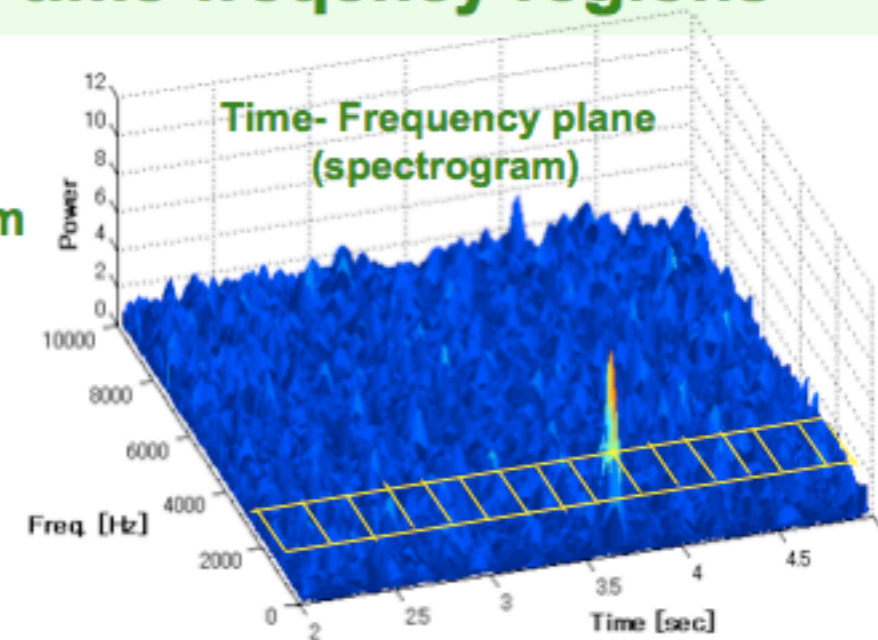
1-1. Excess Power Filter

Burst filter: Excess-power filter

Evaluate **signal power** in given **time-frequency regions**



Fourier transform



Few assumptions for signal ...
time-frequency bands
Robust for waveform uncertainties

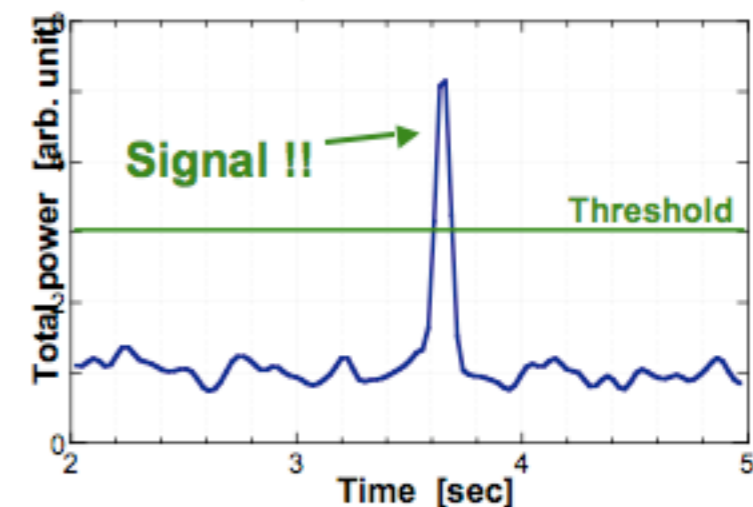


Total power
in given T-F region

Selected parameter:

$$\Delta t = 12.8 \text{ [msec]}$$

$$\Delta f = 2300 \text{ [Hz]}$$



Upper-limit results

- Event candidates

Event-selection threshold : $\text{SNR} > 2.9$

➡ **Detection efficiency** : 1×10^{-5}
Observation result : 7×10^{-2} events/sec

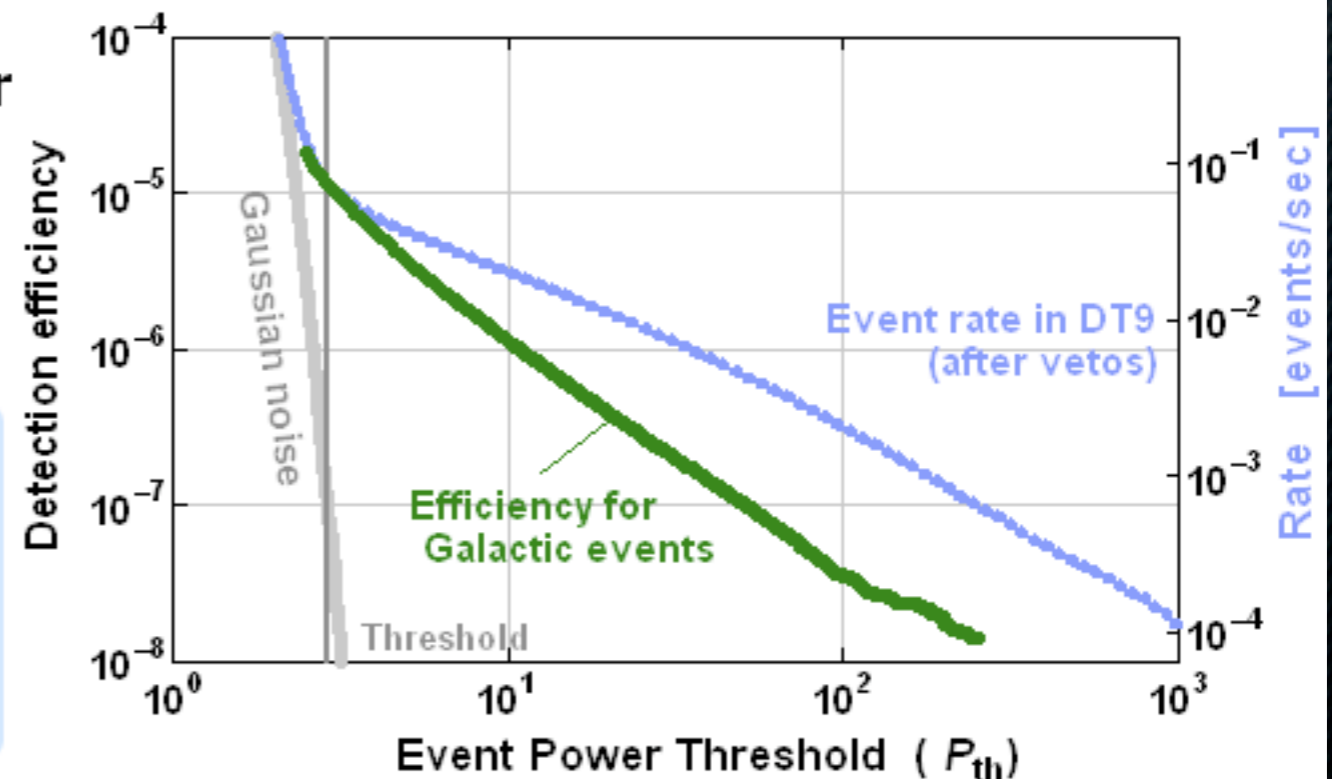
- Upper limit

Assume a Poisson distribution
for the observed event number

$$N_{\text{obs}} \rightarrow N_{\text{ul}}$$

$$R_{\text{ul}} = \frac{N_{\text{ul}}}{\epsilon_{\text{gal}} \cdot T_{\text{obs}}}$$

Galactic event rate
 5×10^3 events/sec
GW energy rate
 $4 \times 10^{-4} M_{\odot} c^2/\text{sec}$
(90% C.L.)

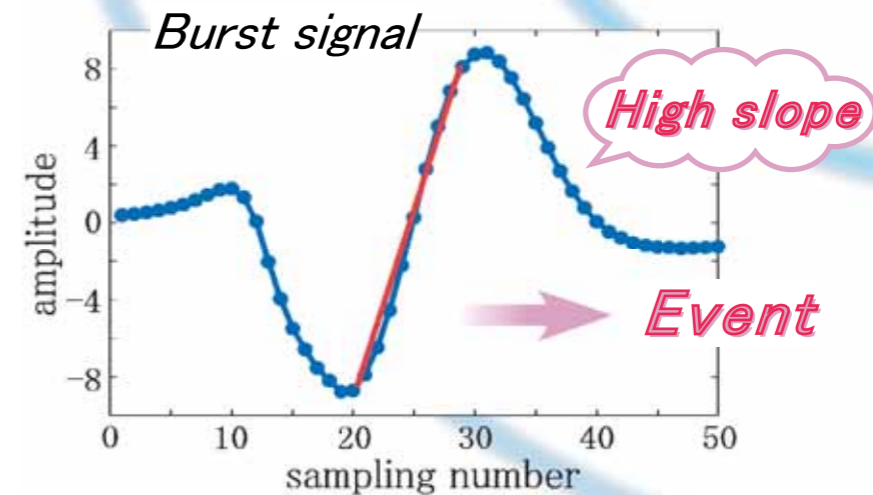
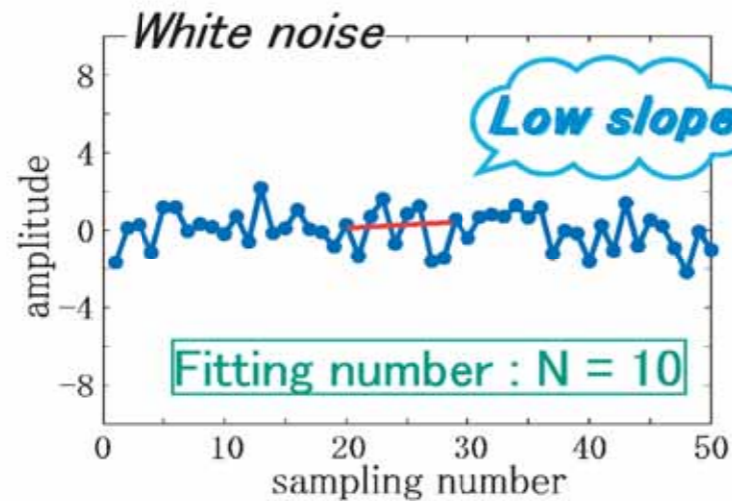


by M.Ando

Phy. Rev. D71, 082002 (2005)

