

# **A method for searching for gravitational waves triggered by astronomical observations**

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**Shantanu Desai**  
**(Pennsylvania State University)**

**Tiffany Summerscales**  
**(Andrews University)**

# Contents

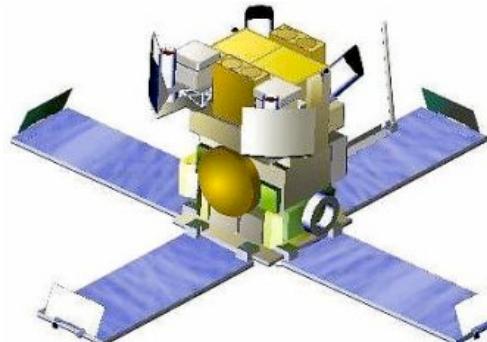
- Gravitational wave search triggered by electro-magnetic observations
- World-wide detector network
- Coherent network analysis
- “RIDGE”--fully coherent network analysis
- Application: monitoring Sco X-1, the strongest X-ray emitted LMXB(low mass X-ray binary).

# Triggered search



LIGO

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HETE

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RXTE

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SWIFT

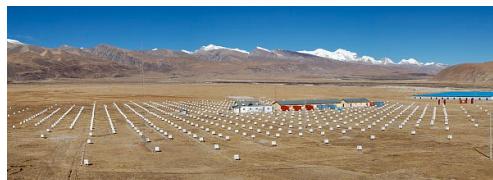


Chandra



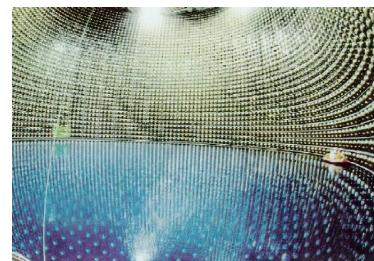
Parkes

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TIBET

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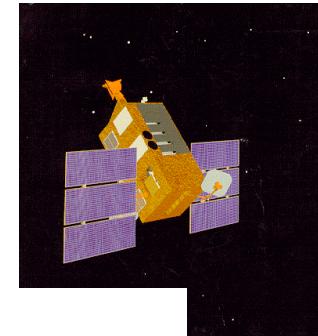
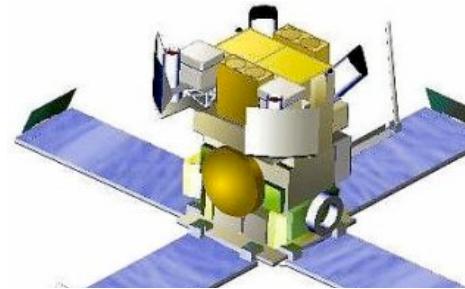
SuperKamiokande

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SDSS

# Triggered search

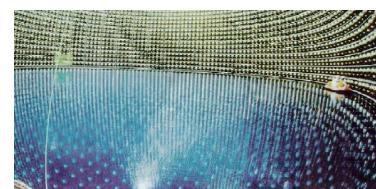


- High energy events are potentially G.W. sources for detection.
- The detection of G.W. can be enhanced by coincidences with electromagnetic observations:  
GRB, SGR, Pulsar glitch, LMXB, Supernova
- Particularly, when a pulsar glitch is observed, we may predict when it occurs next theoretically(Ito(1983))
  - > can adjust the observation schedule to the predicted event.
- Detection efficiency can be increased
  - Time coincidence -- specify data to analyze
    - > sophisticated analysis
  - Source location
    - accurate recovery of waveforms
    - > extract astrophysical parameters-Newton



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TIBET



SuperKamiokande

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SDSS

# Gravitational wave detector network



# Gravitational wave detector network



- When gravitational waves arrive at the earth, the signals are encoded into output of each detector.
- For data analysis to extract the signals,
  - how to combine these data streams from the detectors?
  - how to recover the signal waveforms to obtain astronomical information?

One approach is coherent network analysis



LCGT



VIRGO

# Coherent network analysis

Natural way to handle networks of detectors

- Use arbitrary # of detectors
- Statistics combines all data streams coherently
- Recovery of polarization waveforms and sky position

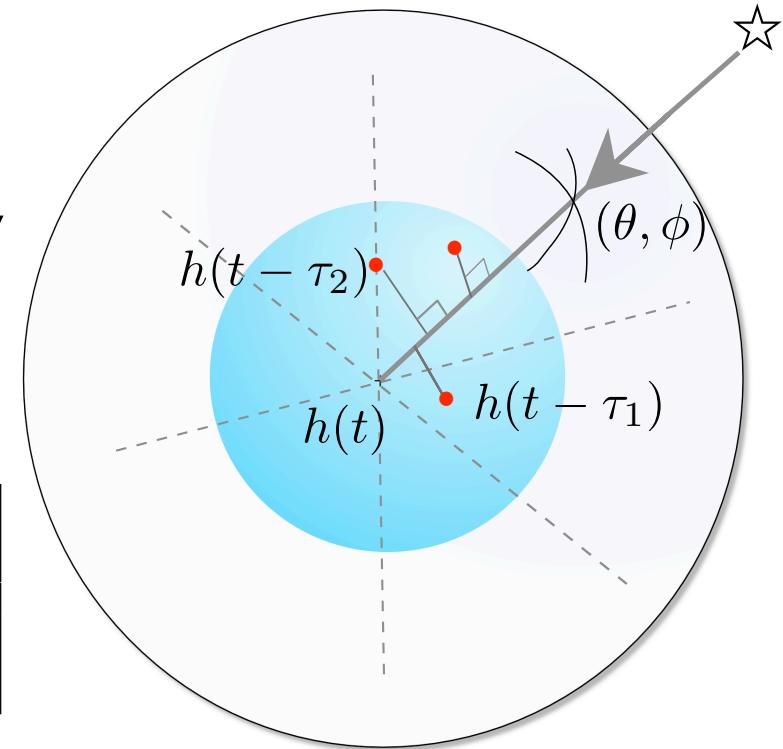
$$\begin{bmatrix} x_1(t) \\ \vdots \\ x_d(t) \end{bmatrix} = \begin{bmatrix} F_{1+}(\theta, \phi) & F_{1\times}(\theta, \phi) \\ \vdots & \vdots \\ F_{d+}(\theta, \phi) & F_{d\times}(\theta, \phi) \end{bmatrix} \begin{bmatrix} h_+(t) \\ h_\times(t) \end{bmatrix} + \begin{bmatrix} n_1(t) \\ \vdots \\ n_d(t) \end{bmatrix}$$

data = response  $\times$  G.W. + noise

$$\text{G.W. } \xi_i(t) = F_{i+}(\theta, \phi)h_+(t) + F_{i\times}(\theta, \phi)h_\times(t)$$

Changing  $(\theta, \phi)$ , look for

$$L = \sum_{i=1}^d \left( \sum_{t=0}^T \| x_i(t) - \xi_i(t + \tau_i, \theta, \phi) \|^2 \right) \rightarrow \text{minimum}$$

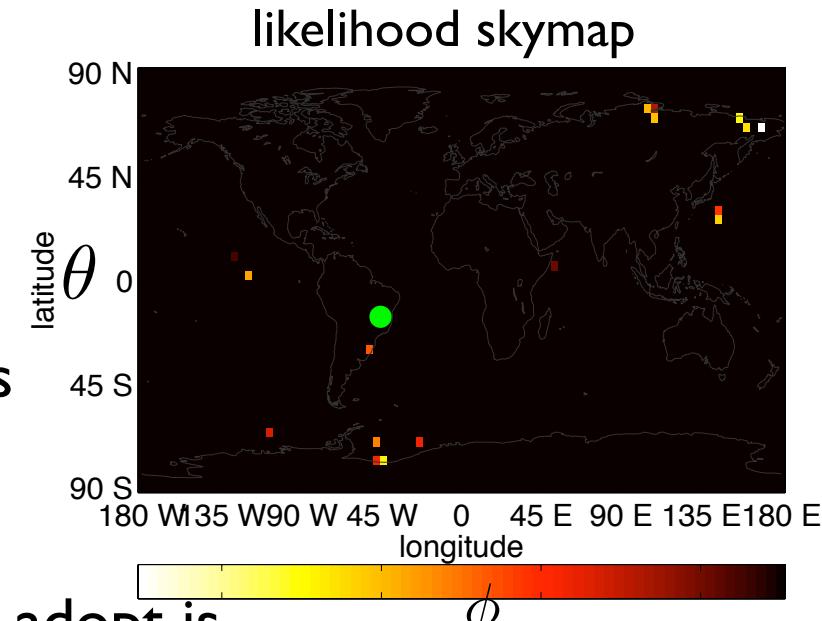


# Tikhonov regularization

$$\begin{bmatrix} x_1(t) \\ \vdots \\ x_d(t) \end{bmatrix} = \begin{bmatrix} F_{1+}(\theta, \phi) & F_{1\times}(\theta, \phi) \\ \vdots & \vdots \\ F_{d+}(\theta, \phi) & F_{d\times}(\theta, \phi) \end{bmatrix} \begin{bmatrix} h_+(t) \\ h_\times(t) \end{bmatrix} + \begin{bmatrix} n_1(t) \\ \vdots \\ n_d(t) \end{bmatrix}$$

$F_+(\theta, \phi)$      $F_\times(\theta, \phi)$

- Detection of G.W. is an inverse problem
- Due to the degree of freedom of the response matrix, the problem becomes ill-posed ( When  $F_\times(\theta, \phi) \propto F_+(\theta, \phi)$  , matrix becomes rank deficient.)
- The error in the best-fit solution is amplified



The technique to address this rank deficiency we adopt is  
Tikhonov regularization based approach (**M. Rakhmaonv CQG 23,S673 (2006)**)

$$L_g = \sum_{i=1}^d \left( \sum_{t=0}^T \| x_i(t) - \xi_i(t, \theta, \phi, \tau_i) \|^2 \right) + g\Omega[h]$$

Impose regulator on standard maximum likelihood statistic

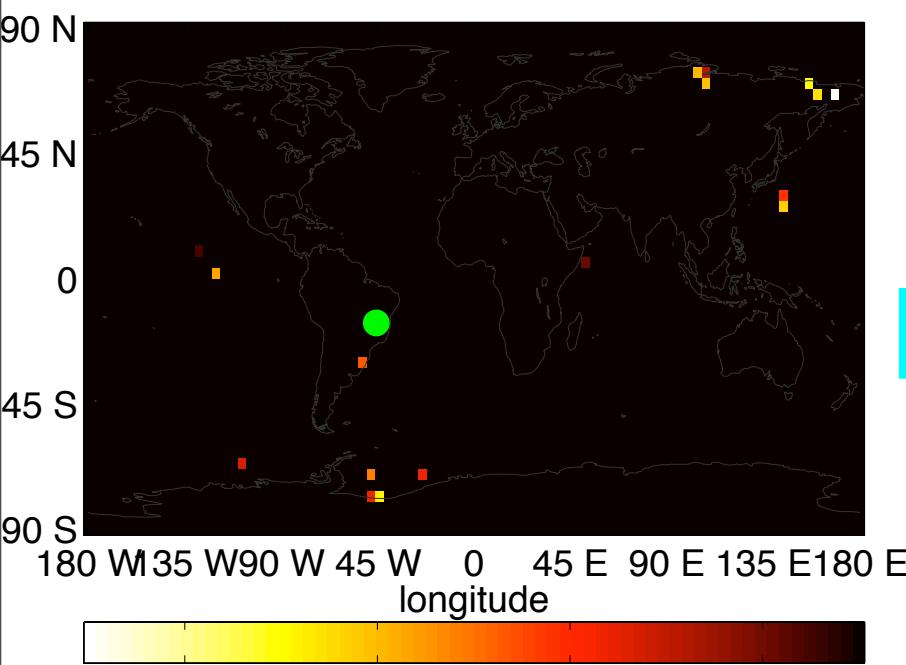
similar approach:

Klimenko et al PRD 72, 122002 (2005)

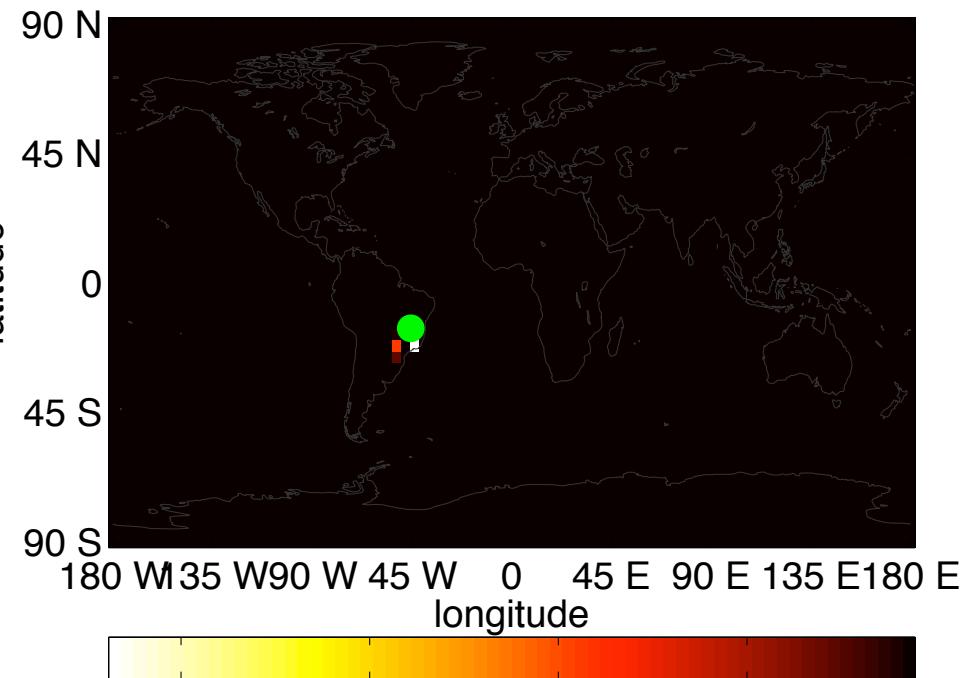
Mohanty et al CQG 23 (2006)

# Effect of regulator

no regulator



with regulator



Without regulator, likelihood values beyond a given threshold are scattered widely.

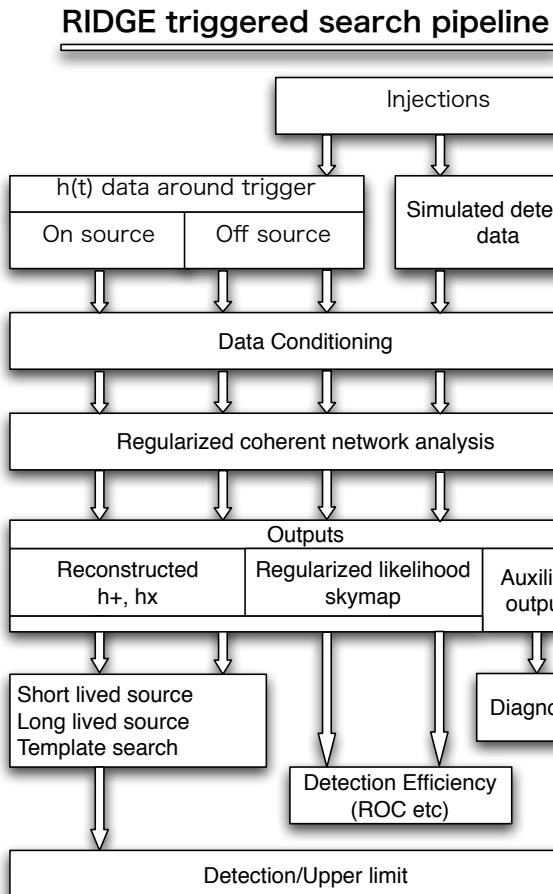
After adding regulator, the values are converged around the true solution.

# RIDGE pipeline

-- fully coherent network analysis pipeline --

Project Page: <http://phys.utb.edu/~kazu/RIDGE>

## Flow chart



- Target : triggered/untriggered search
- Pipeline consists of
  - data conditioning
  - coherent network analysis
- The codes have been fully implemented.
- Currently analyzing LIGO/GEO/VIRGO data:
  - Search for G.W. bursts
  - Understanding various glitches

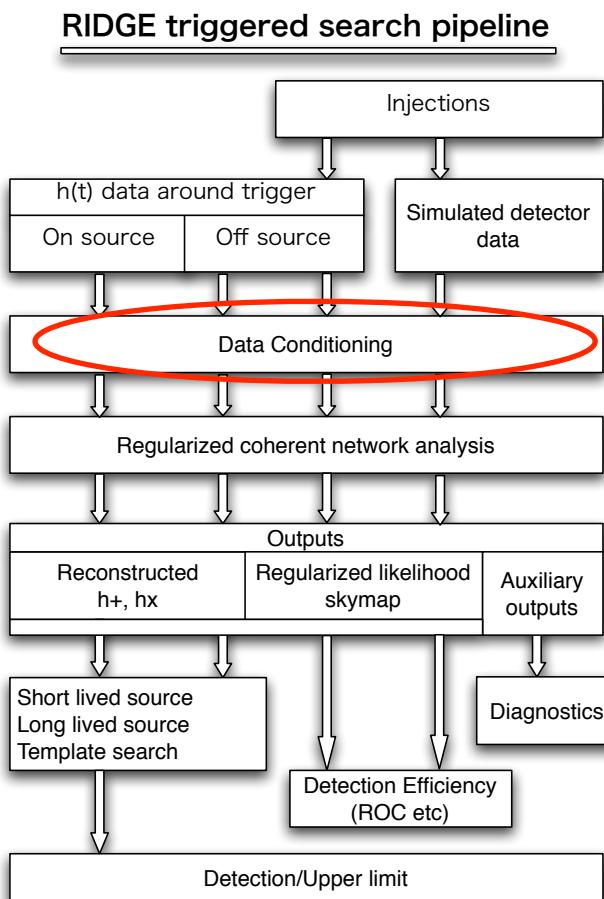
Note:

glitch :A large amplitude noise transient

# RIDGE pipeline

-- fully coherent network analysis pipeline --

Project Page: <http://phys.utb.edu/~kazu/RIDGE>



Feature:

- New data conditioning
- Tikhonov-regularized coherent network analysis

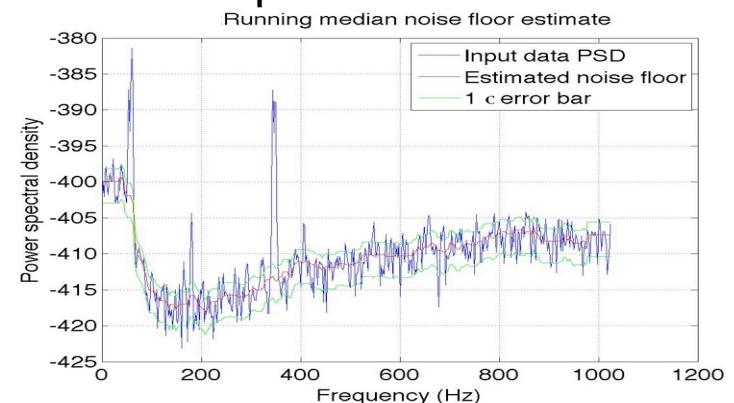
- Time domain noise floor whitening

**S. Mukherjee CQG 21  
(2004) S1783**

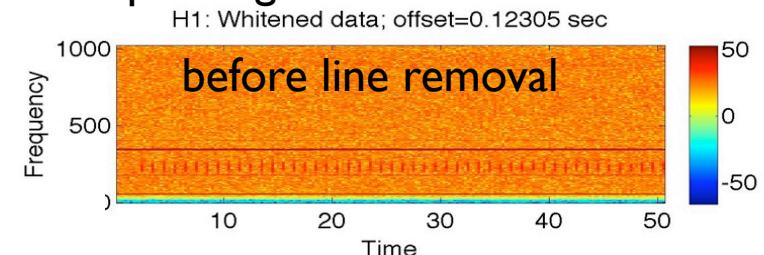
- Remove lines by Median Based Line Tracker

**S. Mohanty CQG 19  
(2002) I513**

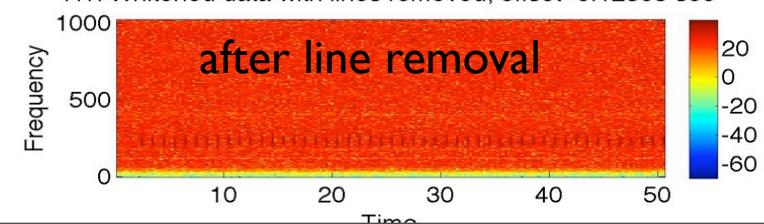
Power spectrum of simulated data

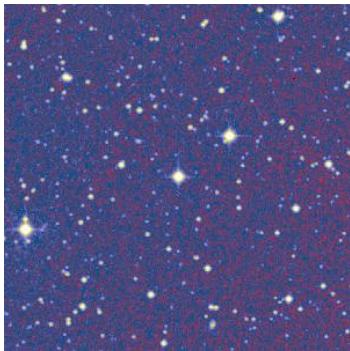


Spectrogram



H1: Whitened data with lines removed; offset=0.12305 sec





# One application of RIDGE

## Monitoring Sco X-1

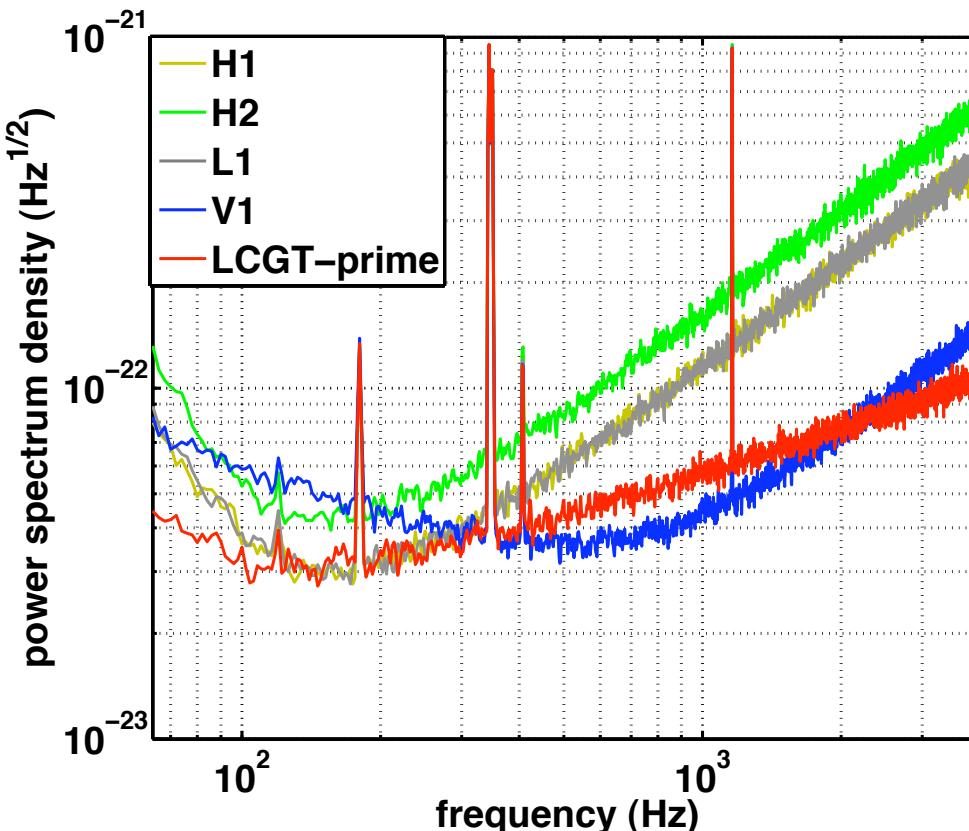
-- *with some combinations of detectors --*

- Sco X-1 is the strongest X-ray source, and has frequent X-ray outbursts
- G.W. observation can derive constraints on accretion or r-mode
- Sensitivities of detectors to Sco X-1 changes in time due to the rotation of the detector antenna patterns.
- Which detector combination is effective for detection?
  - Detection efficiency
  - Signal recovery
  - Here we consider H1-H2-L1,H1-H2-L1-V1,H1-L1-V1-LCGT combination

# Monte Carlo Simulation

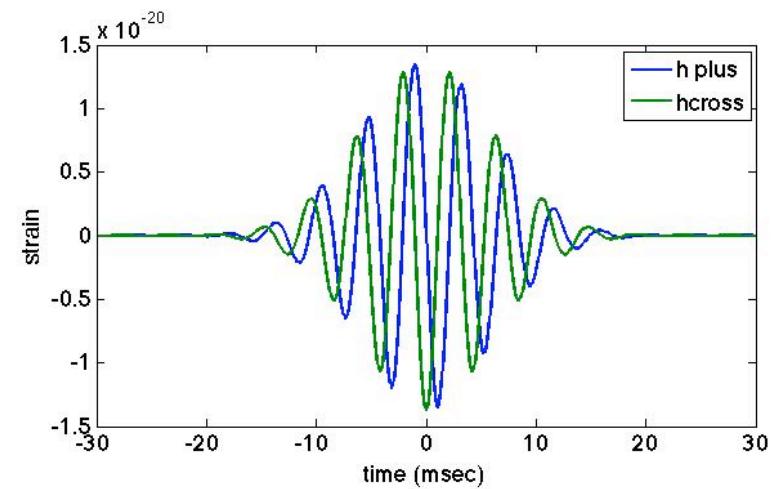
## Simulated data

- H1,H2,L1,V1 design sensitivity
- LCGT-prime: x10 worse than design
- Gaussian noise
- 16384Hz sampling
- 2000sec
- Lines are at same position for all ifo



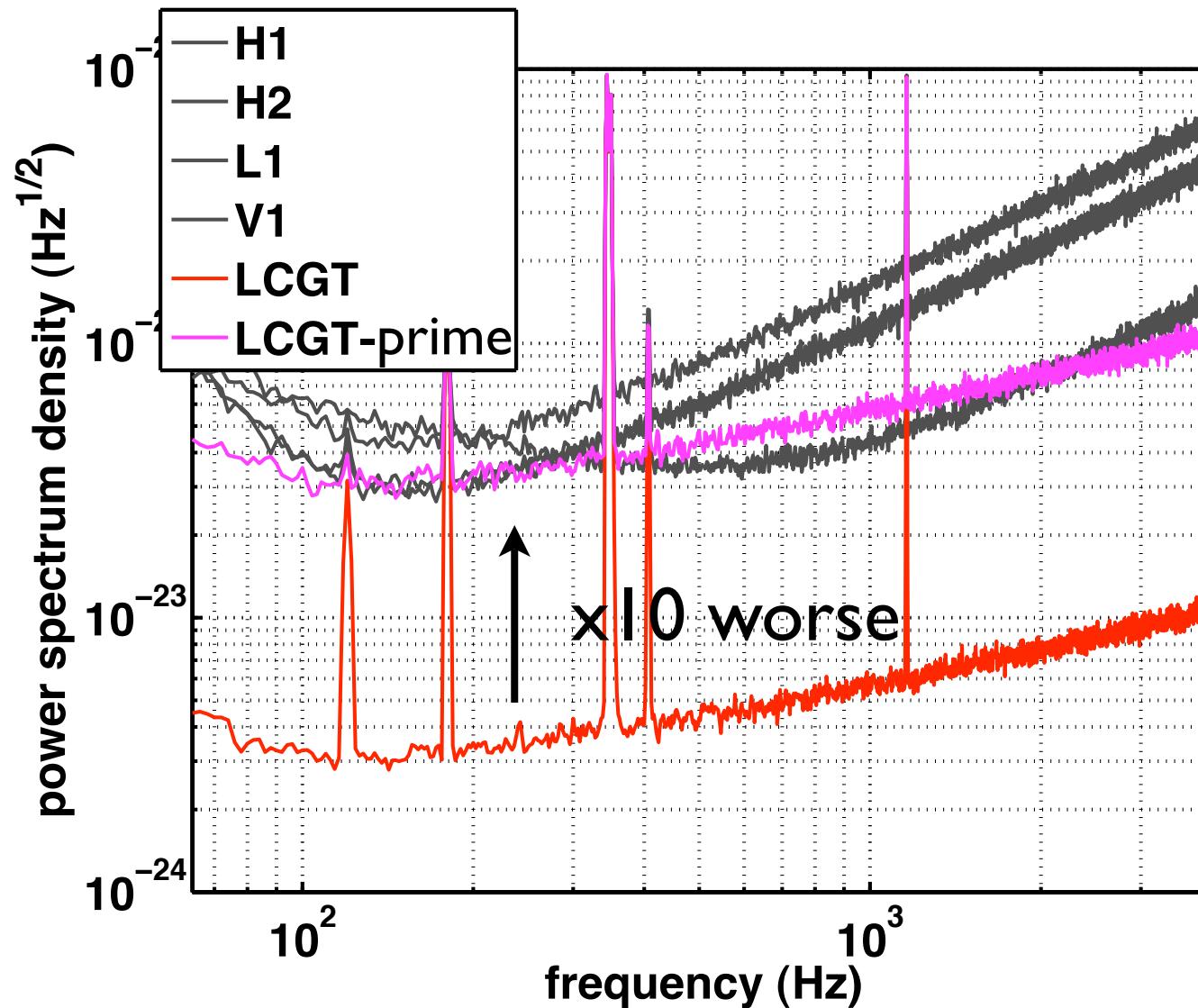
## Injected signal:

- SineGaussian(235Hz)
- Skylocation: ScoX1
- hrss=2x10<sup>-21</sup> Hz<sup>1/2</sup>



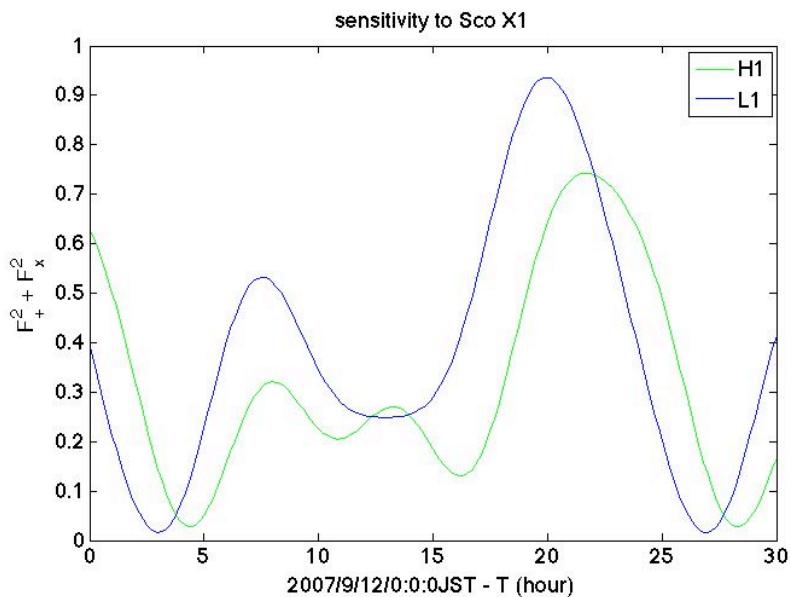
# Monte Carlo Simulation

To focus on importance of detector location, use sensitivity  $\times 10$  worse than the design sensitivity of LCGT.