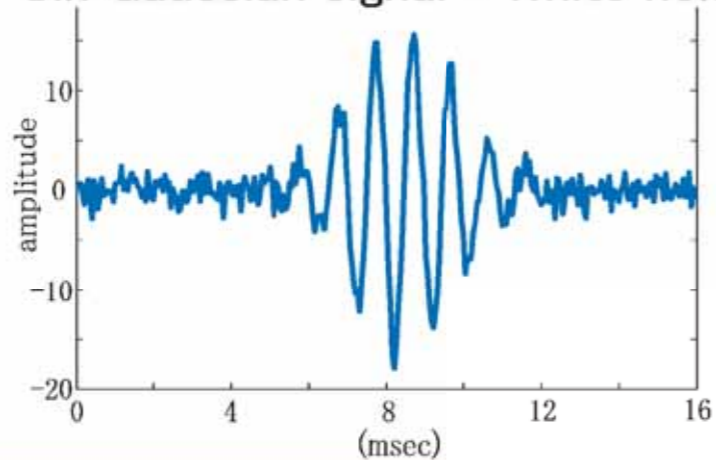
1-2. ALF (Alternative Linear Filter)

A slope value of a raw of data (N samples) is used to trigger an event.
When there is a white noise, a slope value is low. If there is a burst signal, a slope value will be high.

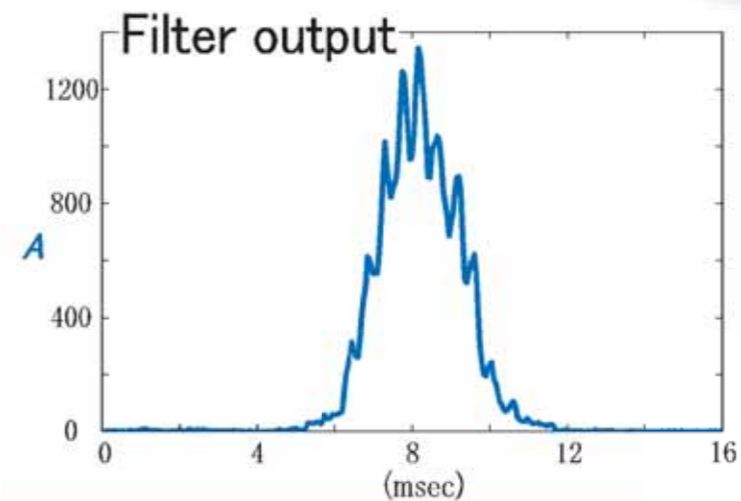


example

Sin Gaussian signal + White noise



ALF filter [3]
is applied



by Tomomi Akutsu (ICRR, Tokyo Univ. / Osaka City Univ.),

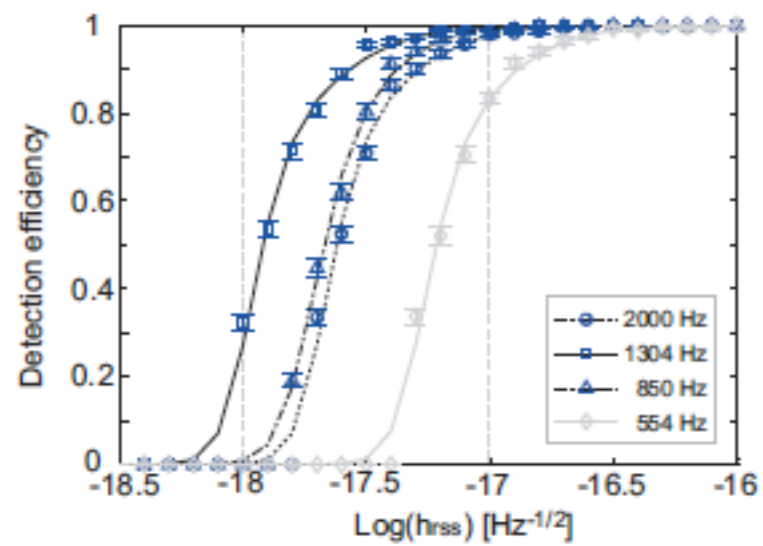


Figure 4. Detection efficiency for sine-Gaussian signals.

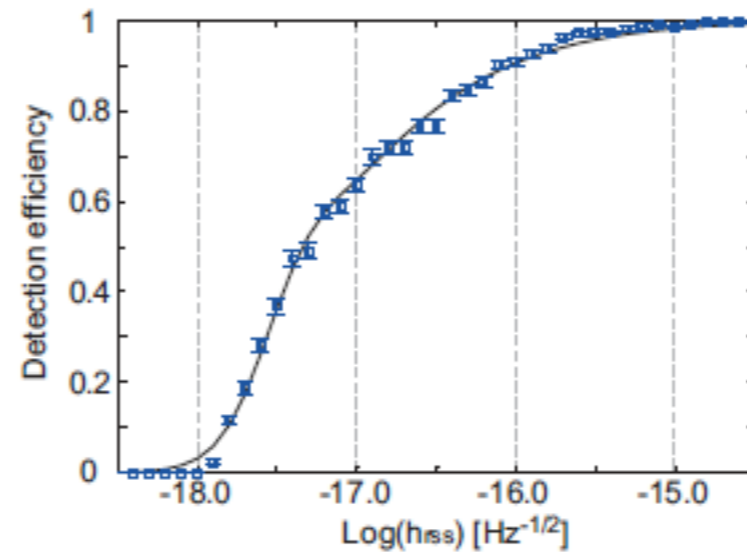


Figure 5. Detection efficiency for the DFM catalogue signals.

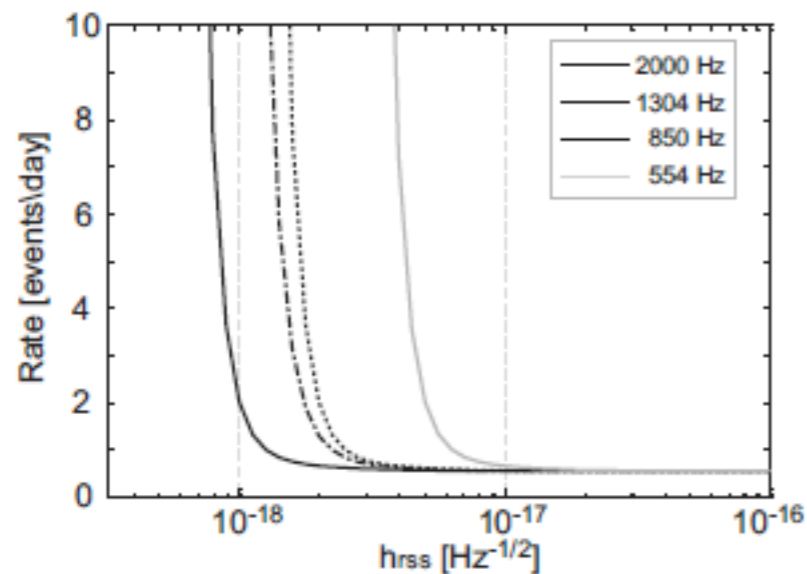
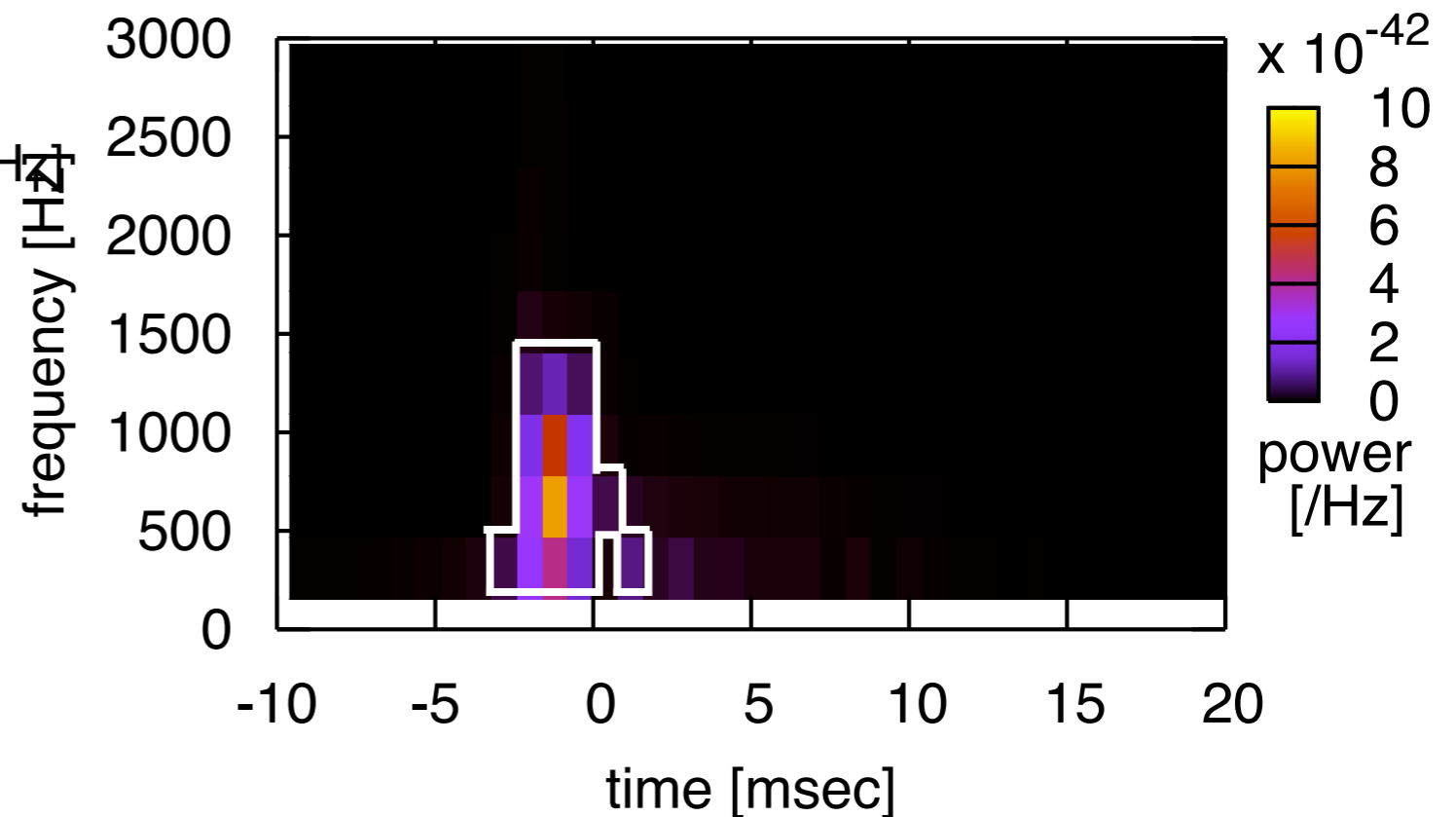
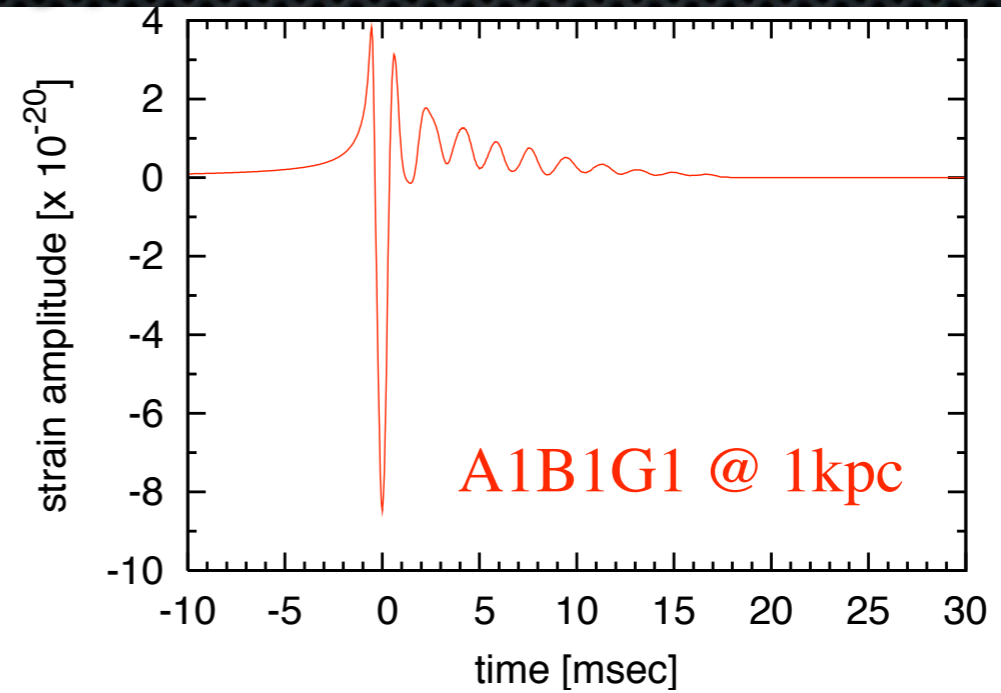
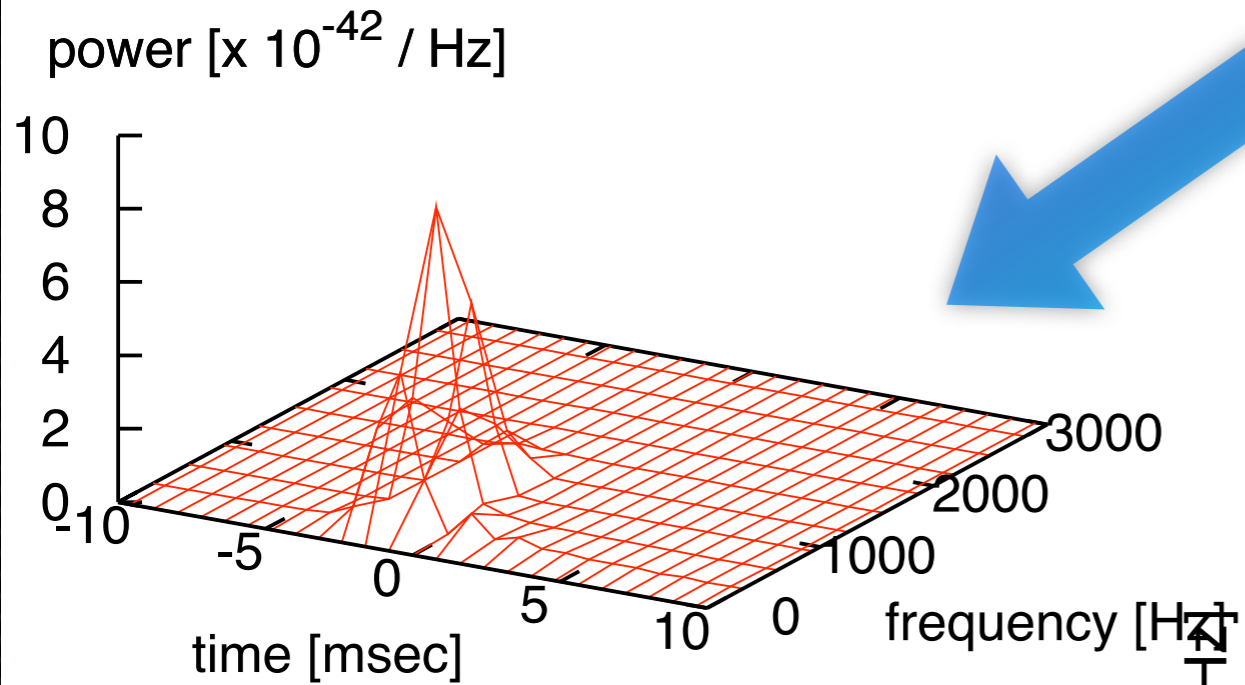


Figure 6. Rate limit for GW amplitude h_{rss} . A vertical axis and a horizontal axis are a rate limit [events/day] with a confidence level 90 % and h_{rss} amplitude, respectively. At the level of $h_{\text{rss}} = 10^{-17}$, we obtained 0.55 events/day of upper rate limit with 90 % confidence level.