# Sensitivity to Sco X-1

H1 - L1



y-axis:

detector response :  $F_+(\theta_s, \phi_s)^2 + F_\times(\theta_s, \phi_s)^2$   
to the location of Sco X-1( $\theta_s, \phi_s$ )

x-axis:

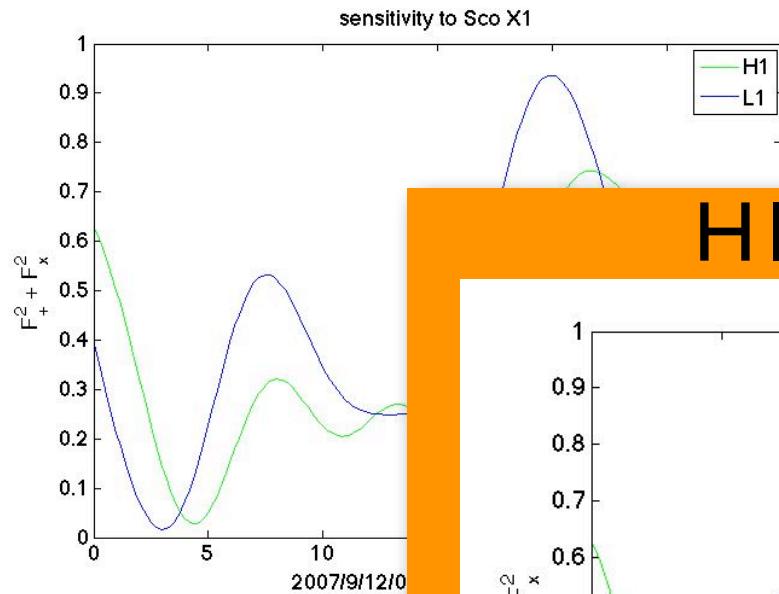
hour from 0:00(JST), today

Due to the rotation of the earth, the response function is 24hr-periodic function.

LIGO only network has sensitivity at the region T = 17-24hr.  
However, T=2-5hr, 10-16hr, the sensitivity worsens

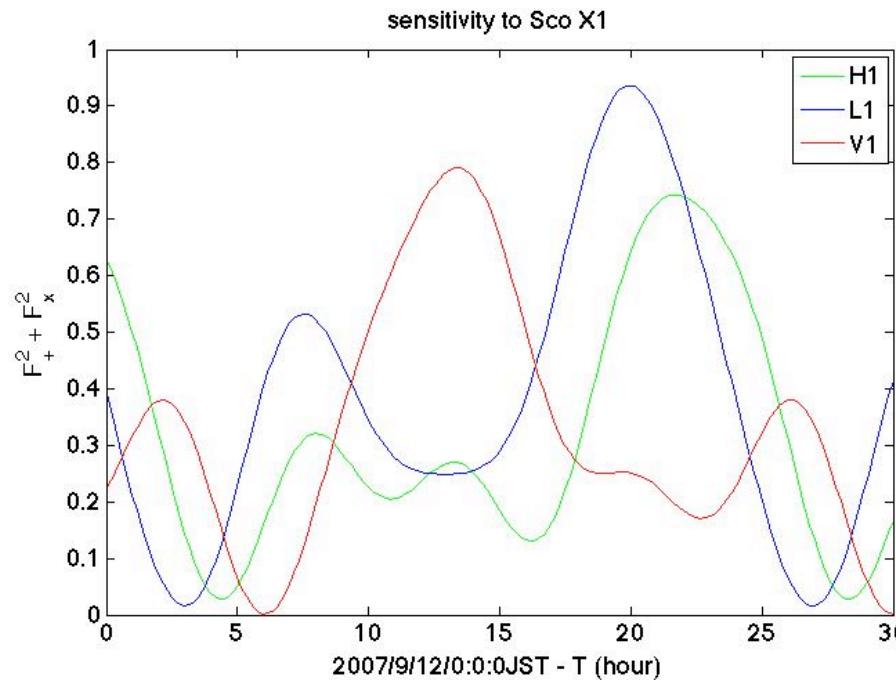
# Sensitivity to Sco X-1

H1,H2 - L1



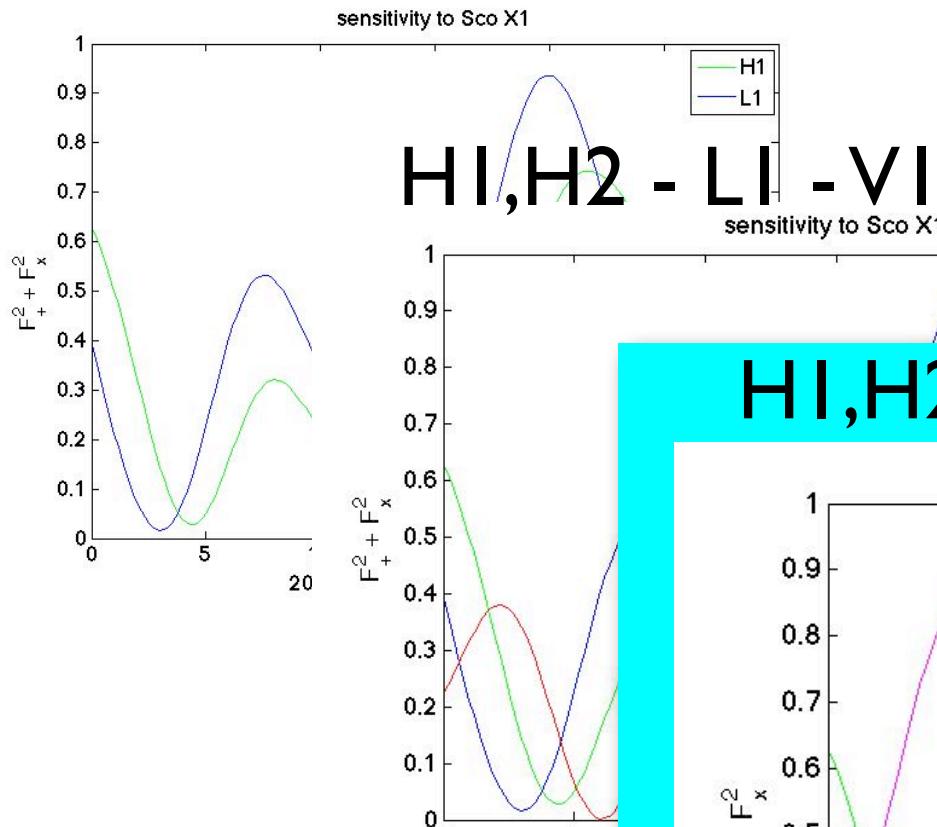
Adding VIRGO to the LIGO network, the sensitivity at the region T=10-16hr is improved.

H1,H2 - L1 - V1



# Sensitivity to Sco X-1

H1,H2 - LI



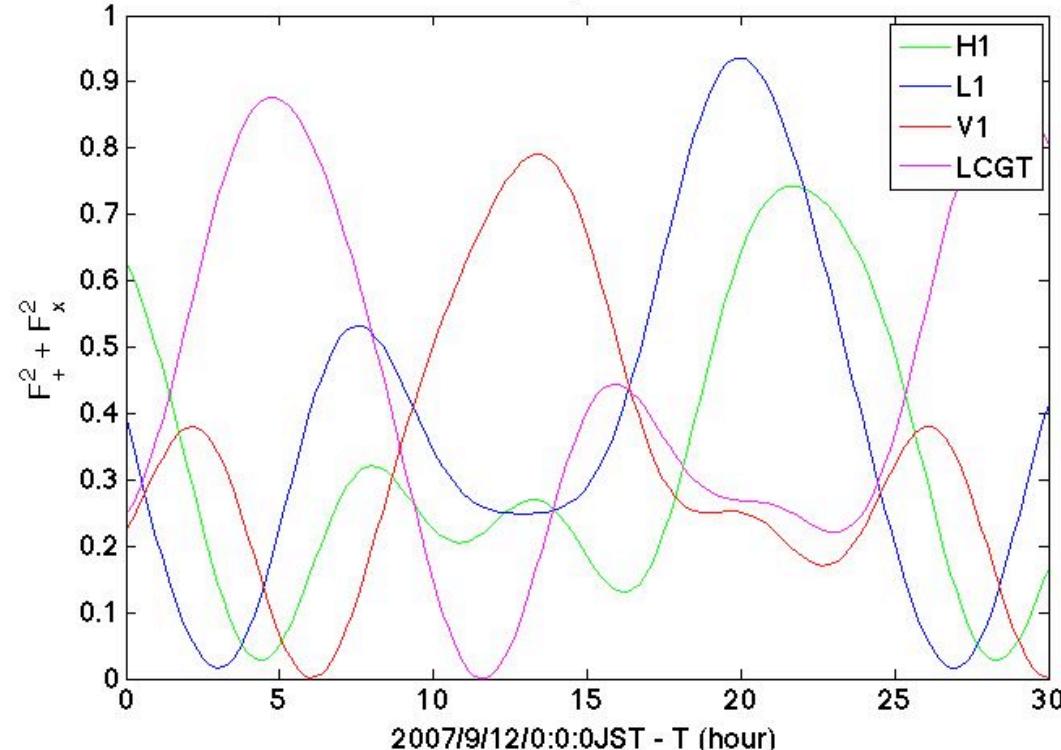
The network covers all region.

H1,H2 - LI - VI

sensitivity to Sco X1

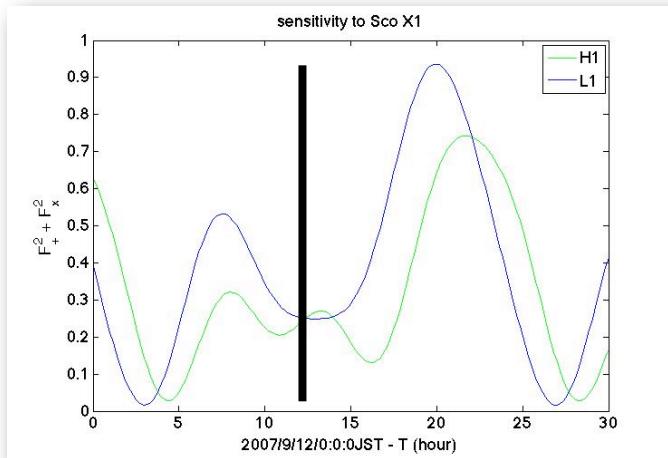
H1,H2 - LI - VI - LCGT

sensitivity to Sco X1

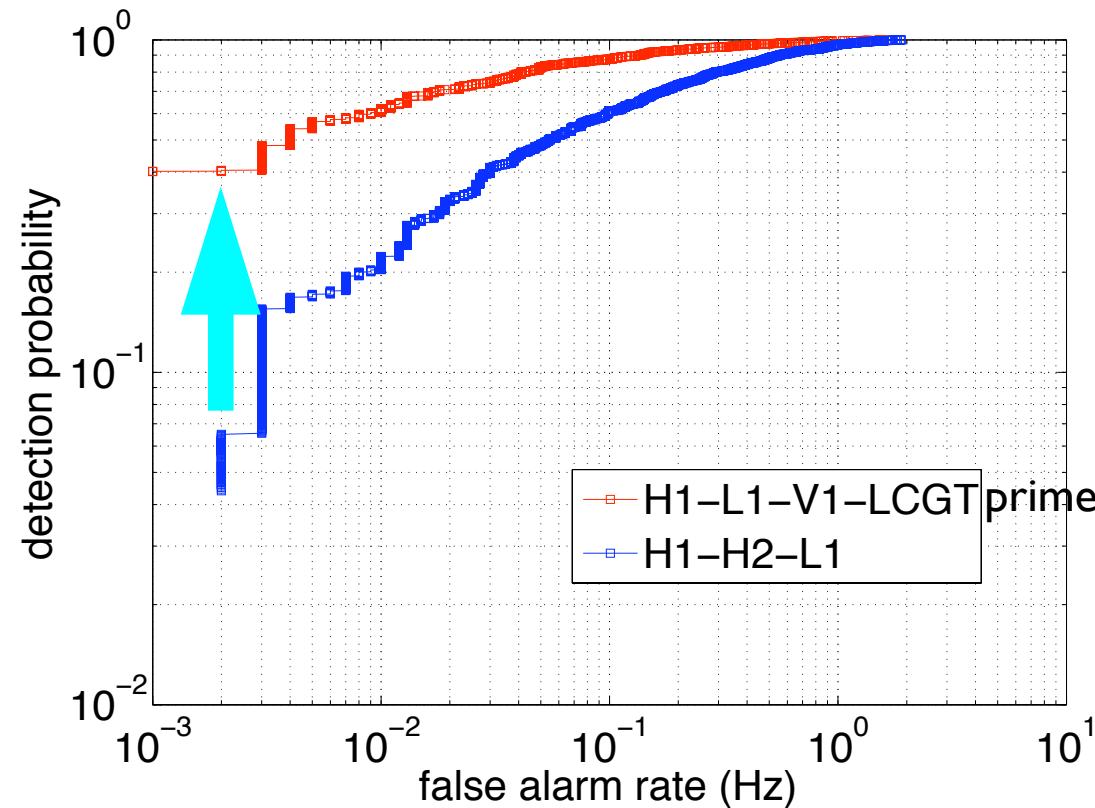
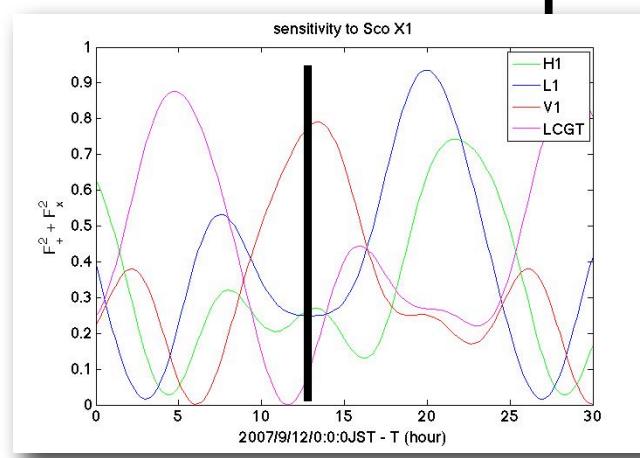


# Detection efficiency

H1+H2+L1



H1+L1+V1+LCGT-prime



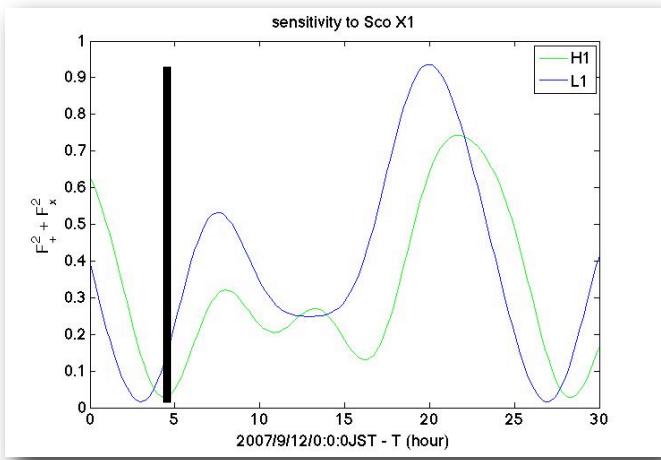
VIRGO compensate the low sensitivity region for LIGO network.