*U.L. for $h_{\text{rss}} > 10^{-17}$
0.55 [events/day] , C.L.90%*

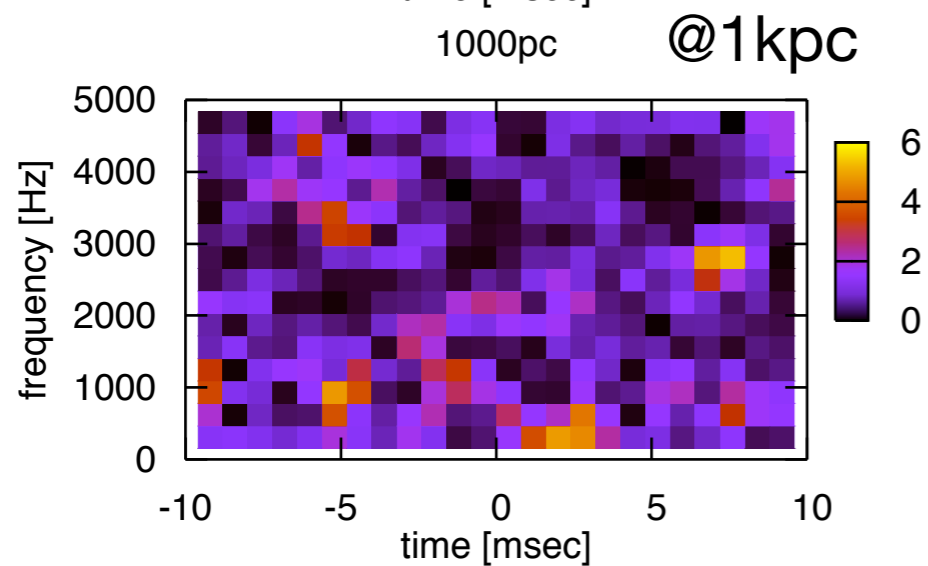
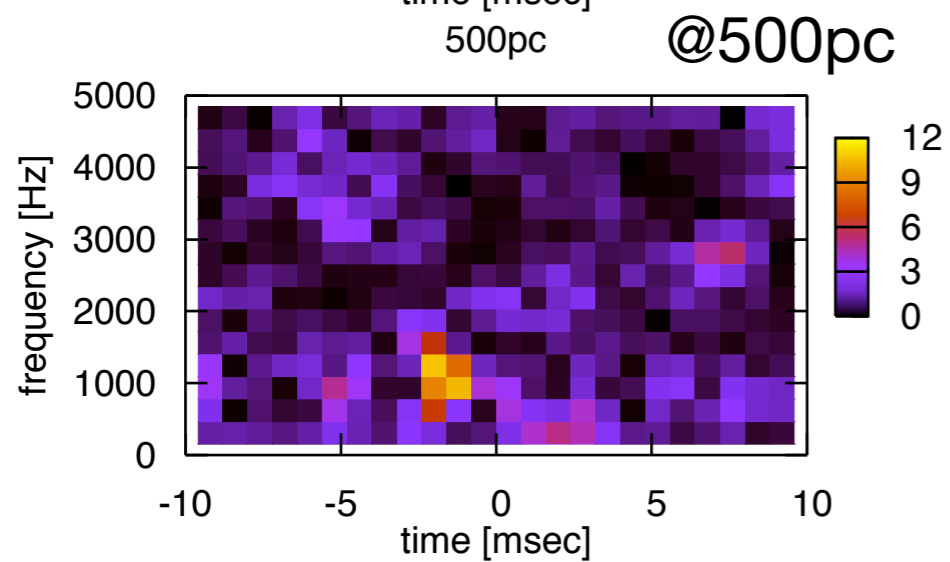
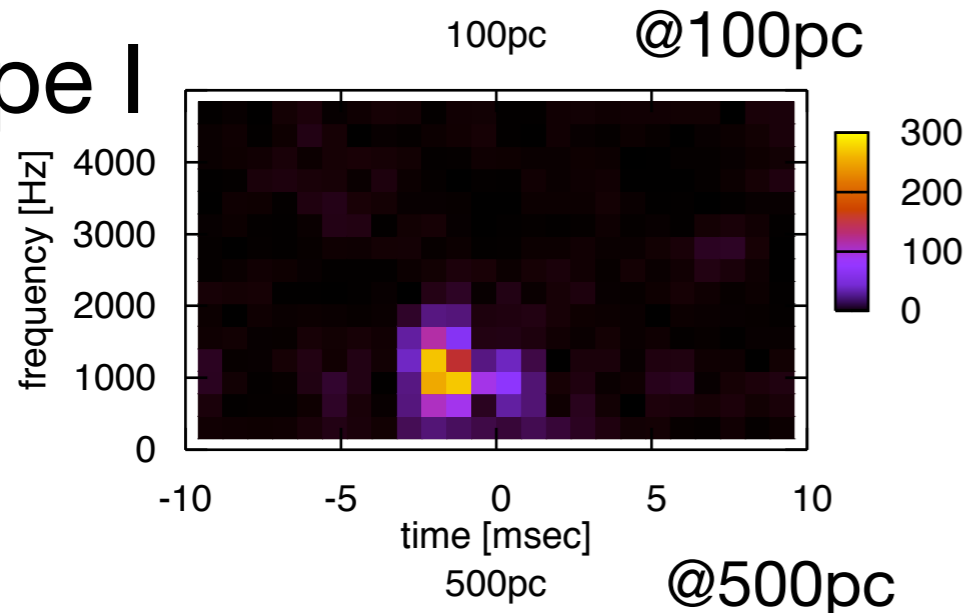
by Tomomi Akutsu , et al.
Class. Quantum Grav. 23 (2006) S715