Detection probability  
@false alarm rate 0.01Hz

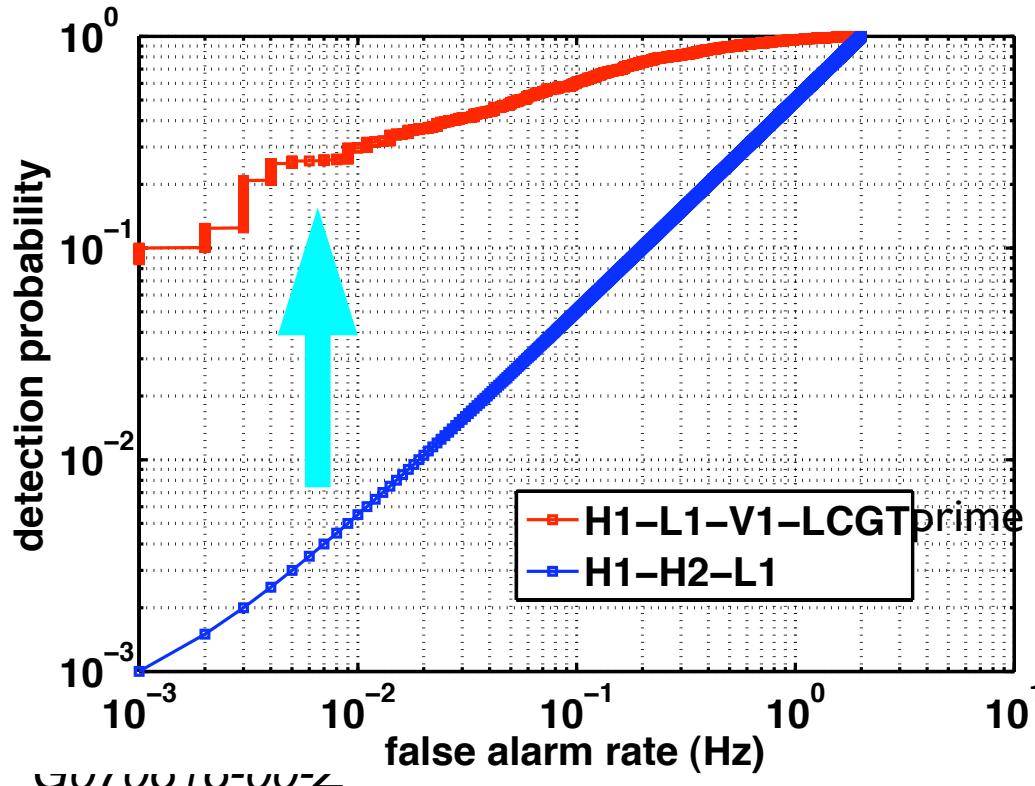
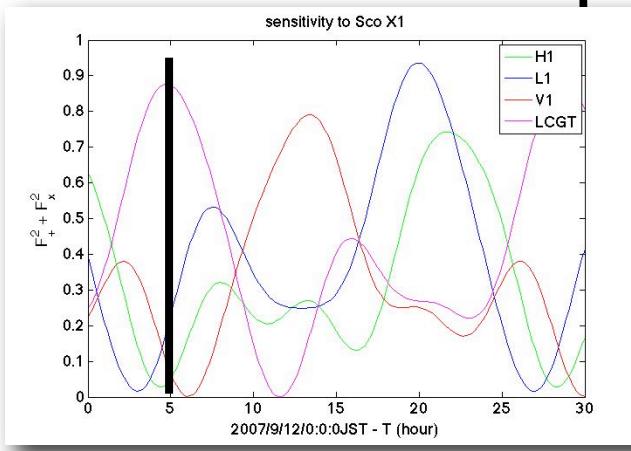
20% -----> 60%

# Detection efficiency

H1+H2+L1



H1+L1+V1+LCGT-prime



LCGT compensates the low sensitivity region for LIGO-VIRGO network.

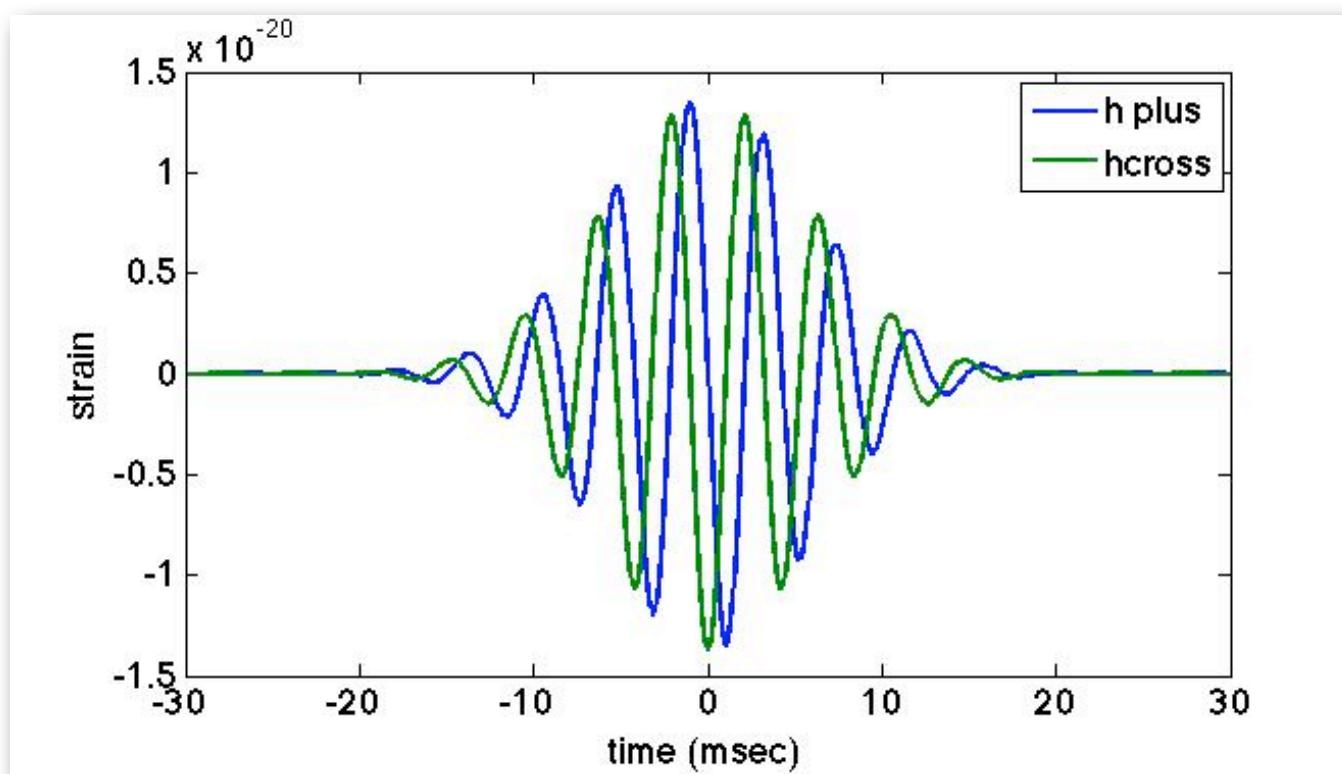
Detection probability  
@false alarm rate 0.2Hz

less 10% -----> 80%

# Reconstruction of G.W. waveforms

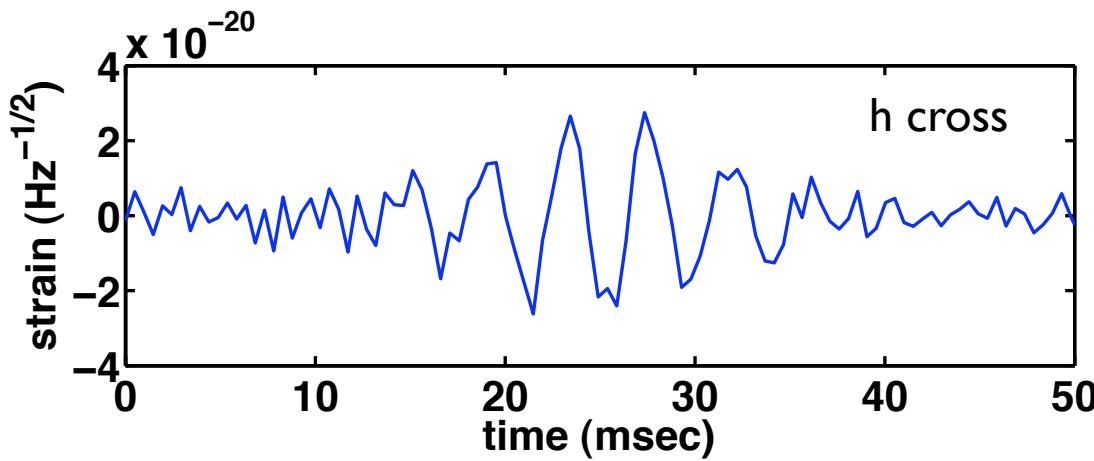
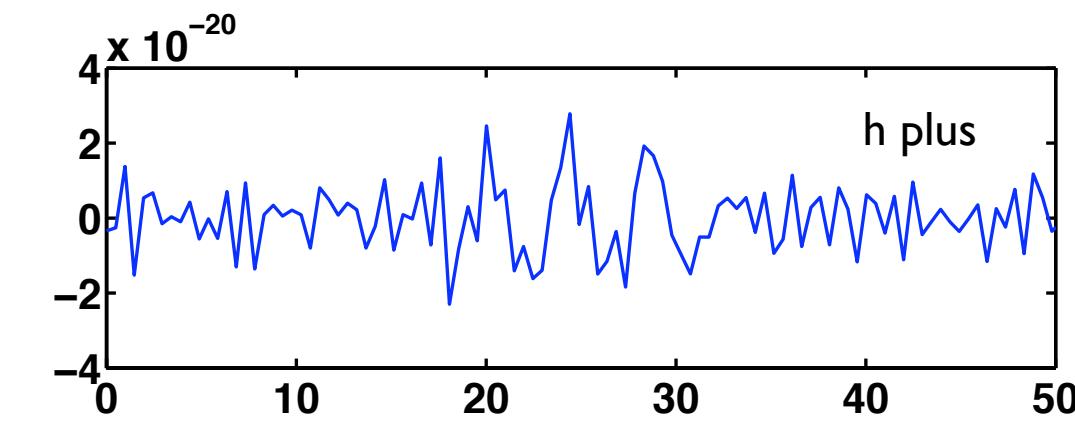
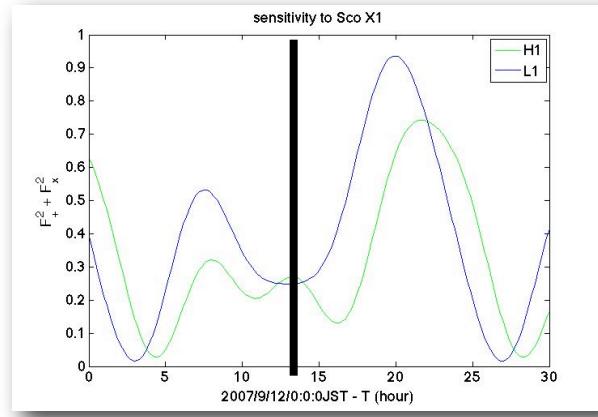
Injected signal:

- Sine Gaussian of the central frequency 235Hz
- $h_{rss} = 2.8 \times 10^{-21} \text{ Hz}^{1/2}$



# Reconstruction of G.W. waveforms

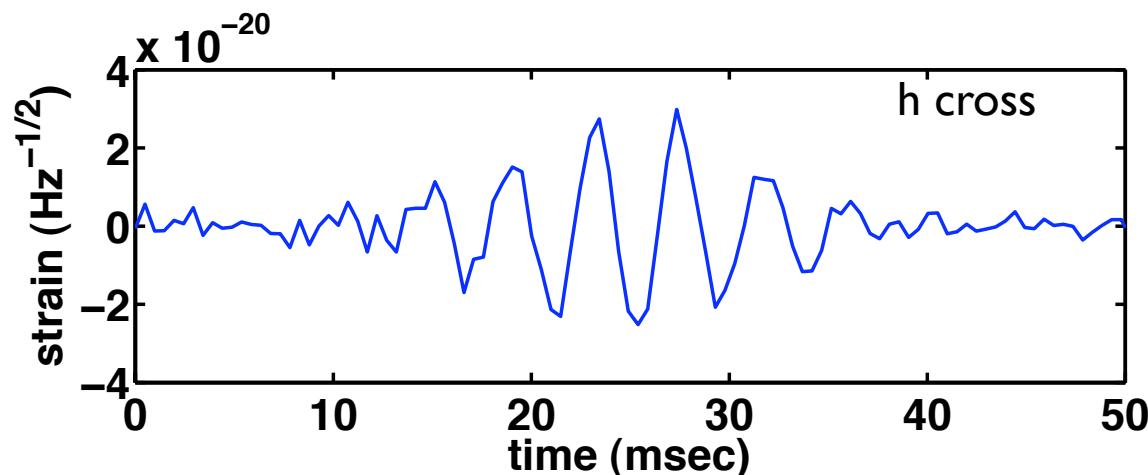
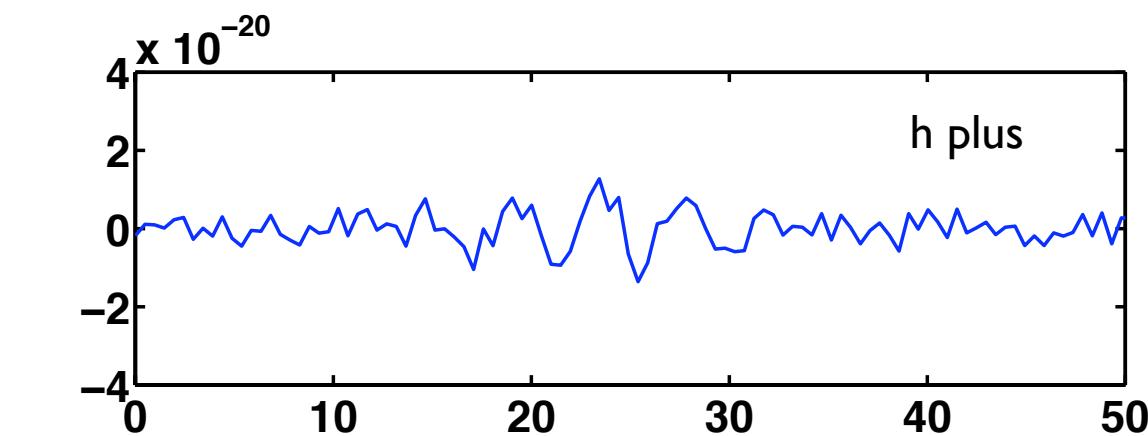
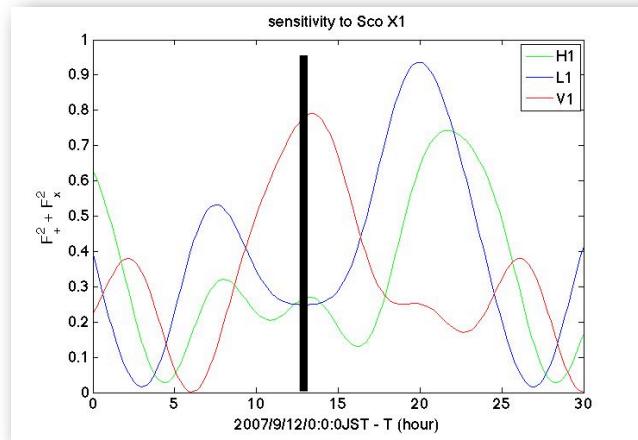
H1+H2+L1



G070616-00-Z

# Reconstruction of G.W. waves

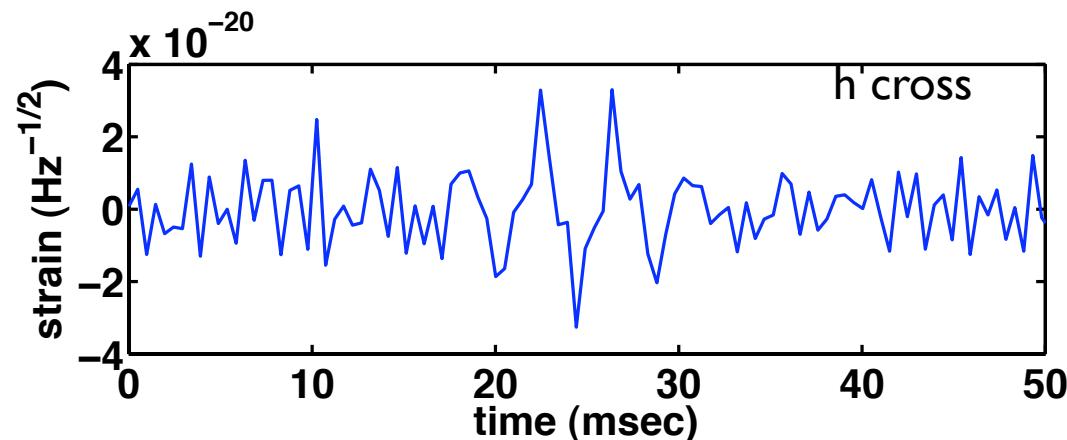
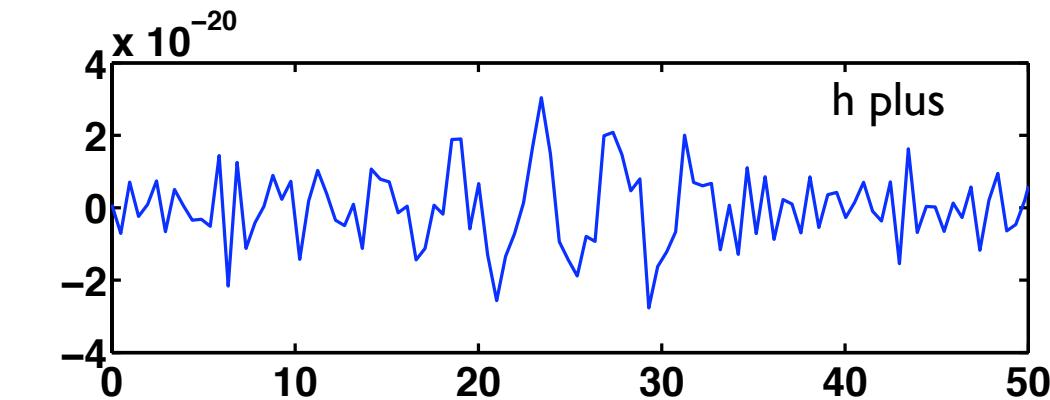
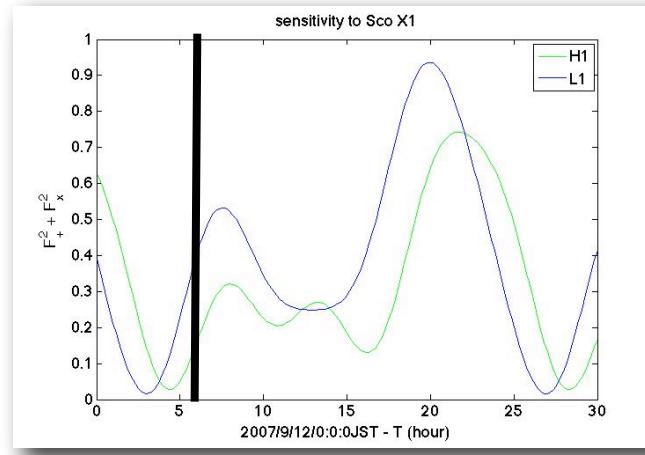
H1+H2+L1+V1



G070616-00-Z

# Reconstruction of G.W. waves

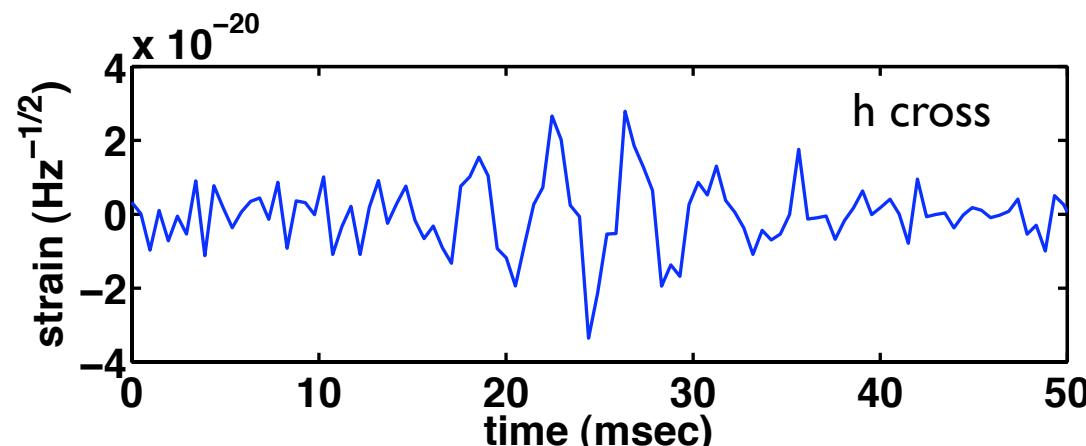
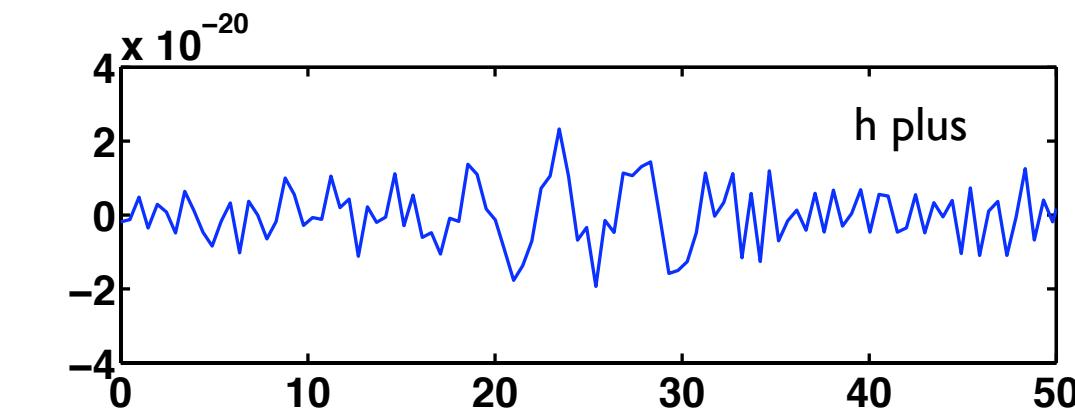
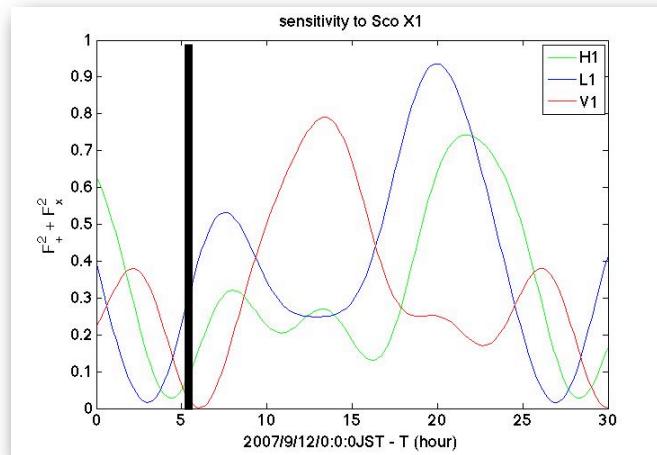
H1+H2+L1



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# Reconstruction of G.W. waves

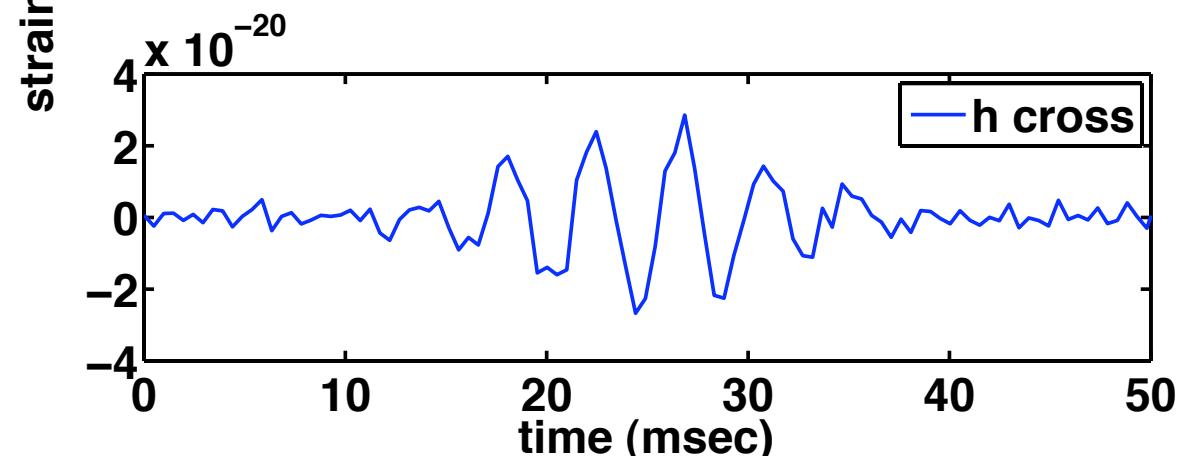
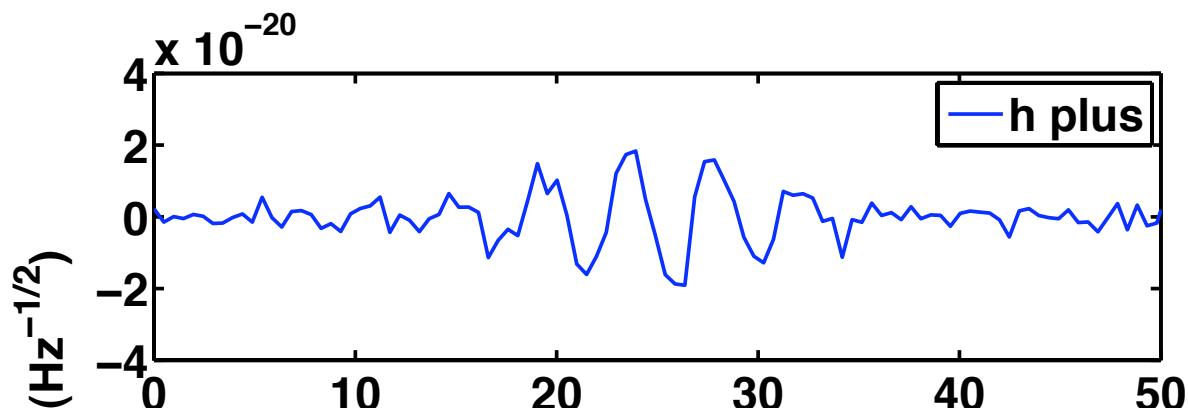
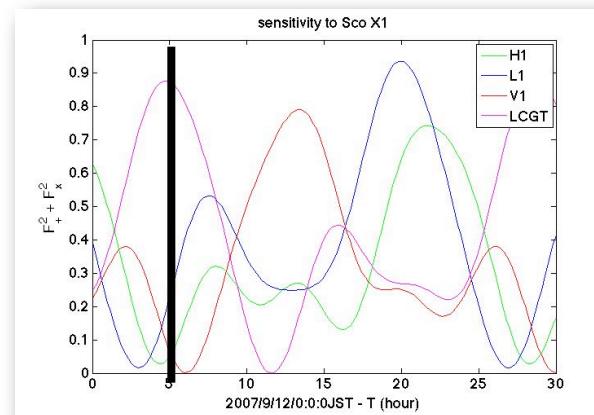
H1+H2+L1+V1



G070616-00-Z

# Reconstruction of G.W. waves

H1+L1+V1+LCGT-prime



G070616-00-Z

# Summary, current status and future plan

## Summary

- The fully coherent network analysis pipeline called “RIDGE” has been developed.
- Coincidence analysis with electro-magnetic observations give us
  - timing information --> more sophisticated analysis
  - source location --> accurate signal recovery and constrain astrophysical parameters
- Sensitivities of some detector combinations and signal recovery are presented

## Current status

- Pulsar glitches during S5 are being analyzed
- Start monitoring Sco X-1
- Various detector noise transients are being analyzed

## Future plan

- Set upper limit on some sources
- Understand detector-originated glitches
- Collaboration with various astronomers needed
  - Building alert system which enables quick analysis.