1-3 TF (Time-Frequency) - cluster

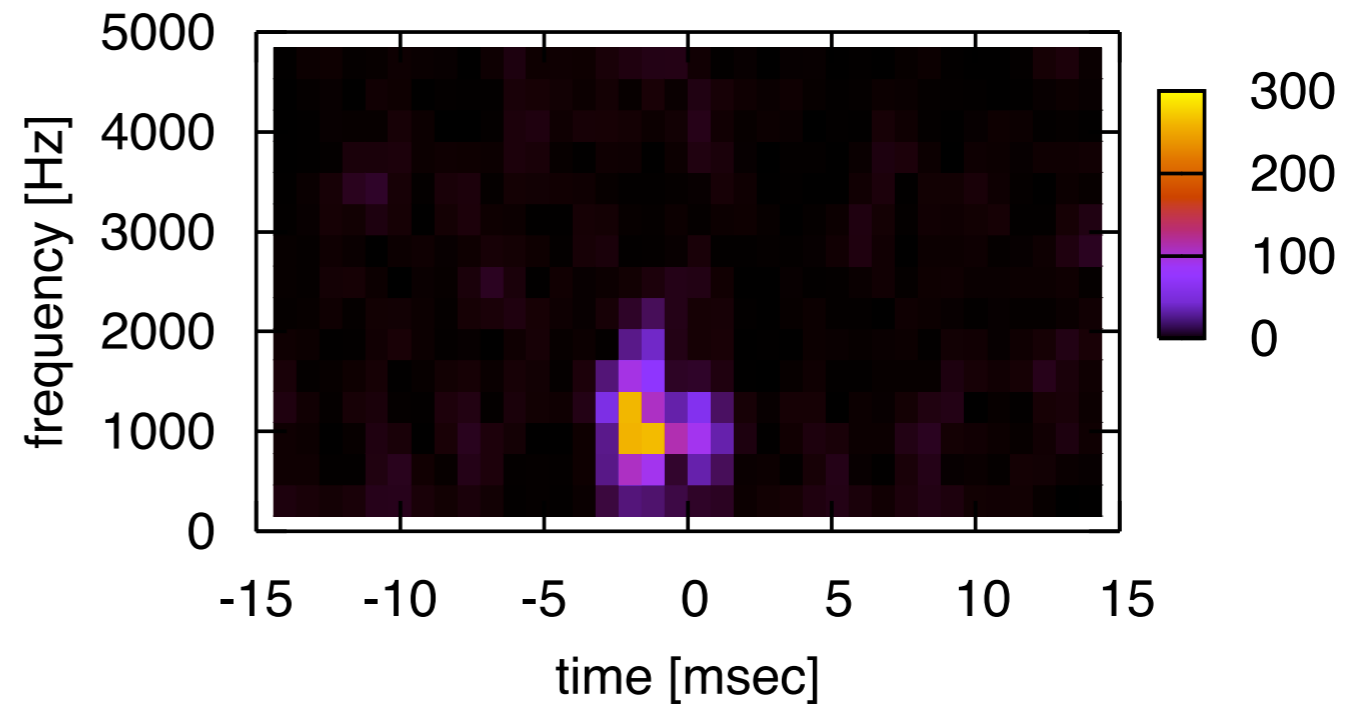


Example

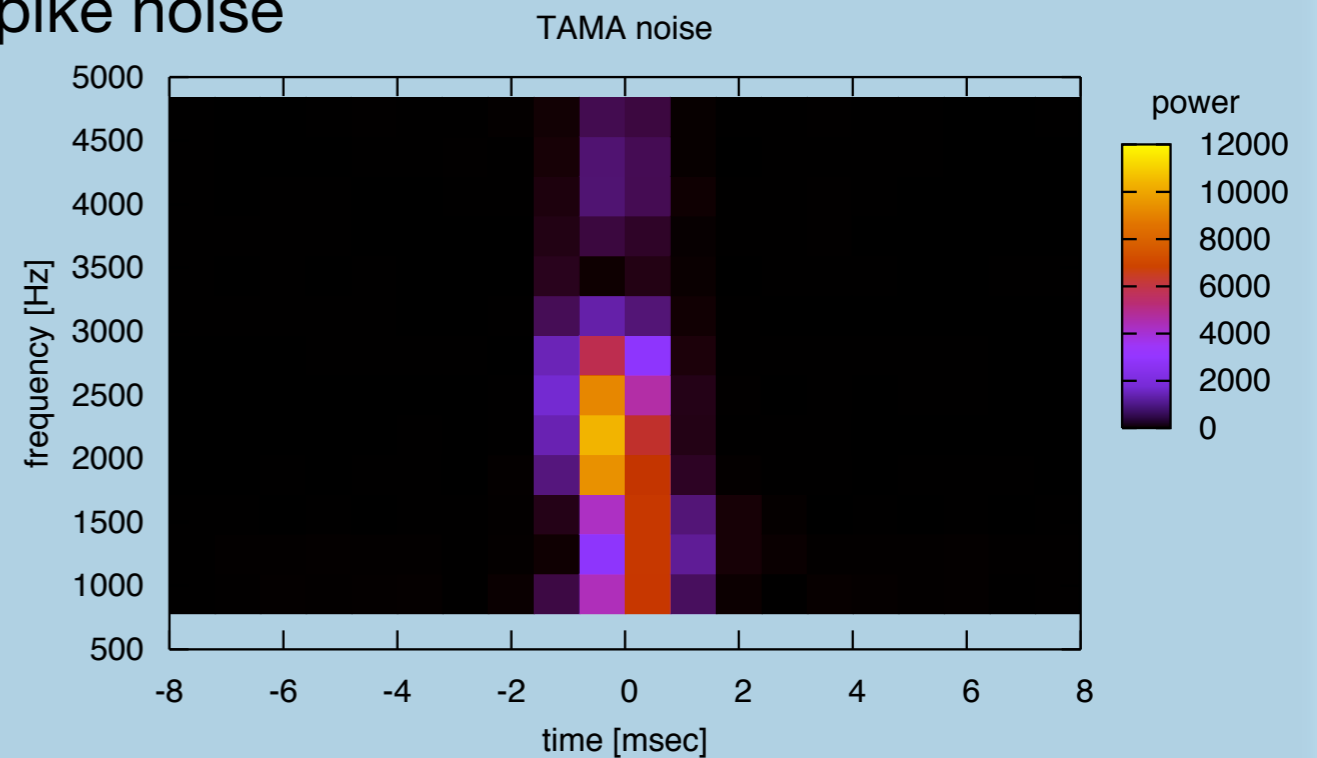
Type I



A4B2G2 type I/II



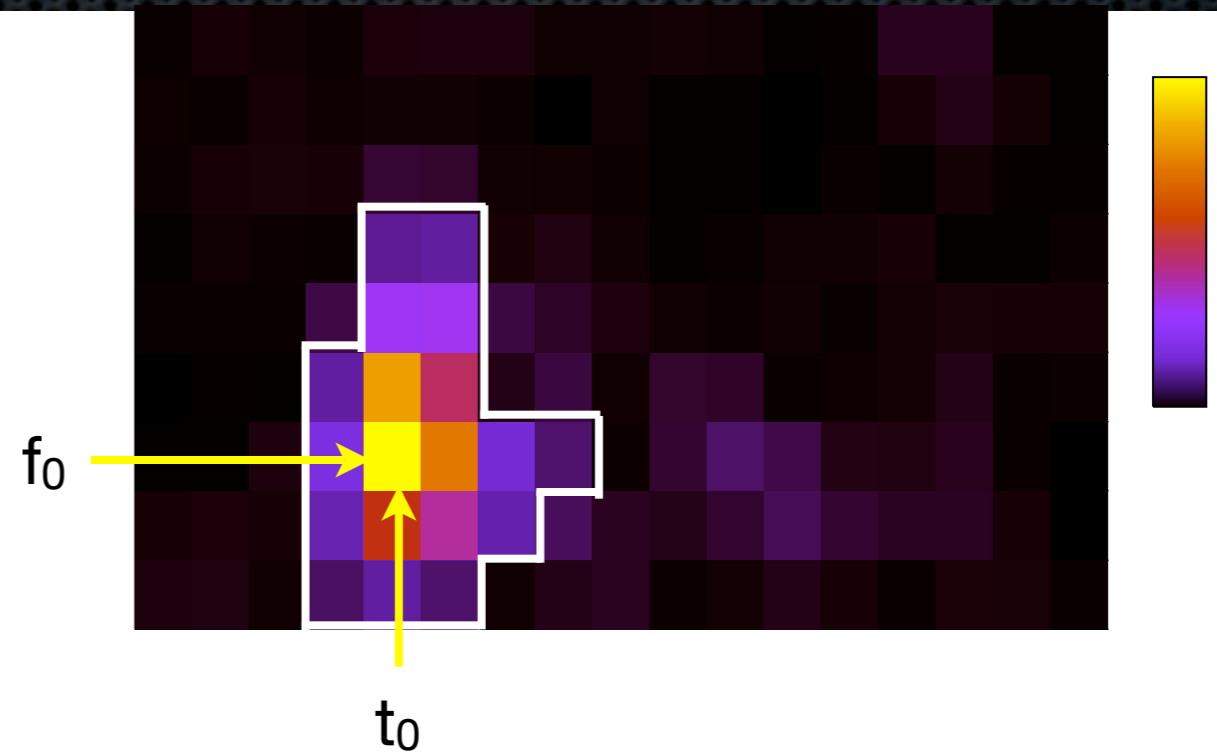
Spike noise



Clustering (recognition of connected region)

peak height : $P(t_0, f_0)$

cluster threshold : $P(t_0, f_0)^{1/2}$



cluster characteristics parameters :

$$S = \sum_{t,f} 1$$

$$V = \sum_{t,f} P(t, f)$$

$$t1s = \frac{\sum t}{S}$$

$$t2s = \frac{\sum (t - t1s)^2}{S}$$

$$t3s = \frac{\sum (t - t1s)^3}{S(t2s)^{3/2}}$$

$$t4s = \frac{\sum (t - t1s)^4}{S(t2s)^{4/2}}$$

$$t1v = \frac{\sum tP(t, f)}{V}$$

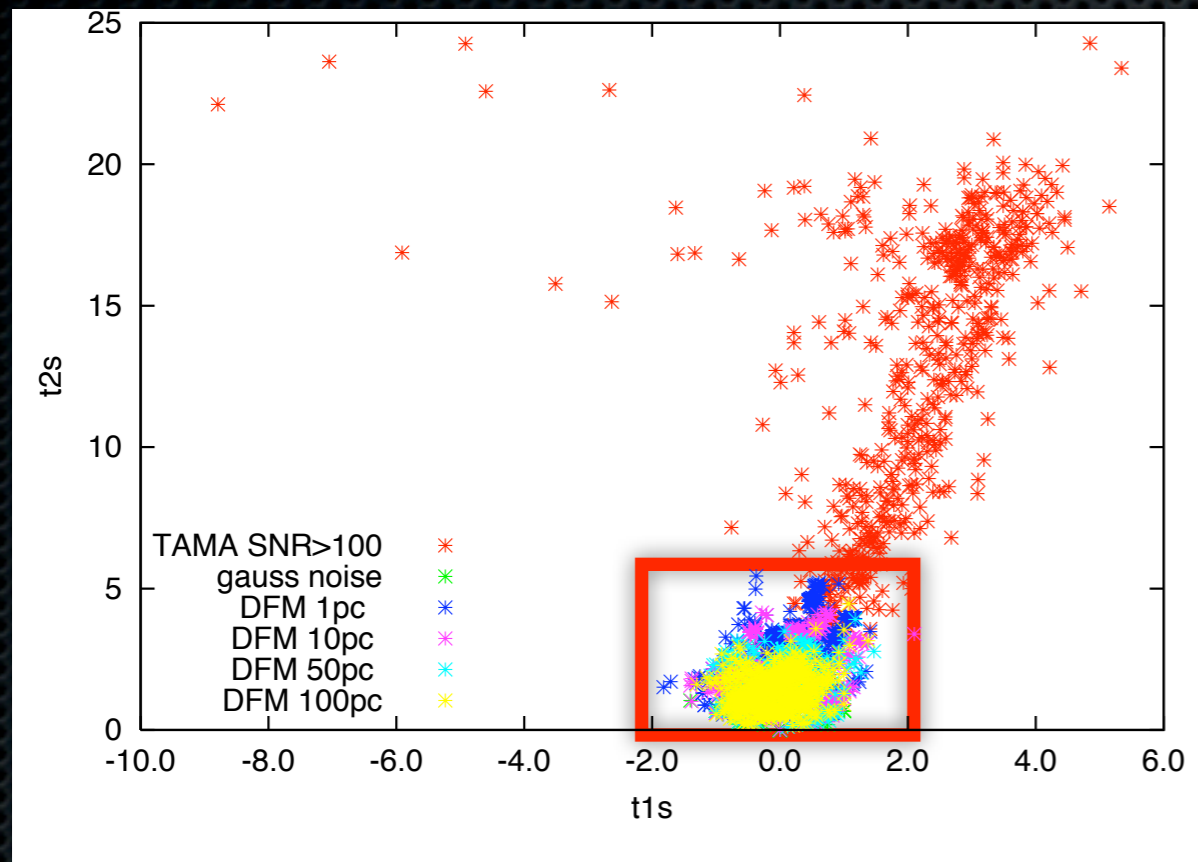
$$t2v = \frac{\sum (t - t1v)^2 P(t, f)}{V}$$