*END*

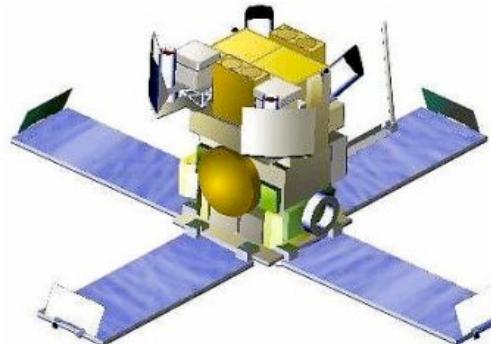


# Triggered search



LIGO

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HETE

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RXTE

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SWIFT

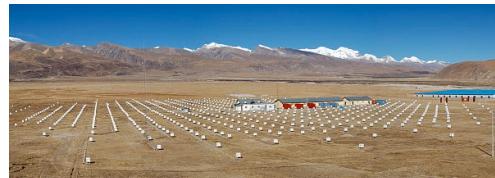


Chandra



Parkes

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TIBET

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AGASA

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SDSS

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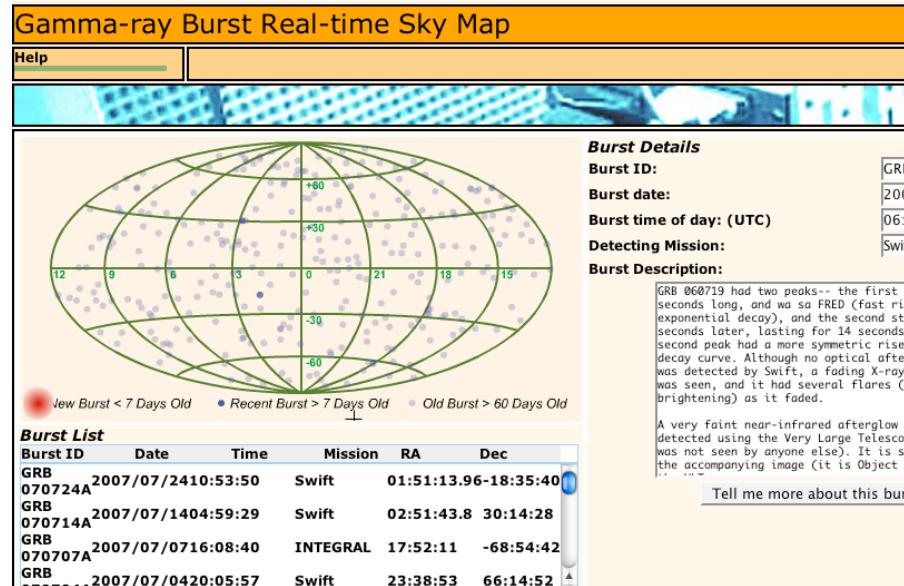
# Gravitational wave detector network



# Analysis procedure

## -- in case of GRB --

### excellent GRB alert system



<http://grb.sonomae.edu/>

# Analysis procedure

-- in case of GRB --

excellent GRB

Gamma-ray Burst Real-time Data

Help

Burst List

Burst ID	Date	Time	Source
GRB 070724A	2007/07/24	10:53:50	SWIFT
GRB 070714A	2007/07/14	04:59:29	SWIFT
GRB 070707A	2007/07/07	01:08:40	INTERLACE
GRB 070704A	2007/07/04	20:05:57	SWIFT

http://gravity.psu.edu/~psurg/grbs/grblist.html

## List of astronomical information and available data

GRB Name	GPS Time	R.A	Declination	Detectors in Science Mode
051105	815207214.000	265.289	34.921	H2
051105B	815223963.000	9.477	-40.481	H2
051109	815533953.000	330.296	40.837	None
051109B	815560792.000	345.440	38.672	None
051111	815723994.000	348.157	18.367	H2
051113	815930568.000	187.222	-26.391	H2
051114	815976703.000	226.274	60.150	H1,H2
051117	816259893.000	228.405	30.870	H1,H2
051117B	816268987.000	85.225	-19.245	H1,H2,L1
051127	817135616.000	223.736	51.340	H1,H2,L1
051210	818228794.000	330.197	-57.634	H1,H2
051211	818304618.000	104.054	32.679	H1,H2,L1
051211B	818373957.000	345.688	55.079	H1,H2,L1
051213	818493197.000	252.123	-59.207	H1,H2,L1

GPS time

sky position

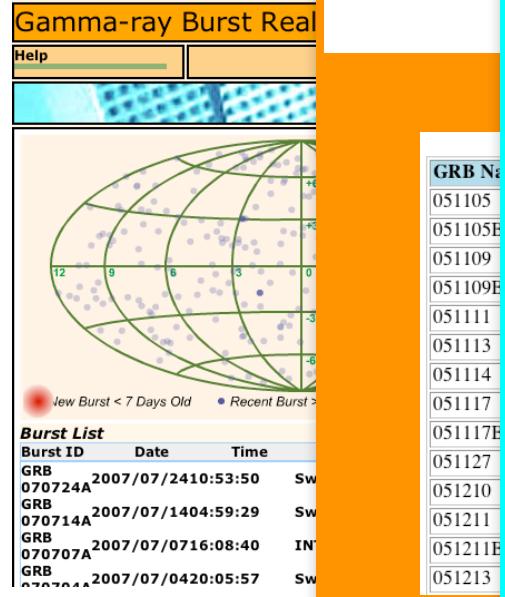
detectors  
on science mode

<https://gravity.psu.edu/~psurg/grbs/grblist.html>

# Analysis procedure

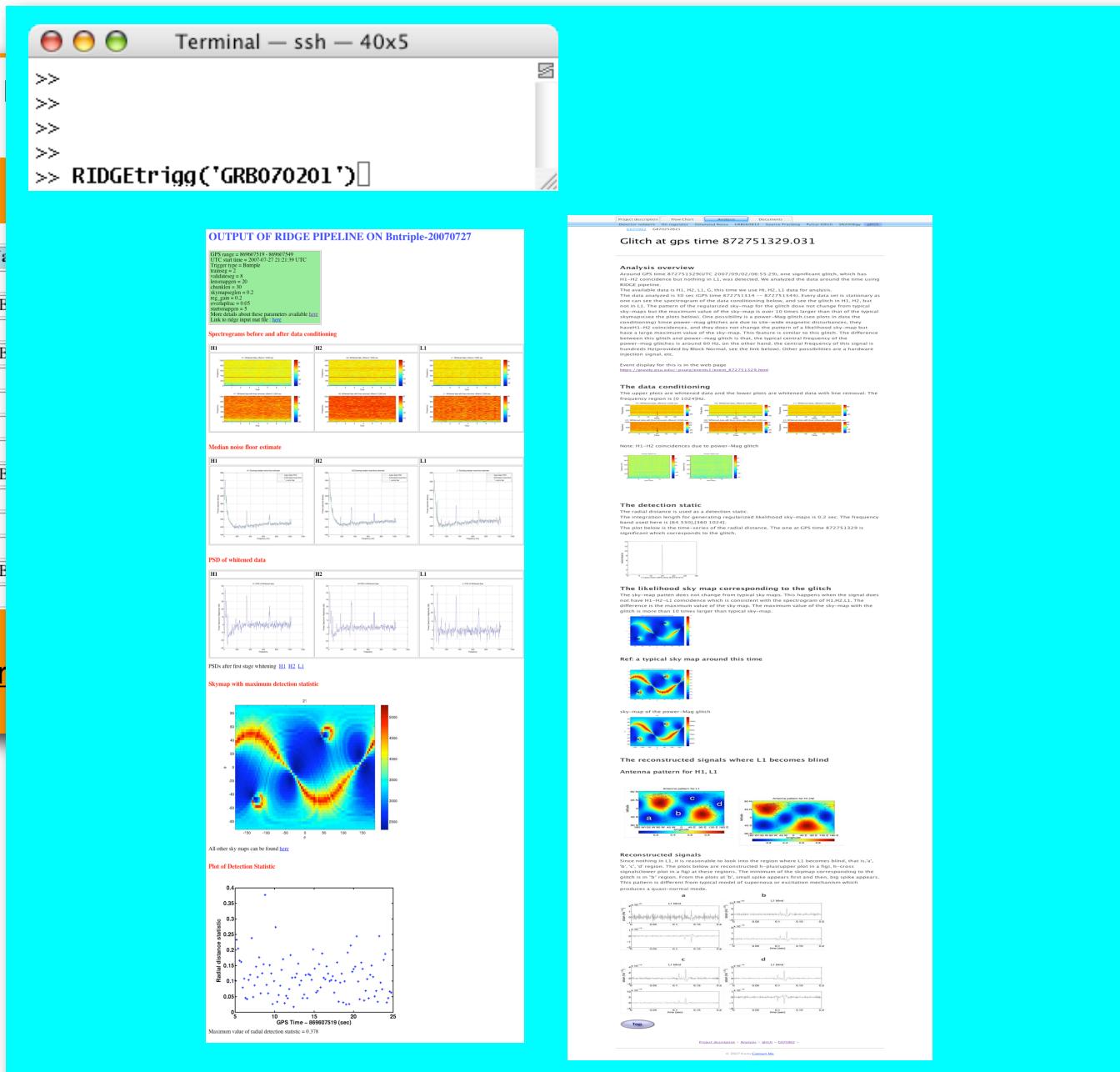
## -- in case of GRB --

excellent GRB detection

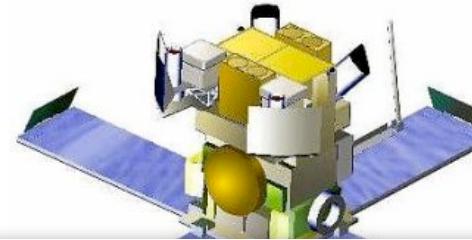
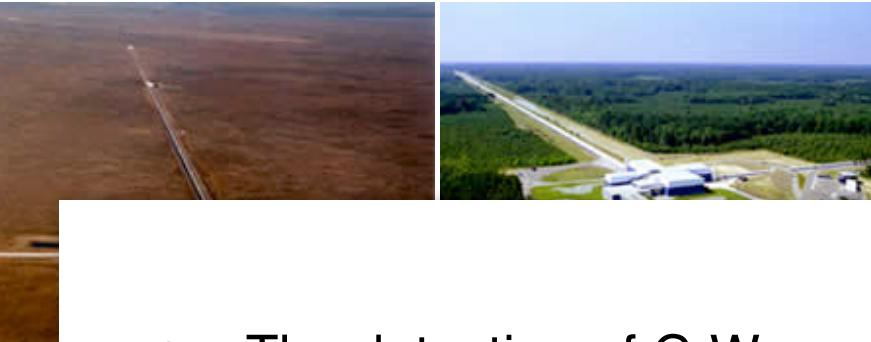


<http://>

<https://grb>



# Triggered search



RXTE  
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Parkes

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G070616-00-Z TIBET



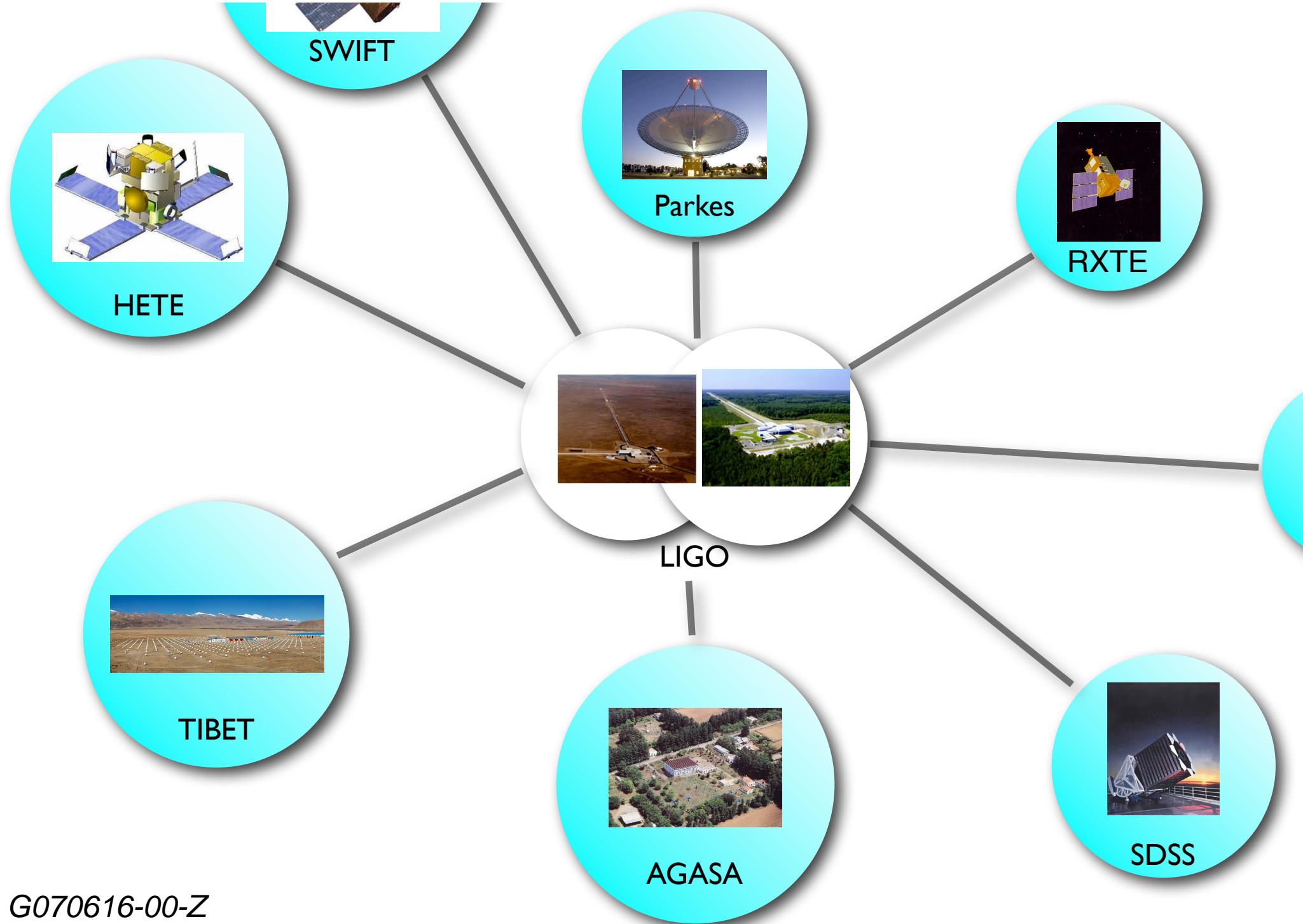
,

AGASA



SDSS

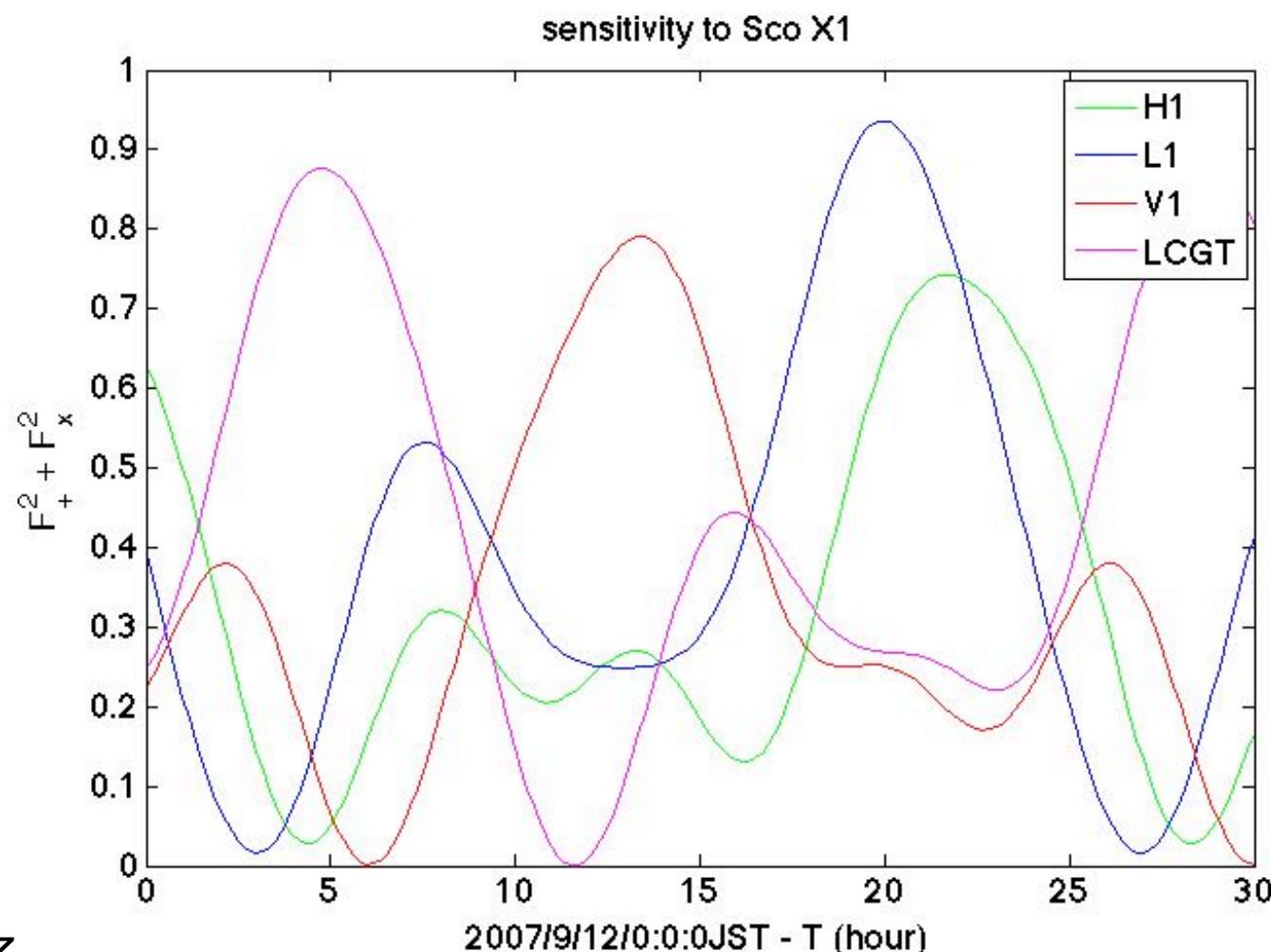
# Triggered search



G070616-00-Z

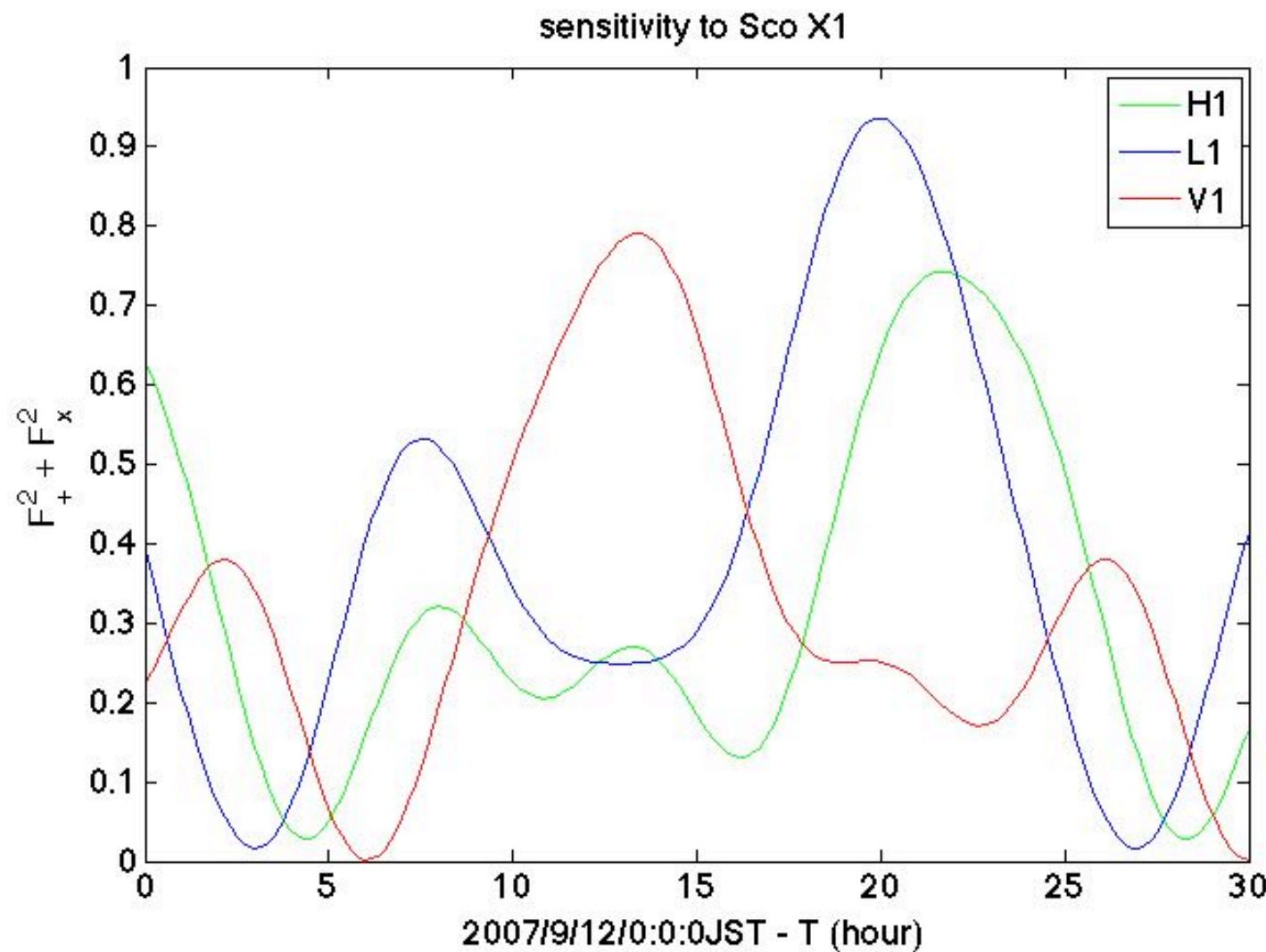
# Sensitivity to Sco X-1

HI - LI - VI - LCGT

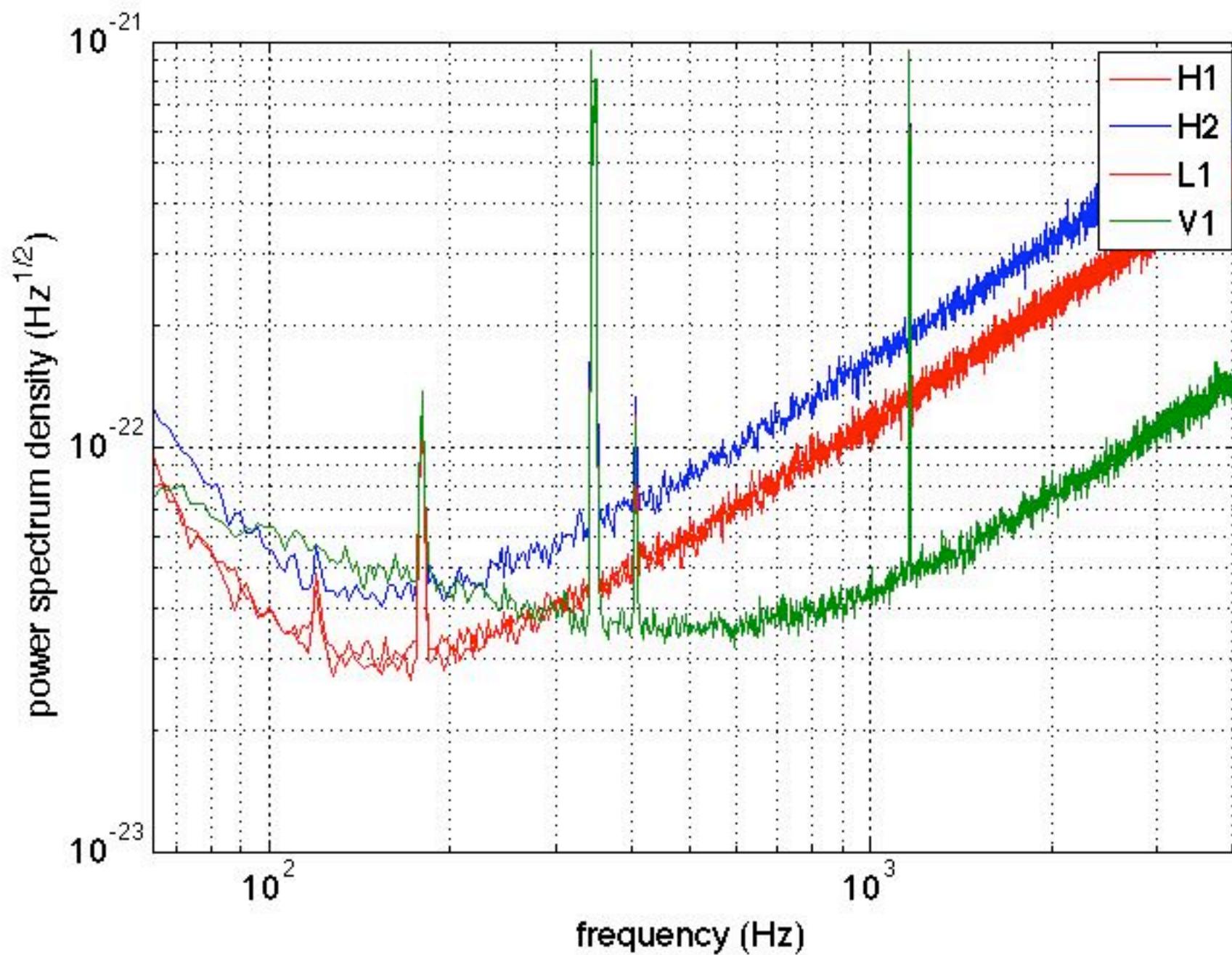


# Sensitivity to Sco X-1

H1 - L1 - V1

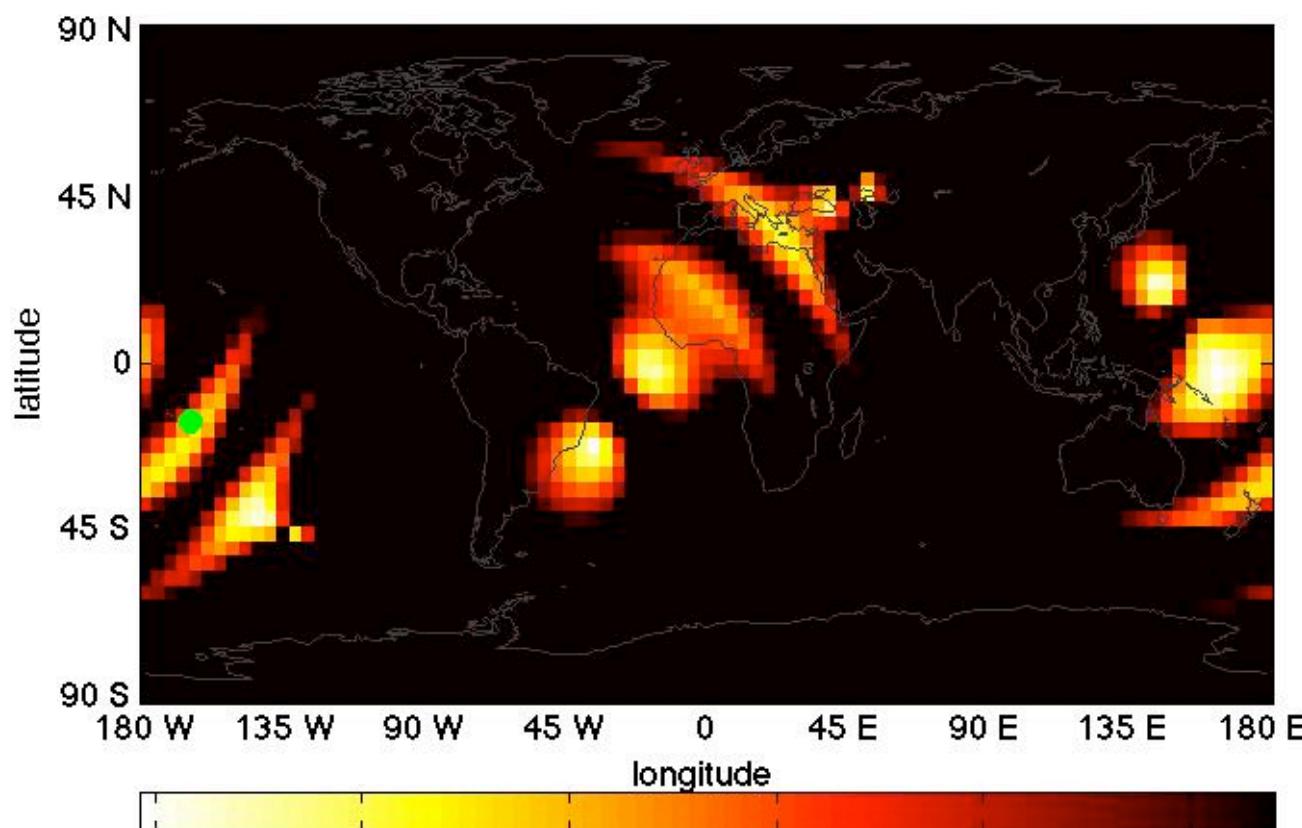
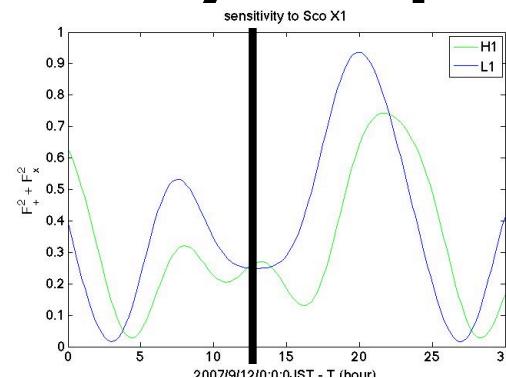