$$t3v = \frac{\sum (t - t1v)^3 P(t, f)}{V(t2v)^{3/2}}$$

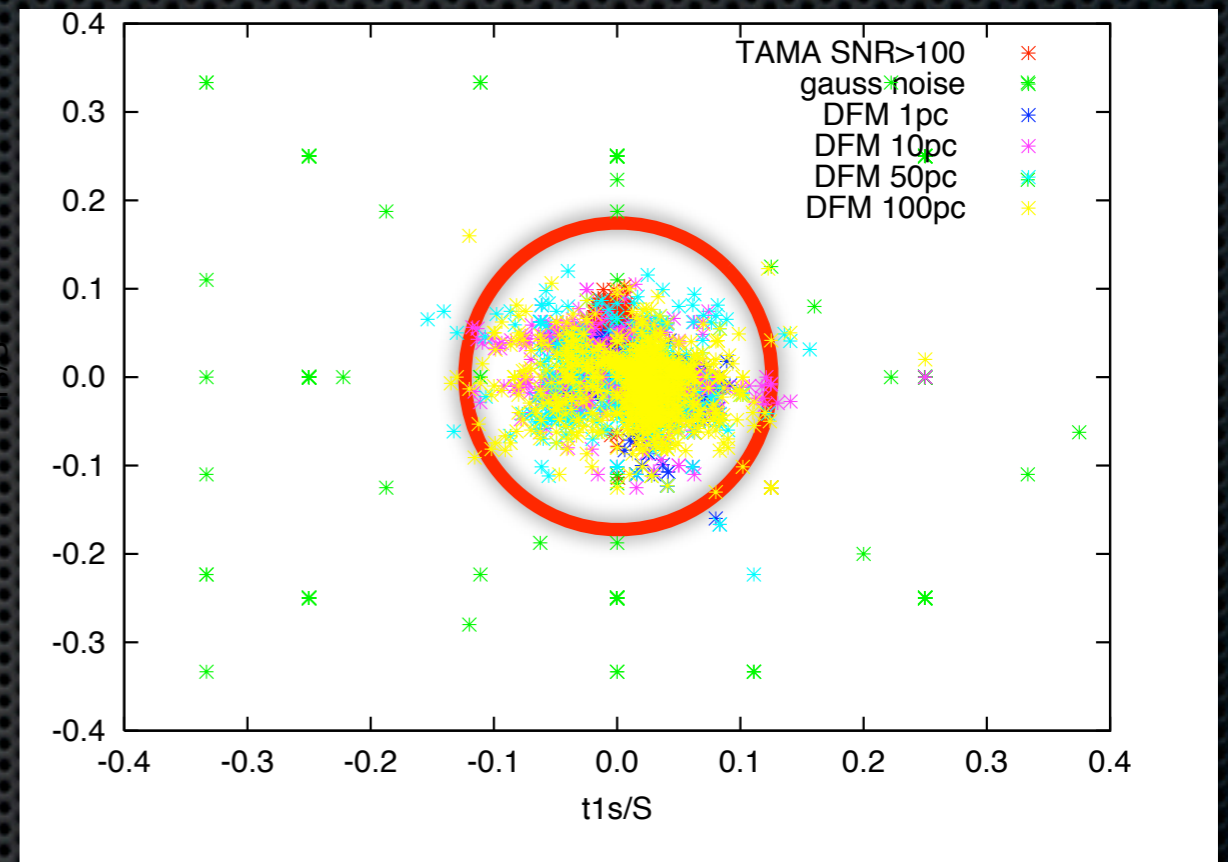
$$t4v = \frac{\sum (t - t1v)^4 P(t, f)}{V(t2v)^{4/2}}$$