# Simulated data



# skymap

H1+H2+L1

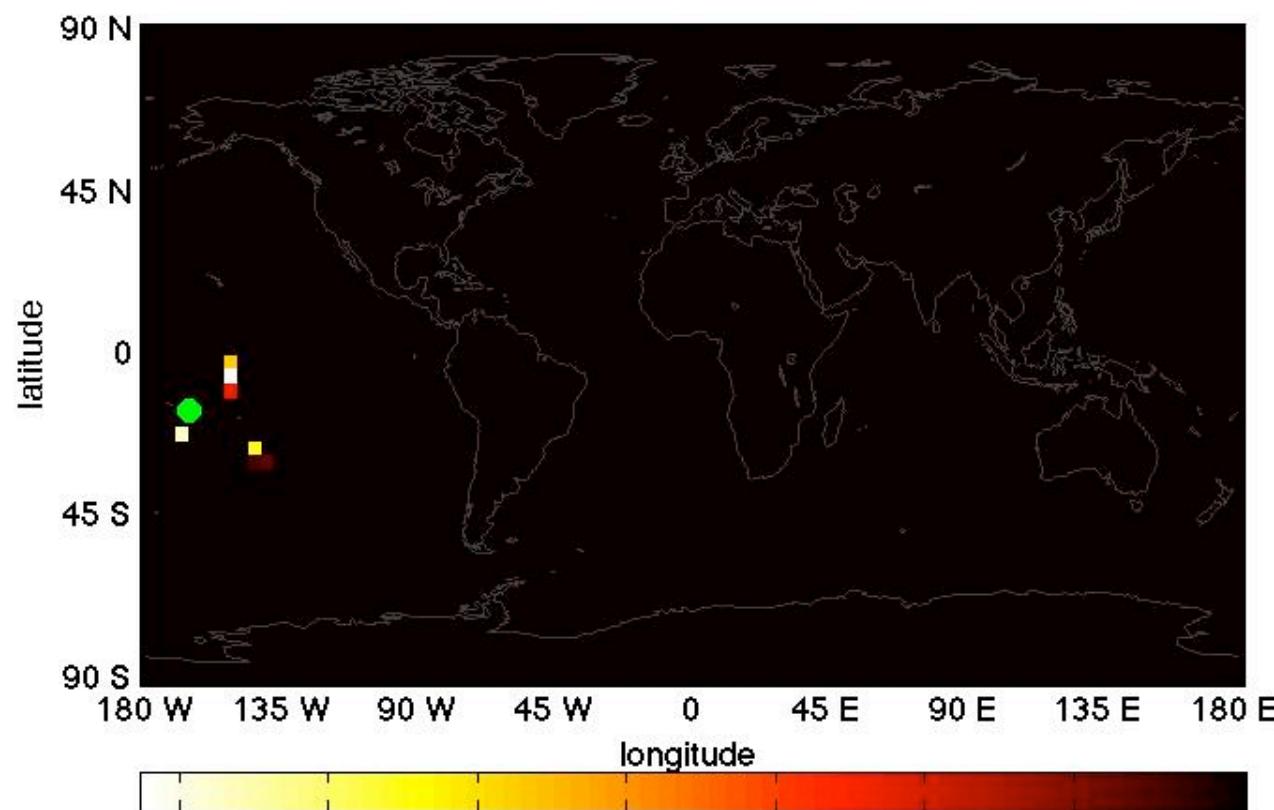
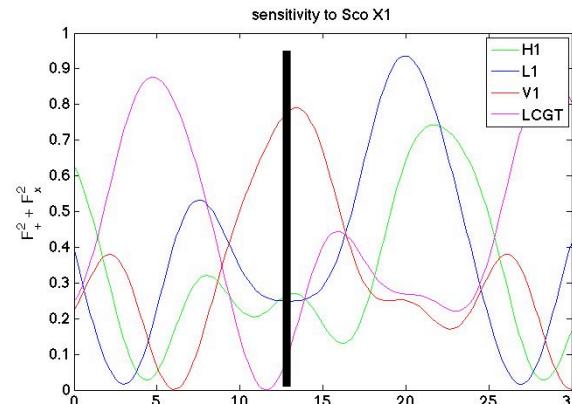


minimum of skymap

1.2 x minimum of skymap

# skymap

H1+L1+V1+LCGT

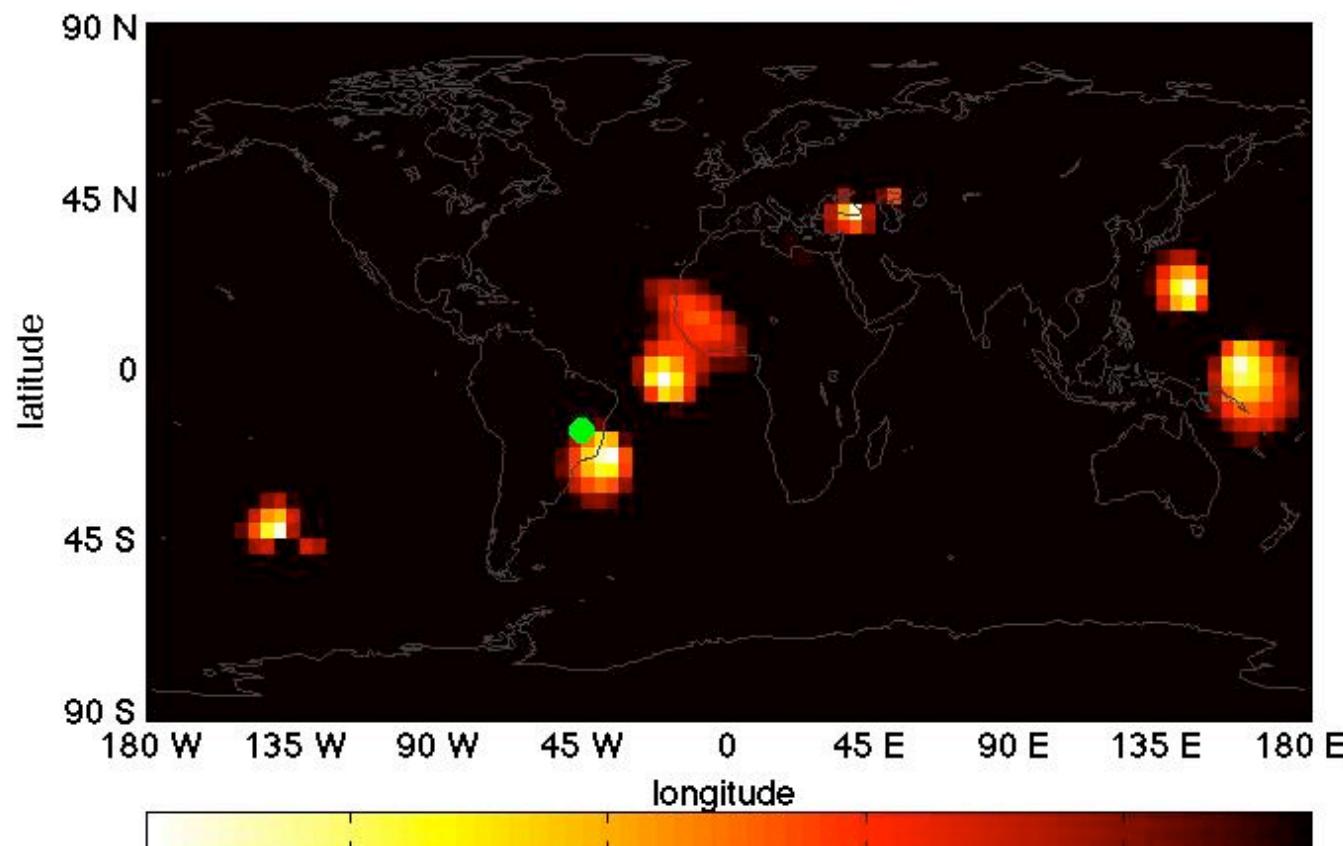
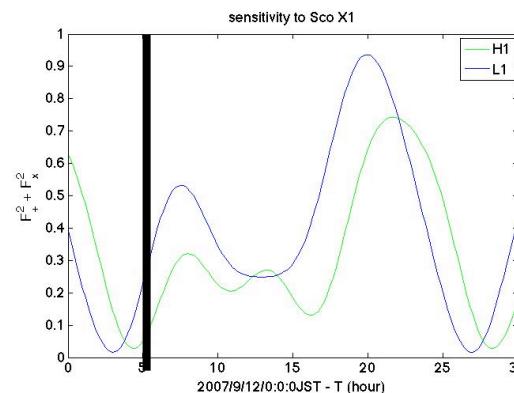


minimum of skymap

1.2 x minimum of skymap

# skymap

H1+H2+L1

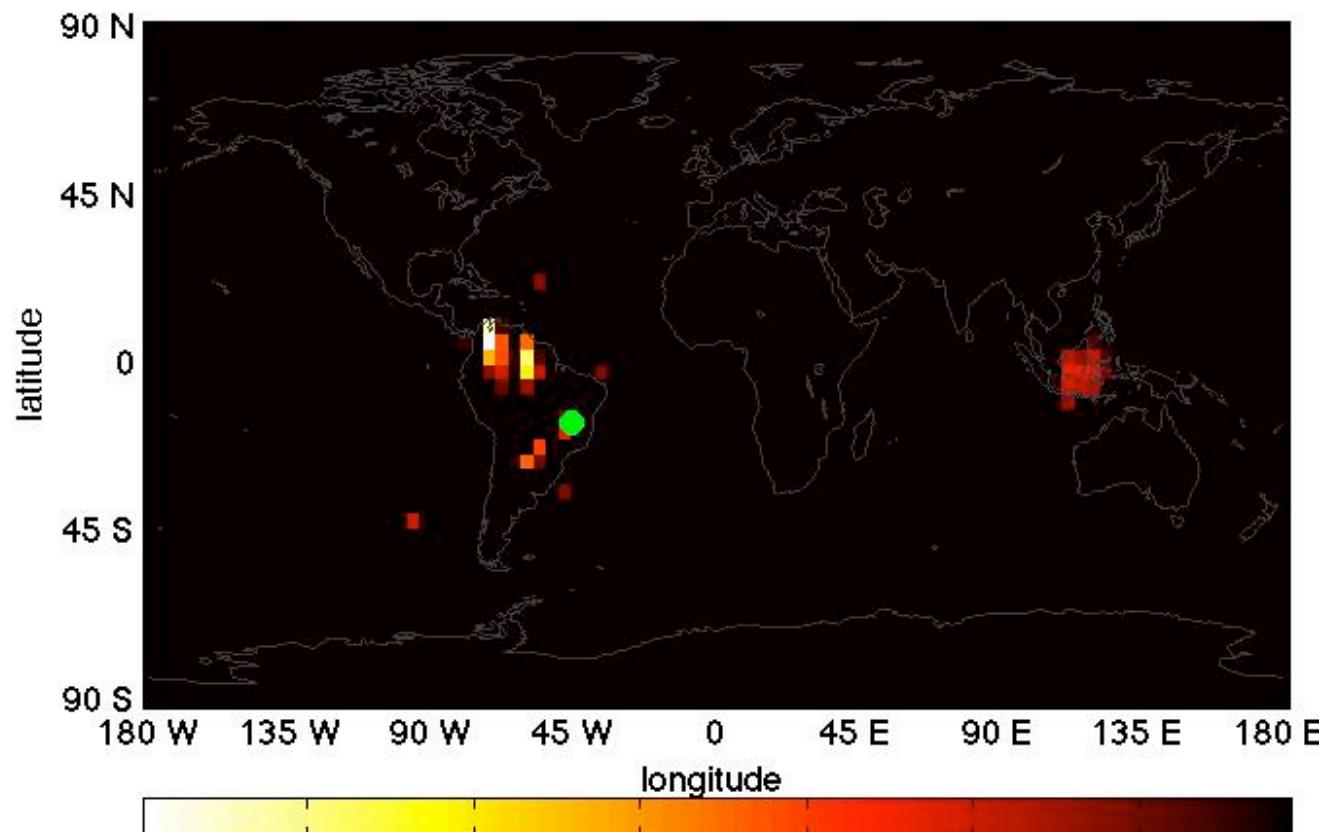
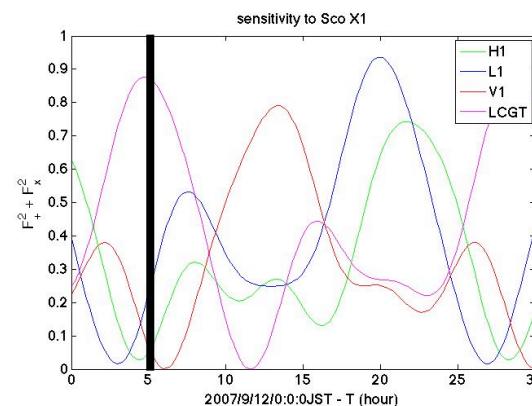


minimum of skymap

1.2 x minimum of skymap

# skymap

H1+L1+V1+LCGT



1.2 x minimum of skymap