TF-cluster : Event Selection

exclude TAMA noises
f1s vs f2s



exclude Gauss noise
t1s/S vs f1s/S



$$-2.0 \leq f1s \leq 2.0$$

$$f2s \leq 5.0$$

$$(t1s^2 + f1s^2)^{1/2} / S \leq 0.15$$

$$S \geq 4$$

$$F \leq 4$$

$$(1250\text{Hz})$$

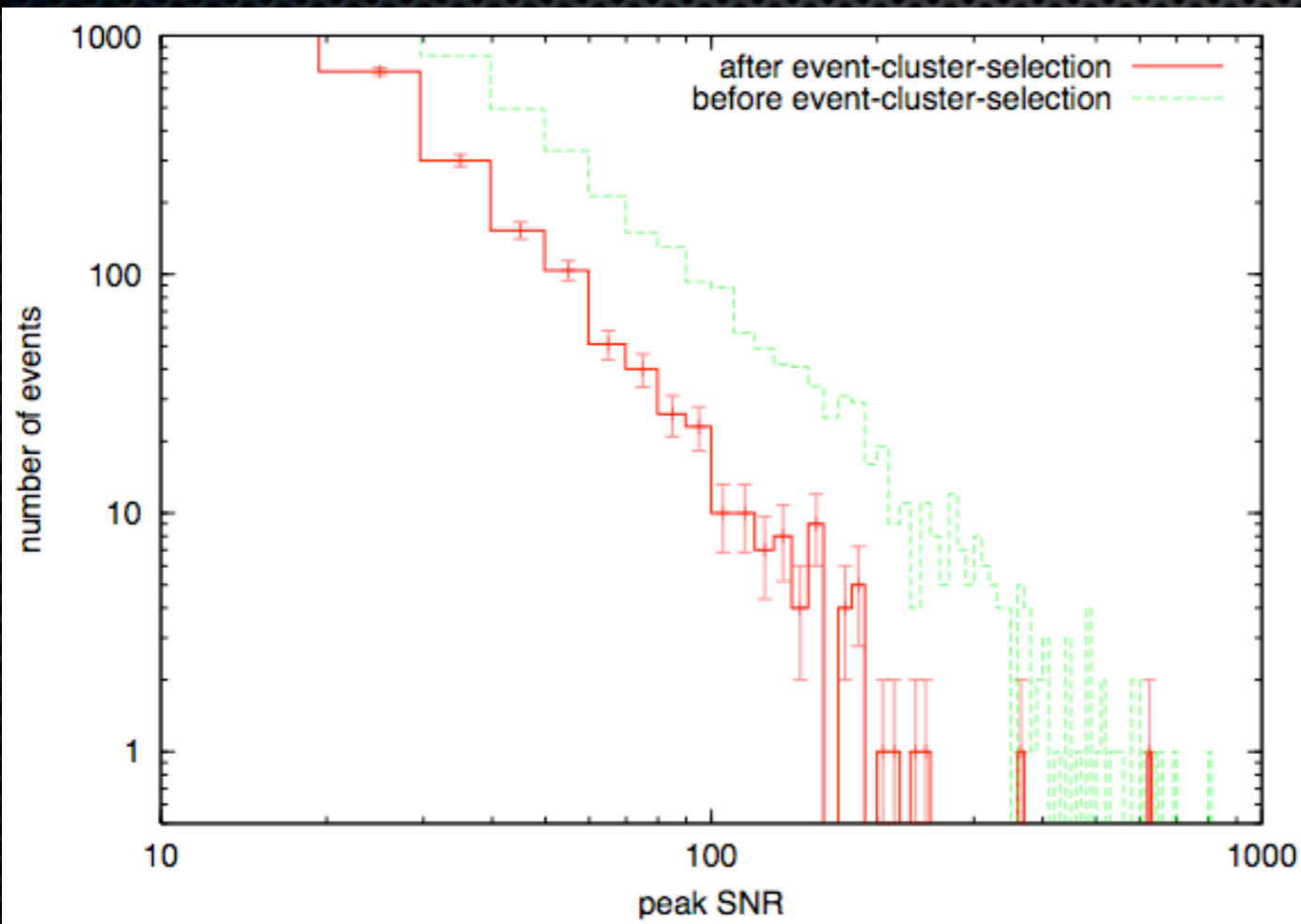
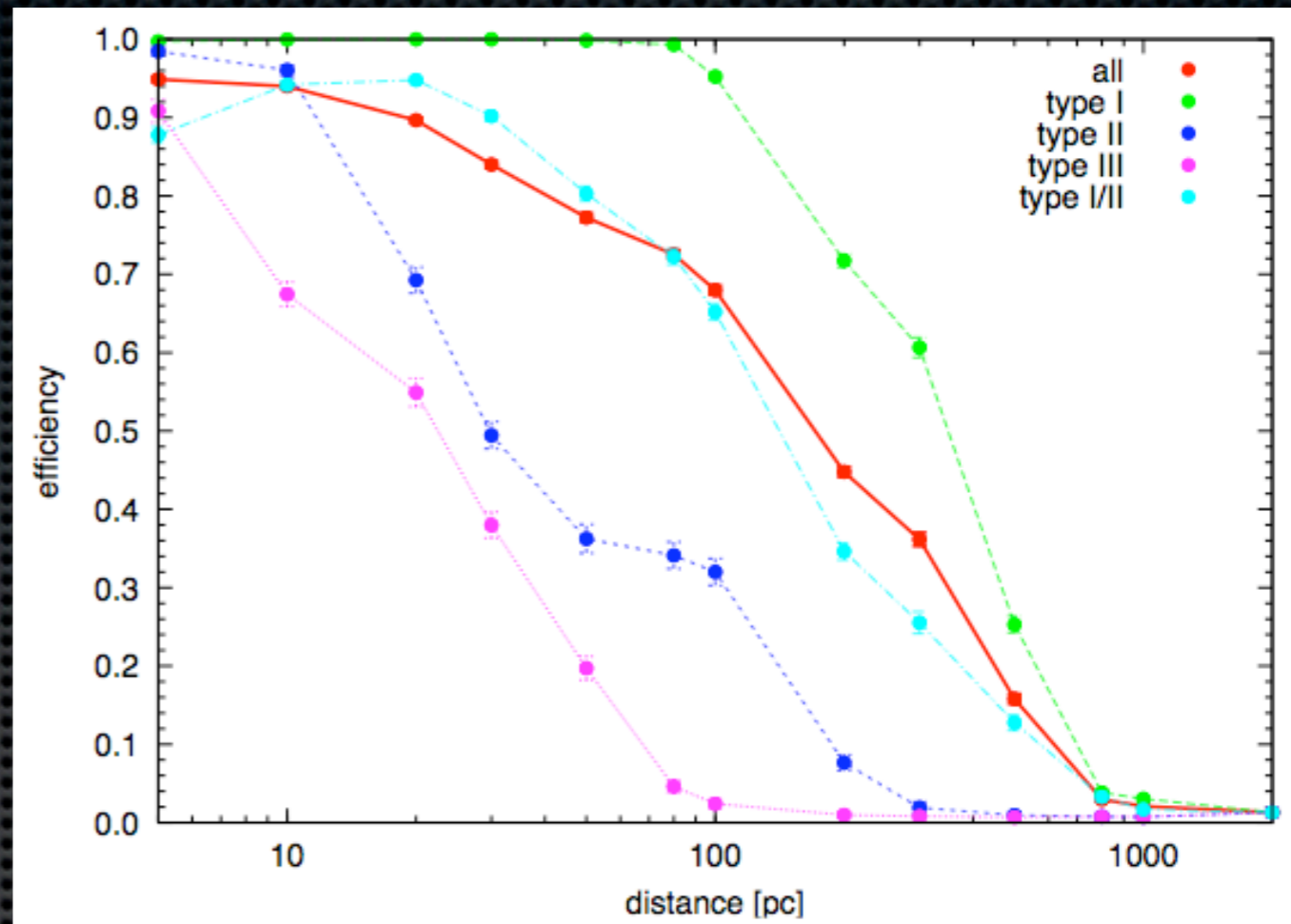
$$-1.5 \leq t1v \leq 1.5$$

$$t2v \leq 3.0$$

$$f4v \leq 6.0$$

$$t2v^{1/2} / S \geq 0.04$$

Efficiency and Selected Events



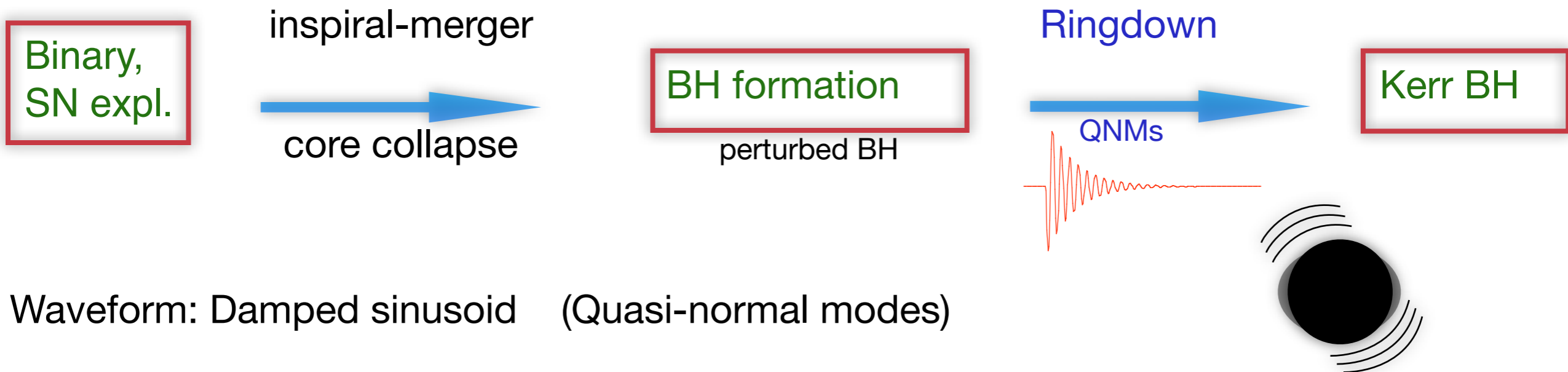
efficiency = 86 % within 10pc
(SNR > 70)

$N = 152$ event for 1.26×10^5 sec
data

Rate = $N / (T \times \text{efficiency})$
= 1.4×10^{-3} events/sec
= 4.9 events/hour

by R.Honda (Osaka City Univ.),
Master Thesis, Feb. 2007

2. Ringdown GW from black-hole quasi-normal mode



$$h(t) = \exp(-\pi f_c t / Q) \sin(2\pi f_c t)$$

central frequency

$$f_c = \frac{3.2 \times 10^4 [\text{Hz}]}{M/M_\odot} \left[1 - (1 - a)^{0.3} \right] \quad \text{Echeverria (1989)}$$

Quality factor

$$Q = 2.0(1 - a)^{-0.45}$$

M: Mass

a: Spin

- * Probe for BH direct observation
- * BH physics in inspiral-merger, core collapses, ...
- * Good SNR expected, ~ 100 @10kpc (TAMA sensitivity)

Matched Filter Design for BH Ringdown

$$\rho = \int \frac{s(f)h^*(f; f_c, Q)}{S_n(f)} df$$

$s(f)$: signal + noise
 $h(f)$: template
 $S_n(f)$: Weight (noise power)

Template construction in (f_c, Q) plane
 (Nakano, Takahashi, Tagoshi, Sasaki, PRD 2003)

$$f_c = 100 \sim 2500 \text{ [Hz]}$$

$$Q = 2 \sim 33.3 \quad (a = 0 \sim 0.998)$$

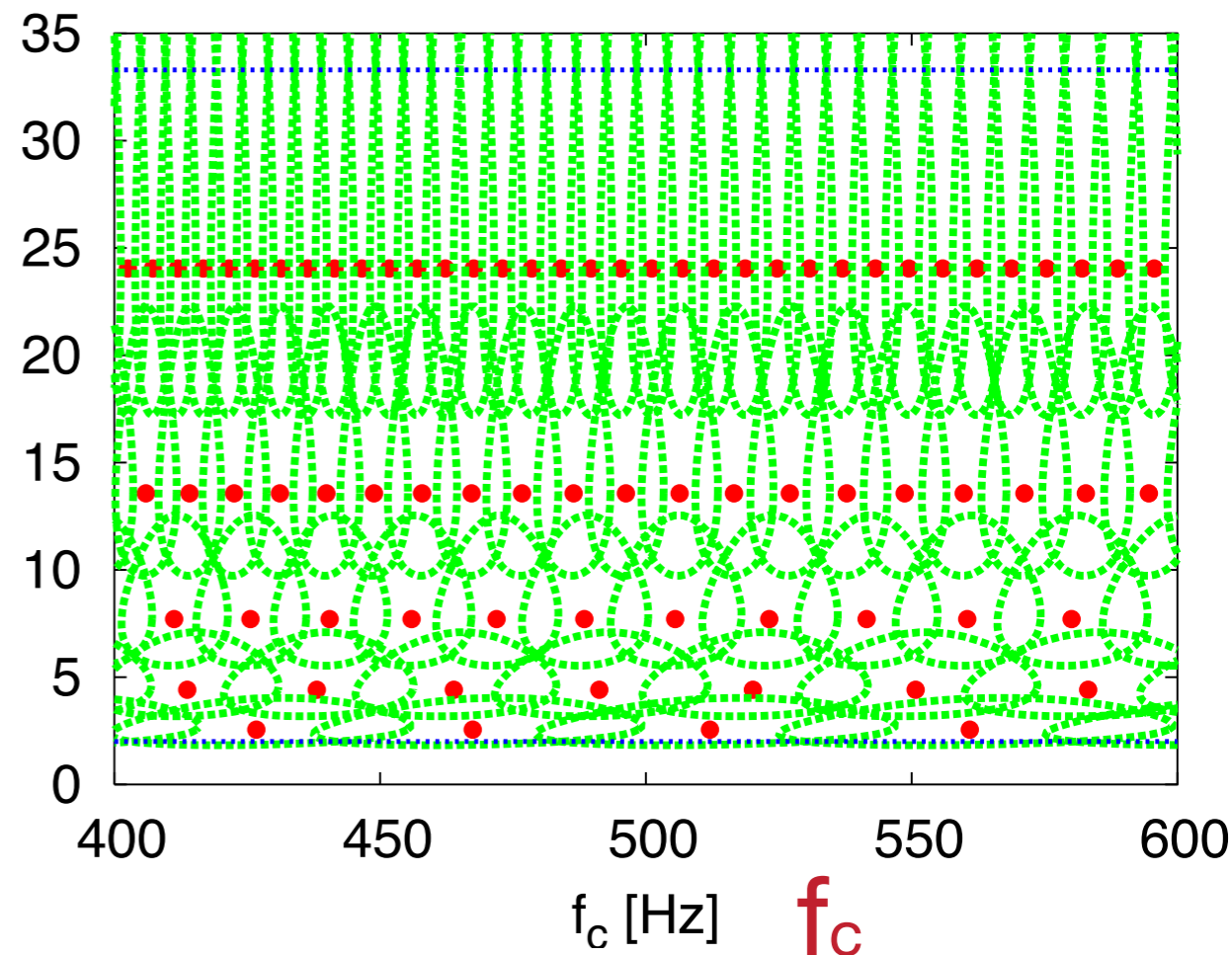
682 templates (SNR loss < 2%)

CPU Time

Intel PenIV 2.5GHz

$$T_{50s}^1 = 130 \left(\frac{N_{\text{tmplt}}}{682} \right) \text{ [sec]}$$

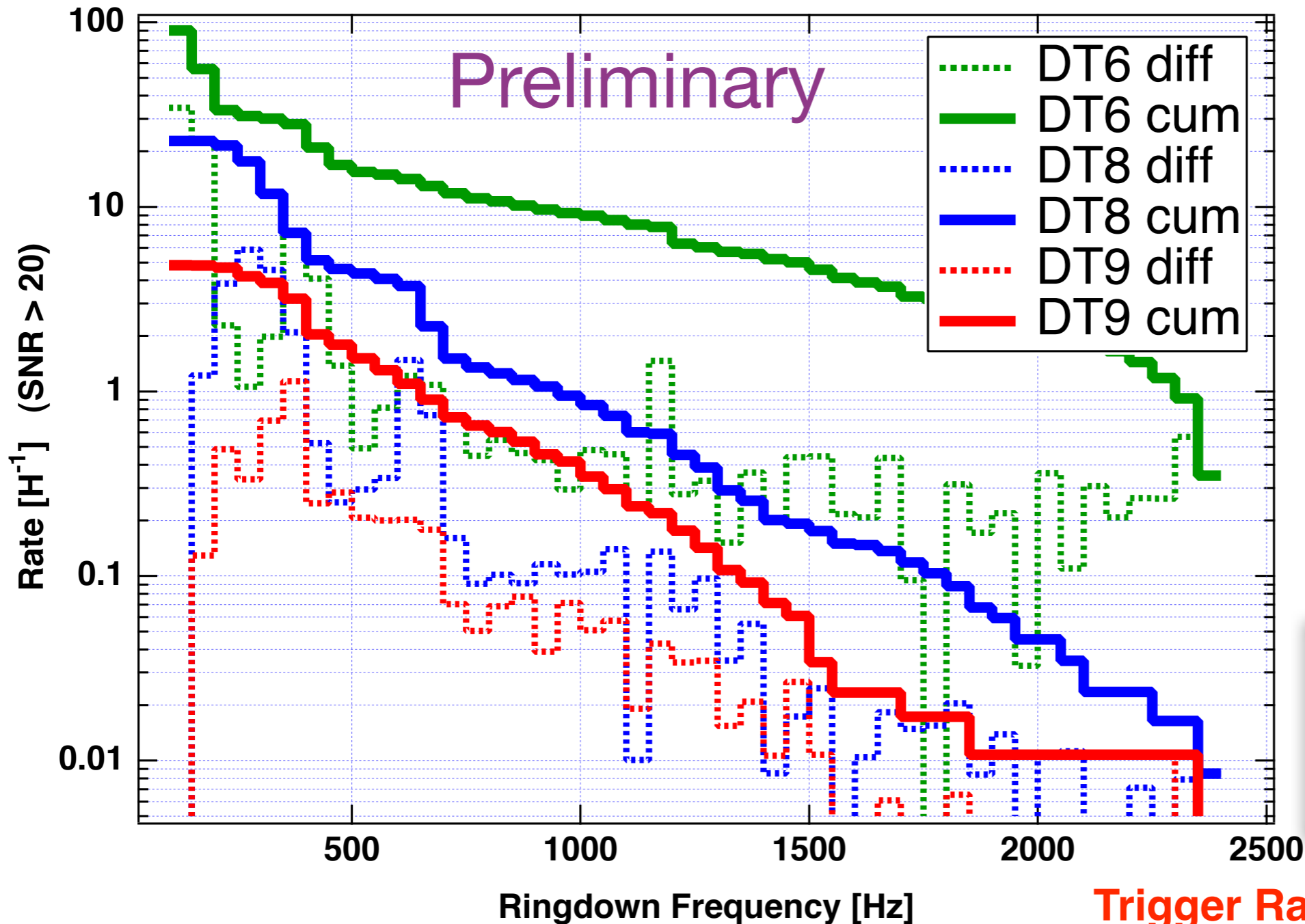
$$T_{1000h} = 6.5 \left(\frac{N_{\text{tmplt}}}{682} \right) \left(\frac{16}{N_{\text{CPU}}} \right) \text{ [days]}$$



Trigger Rate of the Ringdown Search

$$R(f_c) = \frac{N_{\text{trg}}(f_c)}{T_{\text{obs}}} \frac{1}{\epsilon(f_c)} \frac{1}{1 - (\text{false dismissal})}$$

Preliminary



$f_c > 1500\text{Hz}$:
($M < 20M_{\text{solar}}$)

DT6:

$R < 4.6 [\text{H}^{-1}]$

DT8:

$R < 1.8 \times 10^{-1} [\text{H}^{-1}]$

DT9:

$R < 3.4 \times 10^{-2} [\text{H}^{-1}]$
(SNR > 20)

Trigger Rate (DT9) < 1ev/day

by Y.Tsunesada

BH Mass Spectroscopy ...

- Ringdown GW detection can measure;
- Q = Kerr parameter
- f_c = Mass of BH

Q^M	$(\Delta f_c/f_c)_{\text{RMS}}$	$(\Delta Q/Q)_{\text{RMS}}$	$(\Delta M/M)_{\text{RMS}}$	$(\Delta a/a)_{\text{RMS}}$
All	1.3 (1.2)%	22 (16) %		
2.55	8.1 (2.6)	22 (16)	22 (12) %	64 (35) %
4.41	4.0 (1.6)	24 (16)	13 (6.6)	41(35)
7.70	1.6 (1.0)	21 (16)	6.8 (3.9)	39 (36)
13.6	0.77 (0.58)	19 (16)	3.1 (2.4)	40 (36)
24.0	0.39 (0.33)	19 (17)	1.9 (1.6)	41 (37)

3. *Keyword for short signal searches*

- ✦ Different types of 'waveforms' and search methods
 - ✦ Burst : only numerical predicted, power filter
 - ✦ Ringdown : analytical prediction, matched filter
- ✦ Even so, there are same noise sources !
 - ✦ Spike, Glitch, Steps...
 - ✦ Non-Gaussianity
 - ✦ Instability
 - ✦ Short GW search requires 'silent detector'.

Summary

- ✦ TAMA searched for short GW signals, and derive upper limits:
 - ✦ Burst GW
 - ✦ Excess power filter, ALF, TF cluster
 - ✦ BH ringdown GW
 - ✦ Matched Filter
- ✦ The data analysis evaluated a kind of TAMA detector noise characteristics.